

# Physics 211

Sections 1 & 70

Dr. Geoffrey Lovelace

Fall 2012

Lecture 11 (10/04/12)

# Lecture 11 outline

- Announcements
- More quantitative 2nd-law problems
  - Free-body diagrams
  - Example: Atwood machine & ramp
- Friction & air resistance
  - How friction works
  - Example: friction
- Class participation

# Announcements

- piazza.com lecture materials updated
- Homework
  - Homework #5: due 11:59PM
  - Homework #6: will be posted today
- Reading: for next week, begin reading chapter 5
- Office hours
  - 10-11AM, 4PM-5PM today in MH-601B
  - Questions about homework, lecture? Review your exam? ... come to office hours!

Today



<b>Sep 25</b>	<b>Exam 1</b>
Sep 27	Laws of motion, <i>HW #4 due</i>
Oct 2	Free body diagrams
Oct 4	Free body diagrams, friction, <i>HW #5 due</i>
Oct 9	Work, introduction to energy
Oct 11	Energy, kinetic & potential energy, conservation of energy, <i>HW #6 due</i>
Oct 16	Conservation of energy
Oct 18	Linear momentum, conservation of linear momentum, <i>HW #7 due</i>
<b>Oct 23</b>	<b>Exam 2</b>
Oct 25	Conservation of momentum, collisions, <i>HW #8 due</i>
Oct 30	Collisions, center of mass, rockets
Nov 1	Circular motion, gravitation, <i>HW #9 due</i>
Nov 6	Gravitation, Kepler's laws, intro to rigid body rotation
Nov 8	Rotation, torque, angular momentum
Nov 13	Conservation of angular momentum <i>HW #10 due</i>
<b>Nov 15</b>	<b>Exam 3</b>
Nov 20	<i>Fall Recess — No class</i>
Nov 22	<i>Fall Recess — No class</i>
Nov 27	Temperature, gas laws
Nov 29	Phase changes, heat transfer, <i>HW #11 due</i>
Dec 4	Laws of thermodynamics, entropy
Dec 6	Harmonic motion, <i>HW #12 due</i>
Dec 11	Harmonic motion & waves
Dec 13	Gravitational waves, harmonic motion, black holes, <i>HW #13 due</i>
<b>Dec 20</b>	<b>Final exam 9:30AM–11:20AM</b>



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- More quantitative 2nd-law problems
  - Free-body diagrams
  - Example: Atwood machine & ramp
- Friction & air resistance
  - How friction works
  - Example: friction
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# Free-body diagrams

# Free-body diagrams

1. Read carefully
2. Draw a sketch
3. Given? Goal?
4. Brainstorm: 2nd law
  - 4a. **For each body, draw a free-body diagram**
5. Calculate
6. Plug in numbers
7. Is answer reasonable?

