



Menoufia University  
Faculty of Electronic Engineering  
Electronics and Electrical Communications Eng. Dept.  
Third Year – Spring 2018  
**ECE 323 - Microwave Engineering**  
**Problem Set #5**



## Rectangular Waveguides

[P1] A rectangular waveguide filled with a dielectric material with  $\mu = \mu_o$ ,  $\varepsilon = 4\varepsilon_o$  and with inner dimensions  $a=5$  cm and  $b=3$  cm.

- (a) Find the lowest 5 modes which can propagate in this waveguide and obtain the cutoff frequencies for each mode. Plot the mode chart.
- (b) Find the frequency range of single-mode operation in this waveguide.

[P2] **3.4 (modified)** - Consider a section of air-filled K-band waveguide WR42 with outside dimensions  $(0.5'' \times 0.25'')$  and thickness  $0.04''$ . Determine the cutoff frequencies of the first two propagating modes. If it is recommended to operate with the operating frequency at least 25% above the cut-off frequency of the  $TE_{10}$  mode but not higher than 95% of the next higher cutoff frequency, determine the percentage reduction in bandwidth that this operating range represents, relative to the theoretical bandwidth for a single propagating mode.

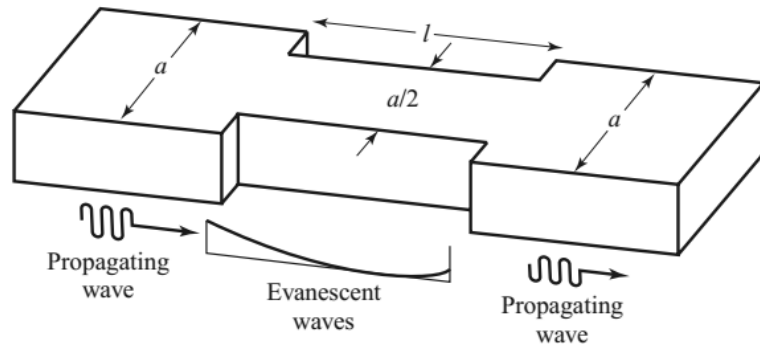
[P3] A metallic rectangular waveguide with  $a = 5$  cm and  $b = 2$  cm operating at 20 GHz in TE mode is filled with a dielectric material with  $\mu = \mu_o$ ,  $\varepsilon = 4\varepsilon_o$  has the following electric field component:

$$E_x = jE_o \sin\left(\frac{2\pi y}{b}\right) e^{-j\beta z}$$

- (a) operation mode
- (b) Cutoff frequency
- (c) Propagation constant  $\beta$

[P4] **3.6-** An attenuator can be made using a section of waveguide operating below cutoff, as shown in **Fig. P4**. If  $a = 2.286$  cm and the operating frequency is 12 GHz, determine the required length of the below-cutoff section of

waveguide to achieve an attenuation of 100 dB between the input and output guides. Ignore the effect of reflections at the step discontinuities.



**Fig. P4:** Circuit for Problem P4.

[P5] A rectangular waveguide filled with air has dimensions  $a = 8.636$  cm and  $b = 4.318$  cm, and operates at 4 GHz.

- Find if the  $TE_{10}$  mode can propagate and, if so, calculate the phase and group velocities.
- Repeat for the  $TM_{11}$  mode.