# Free-body diagrams

- Guide: how to apply  $F = ma$

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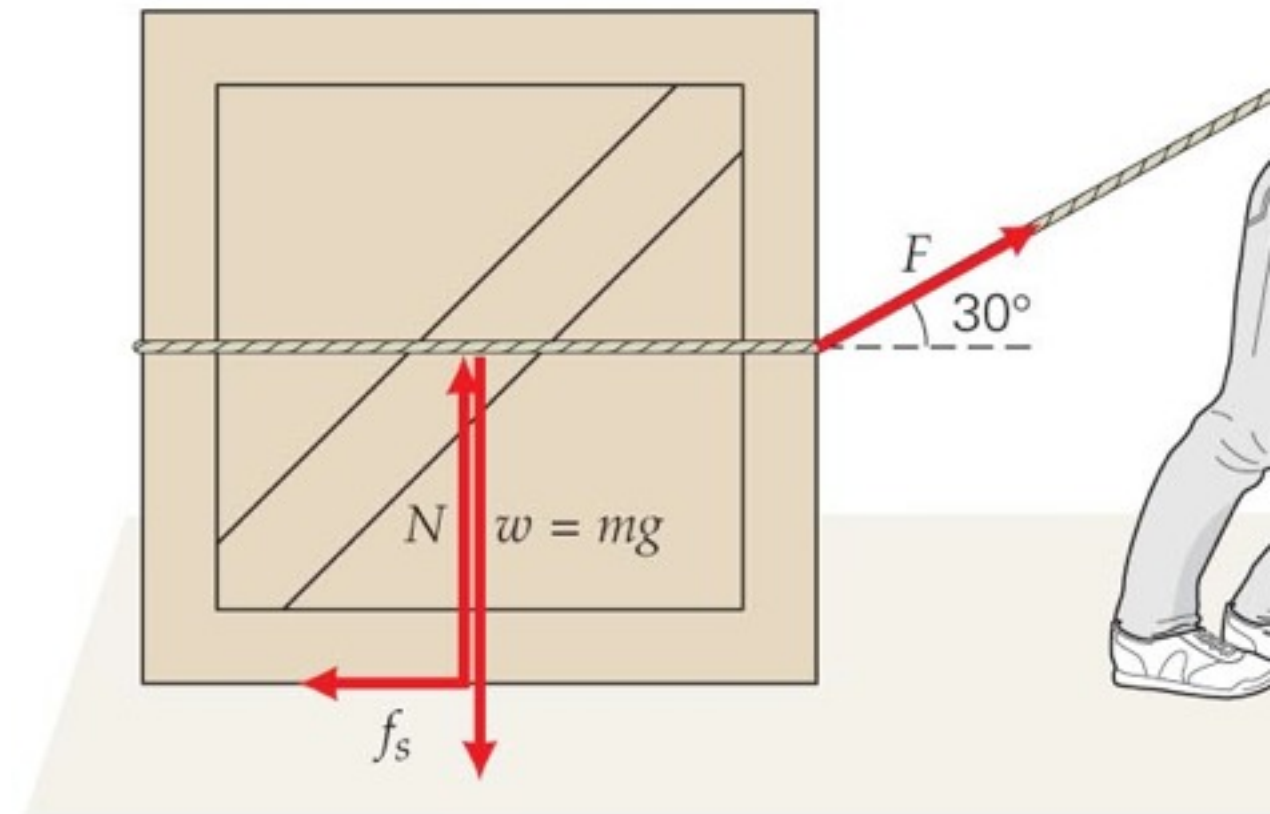
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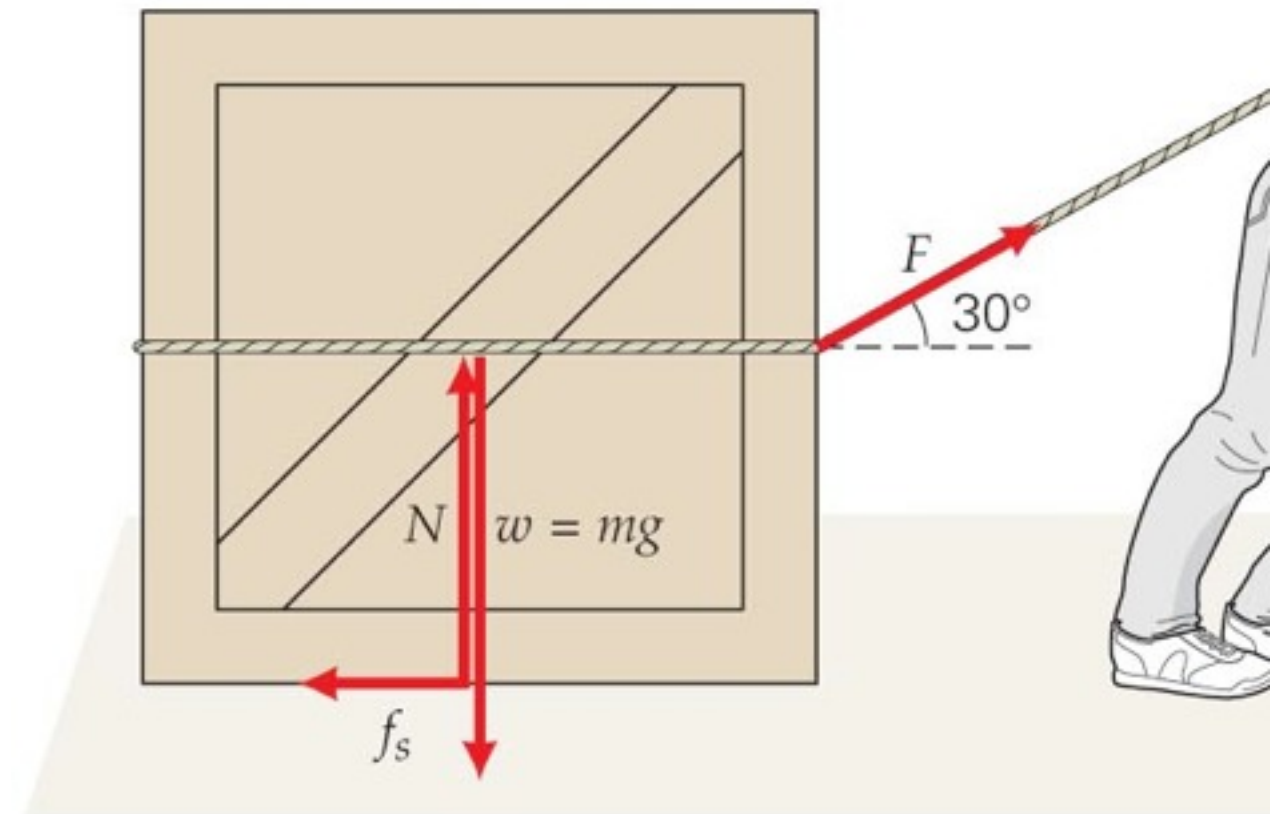
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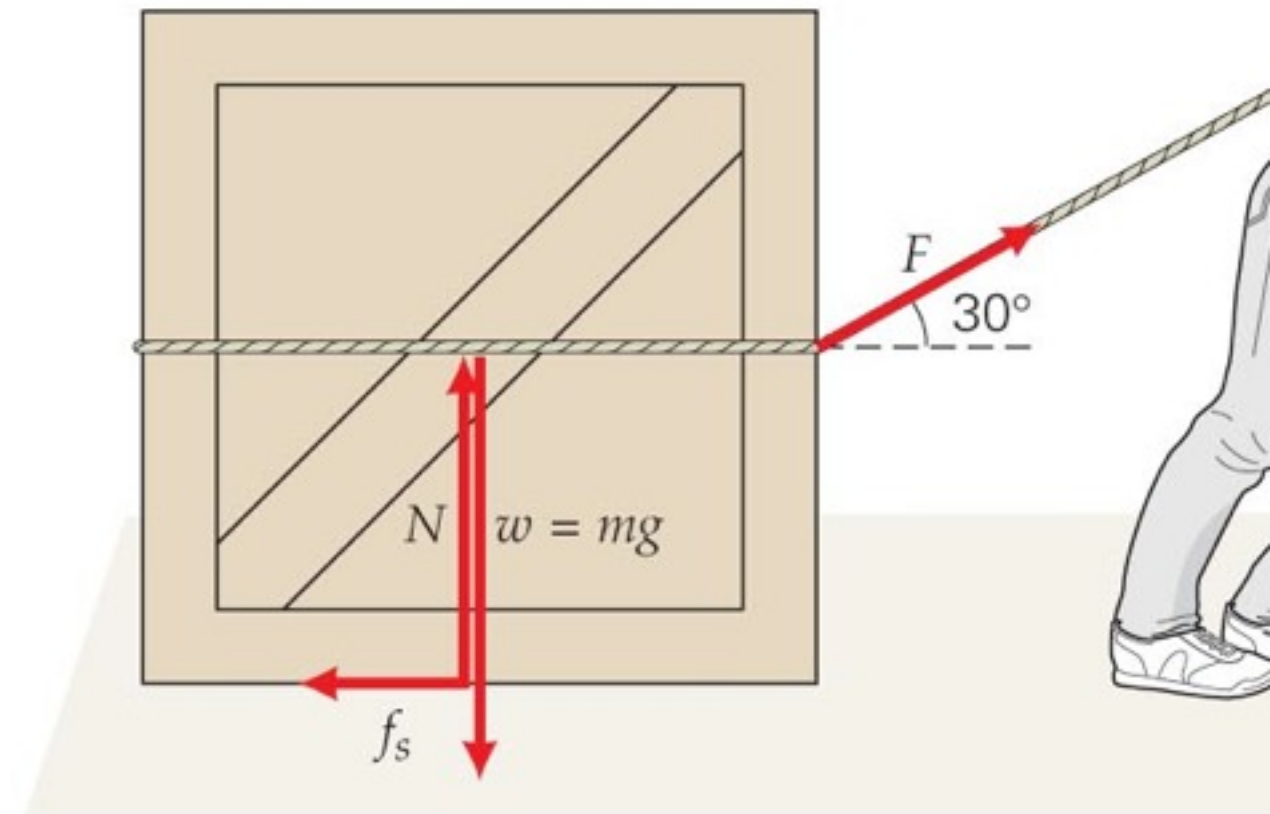
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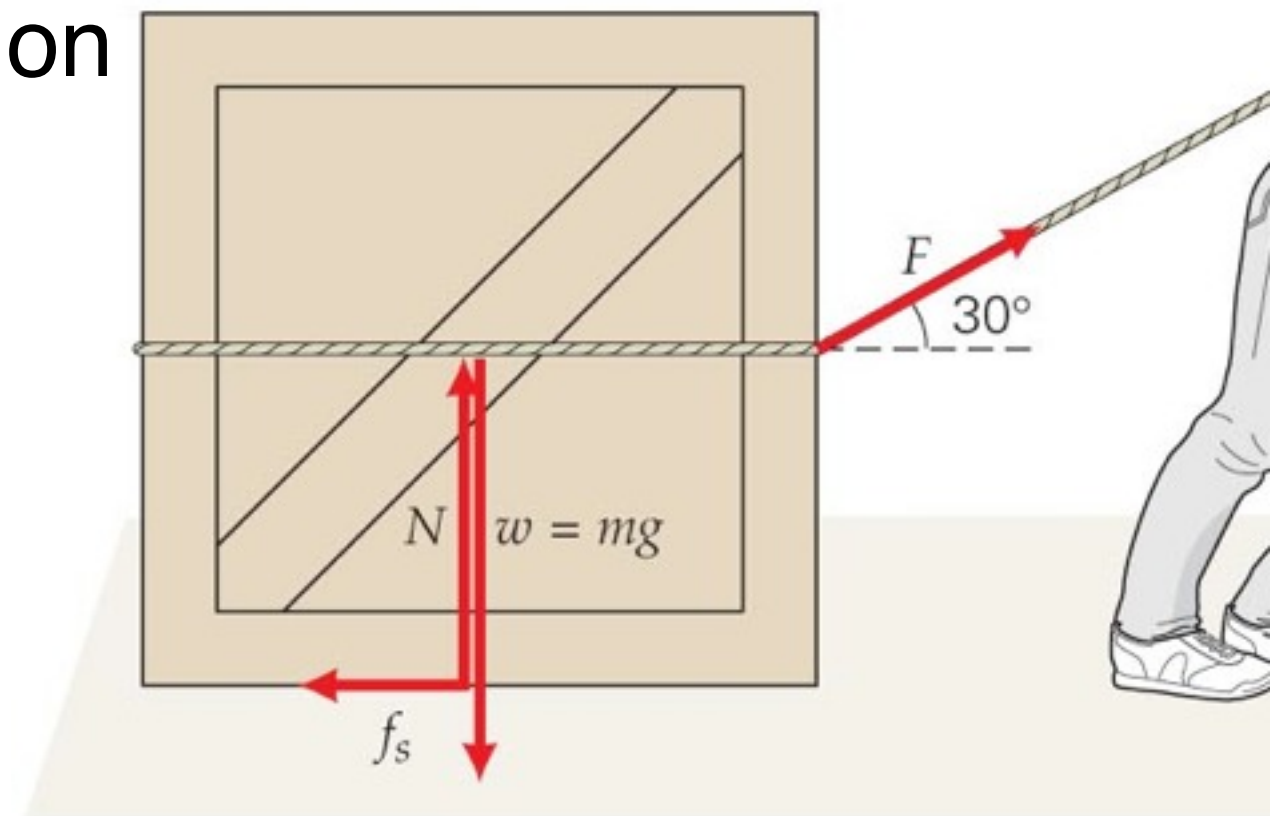
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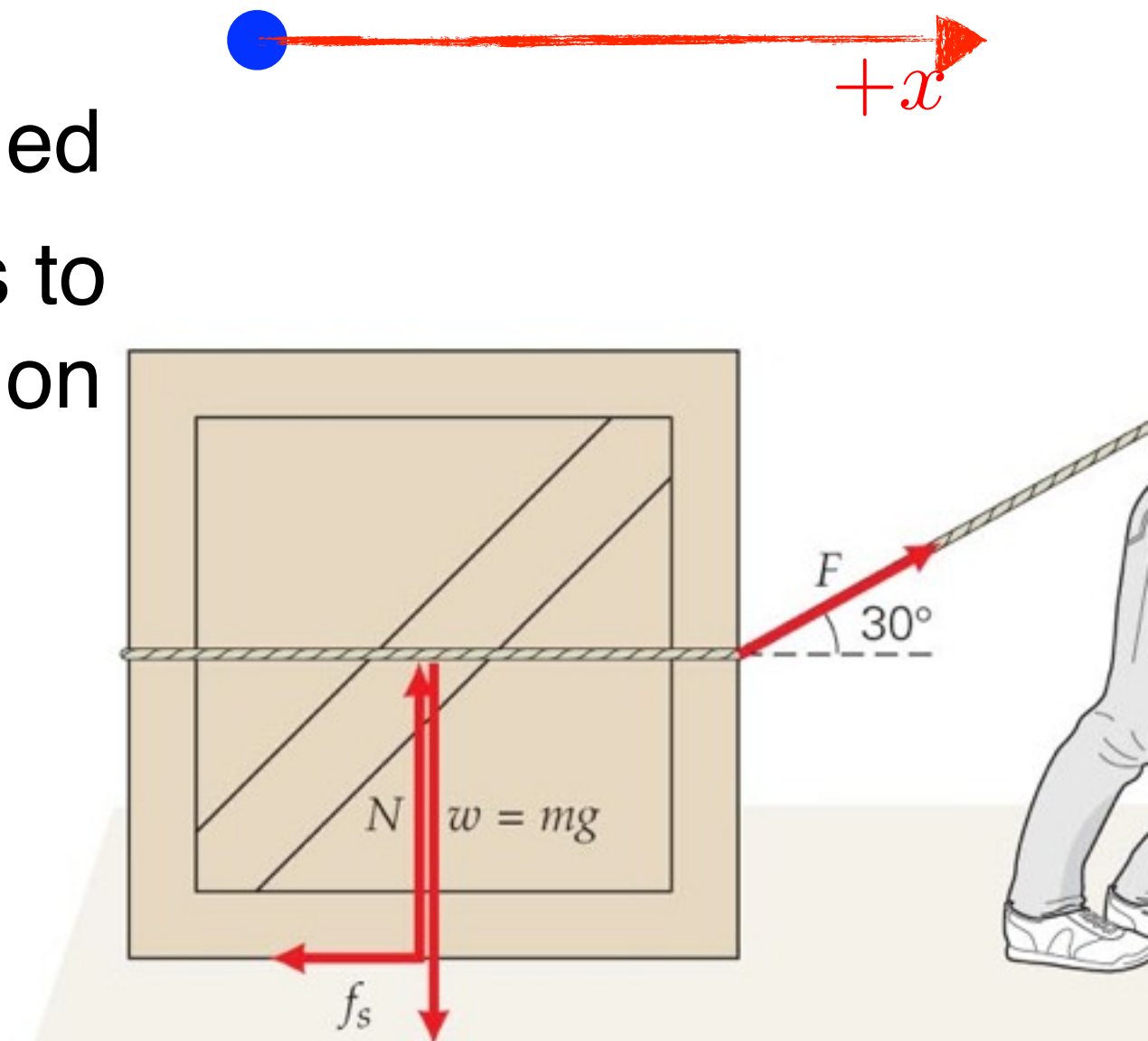
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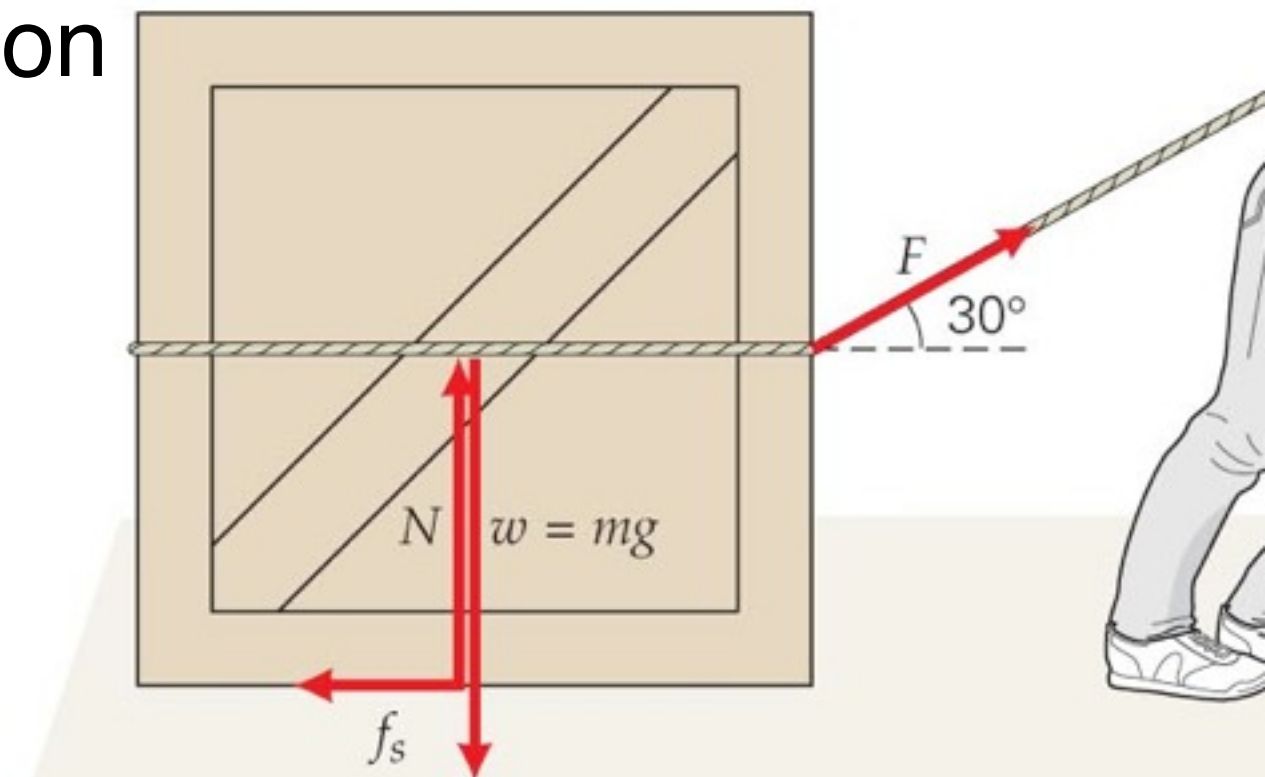
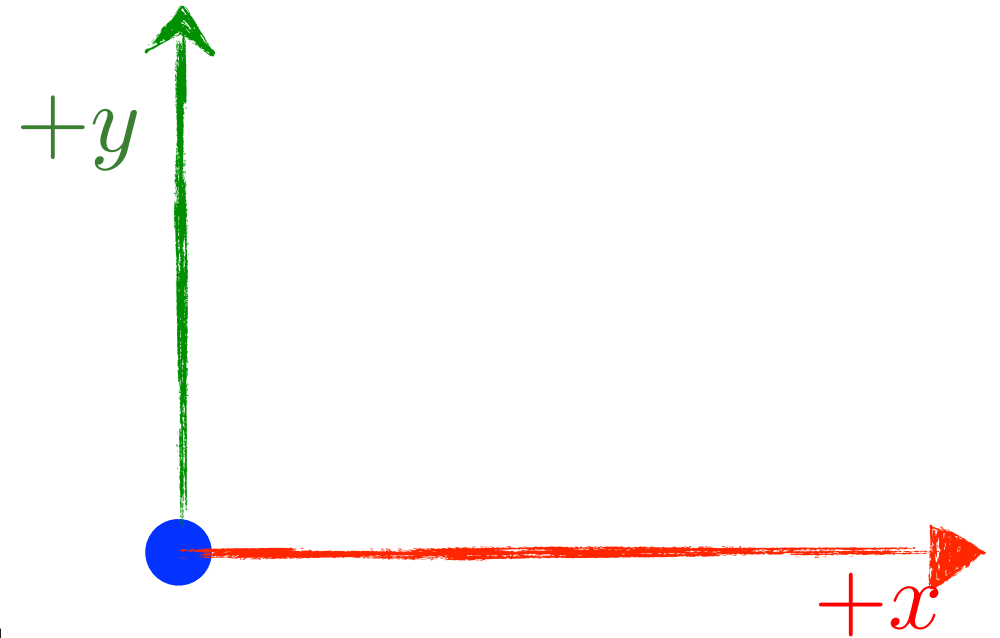
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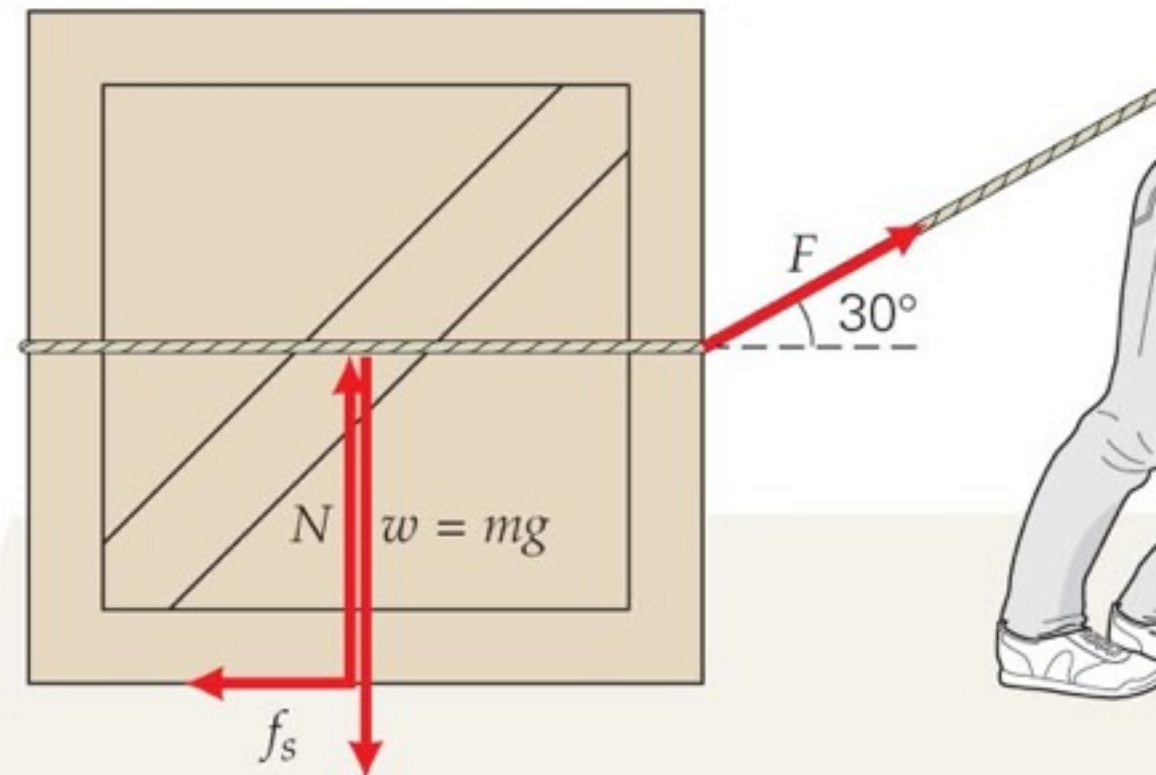
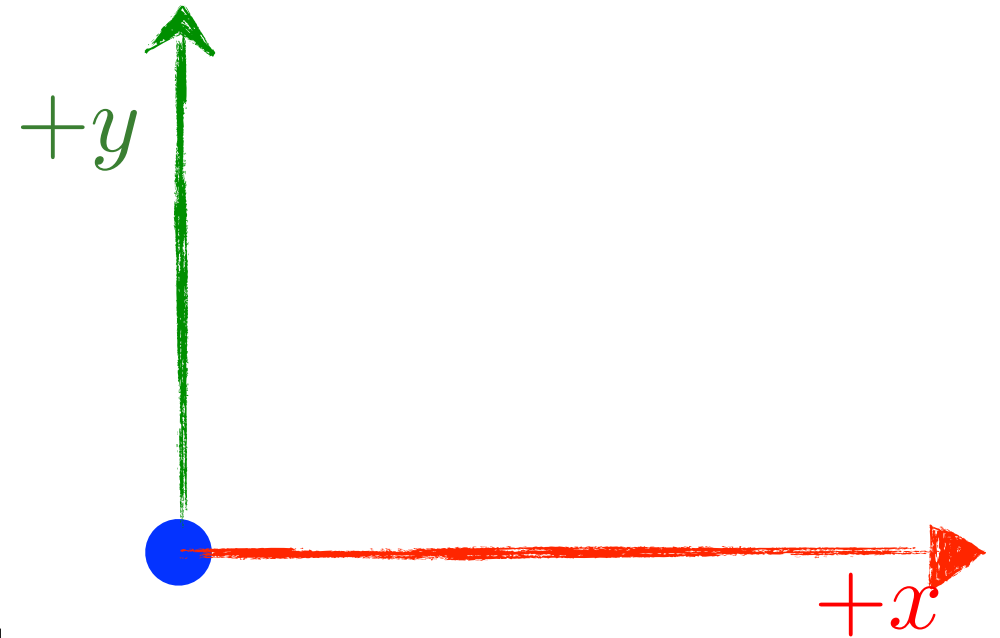
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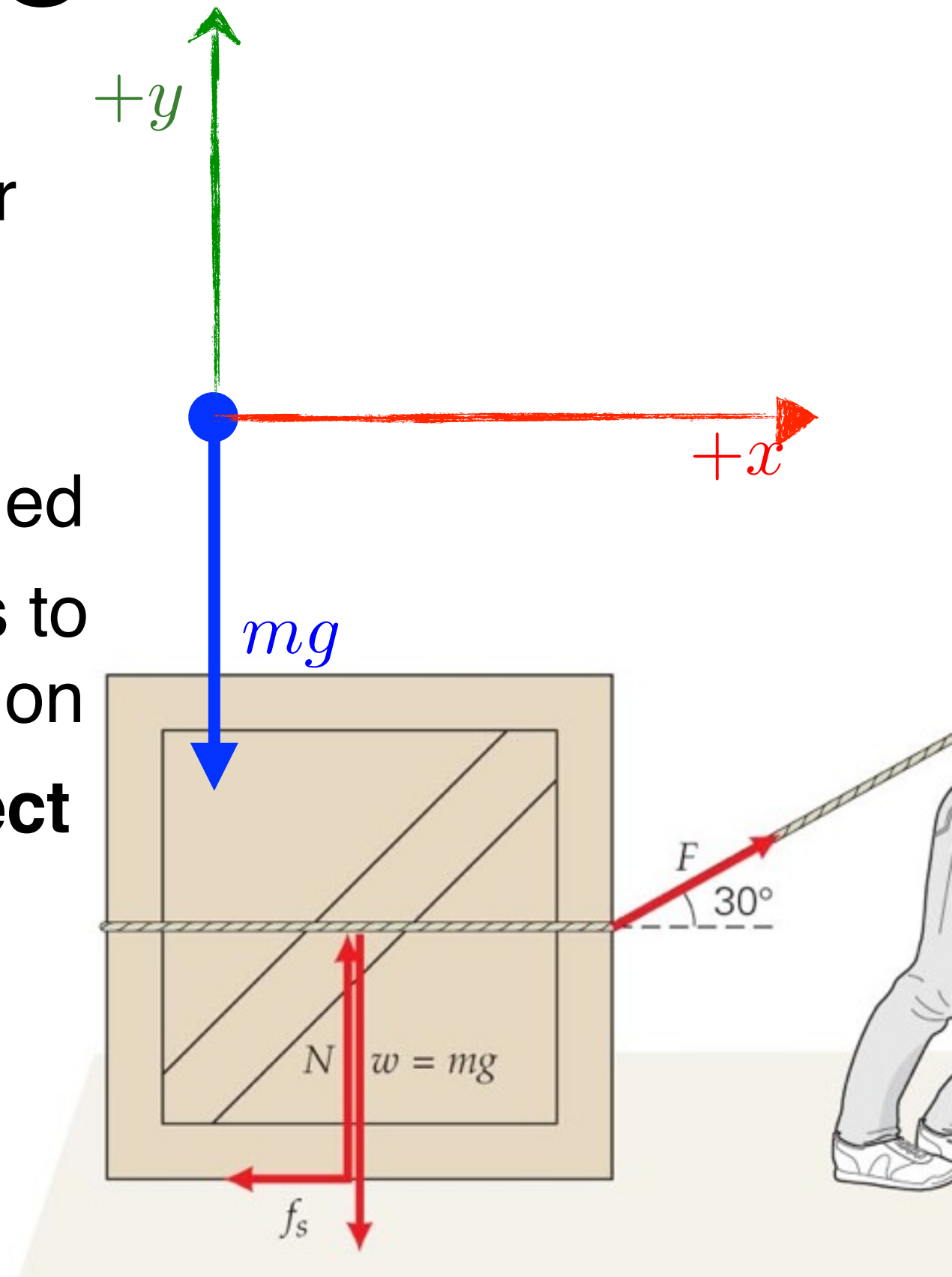
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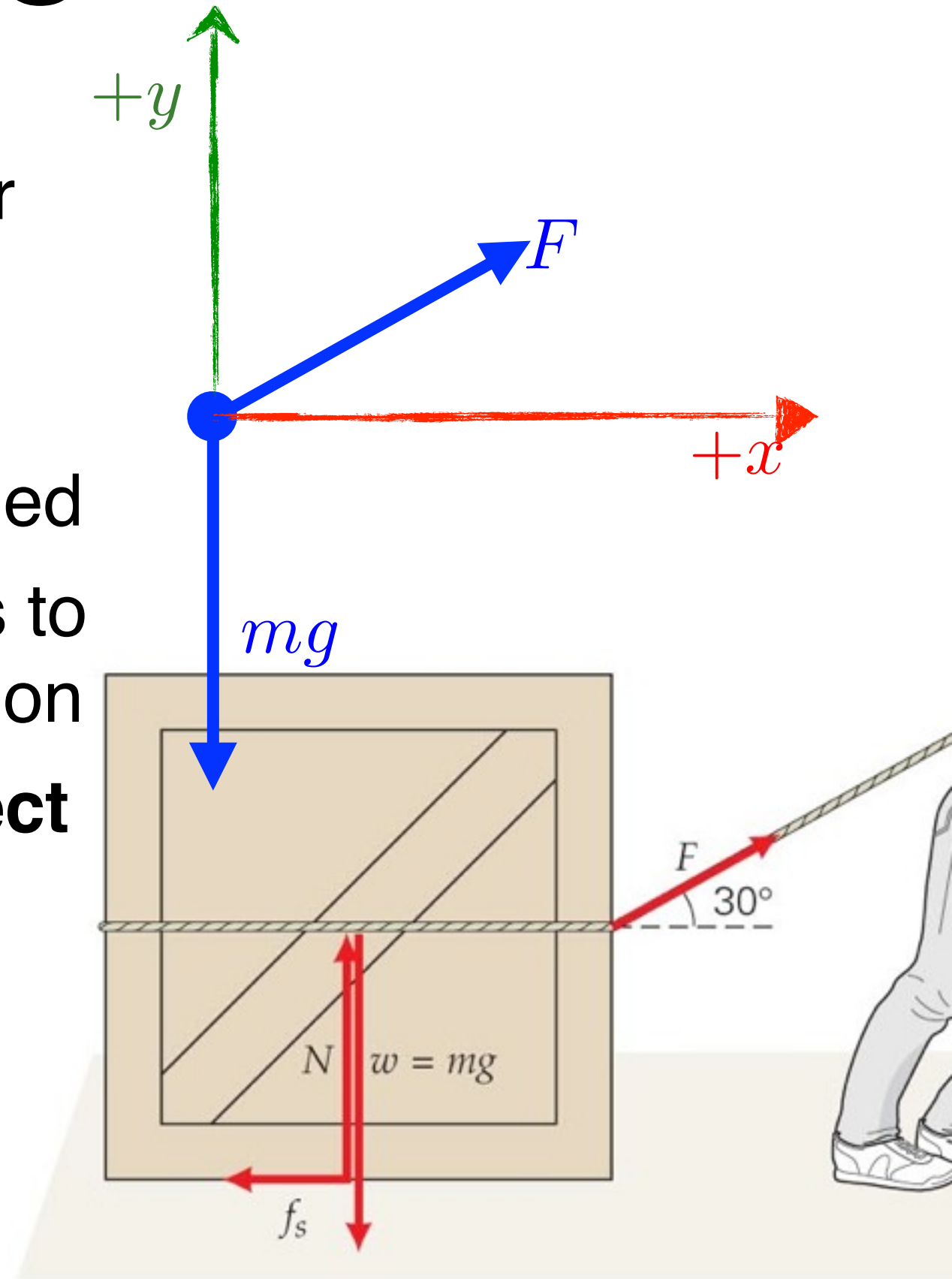
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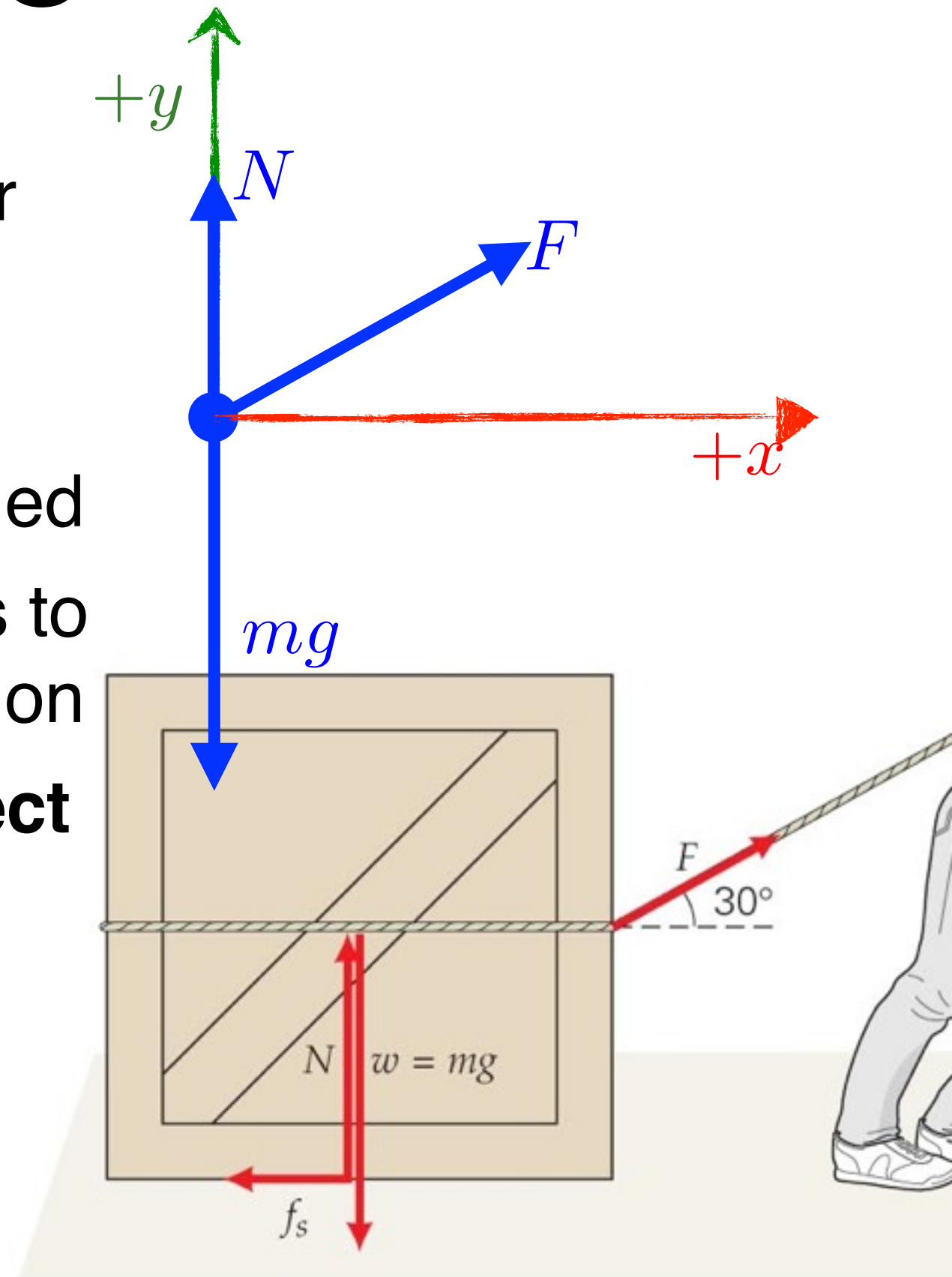
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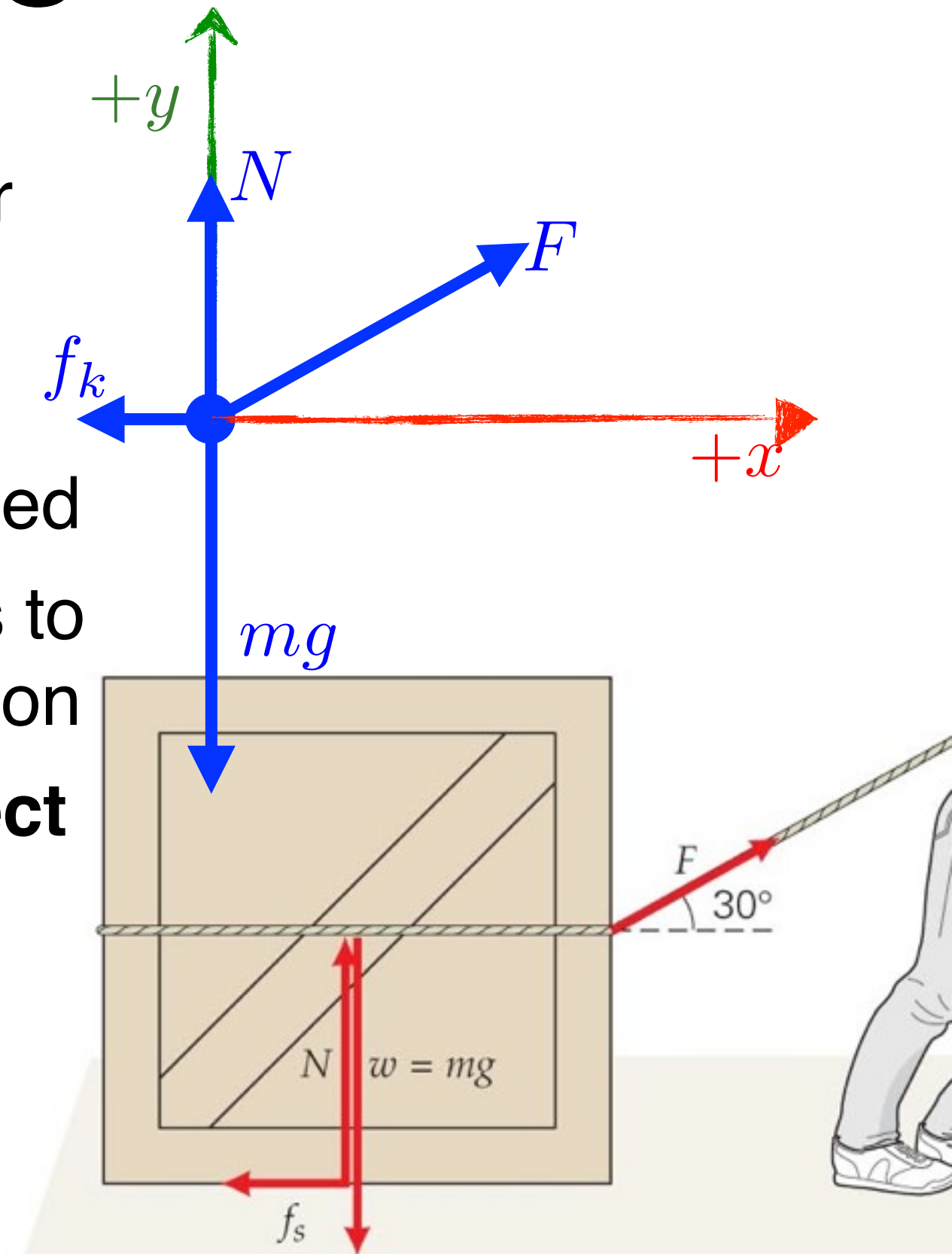
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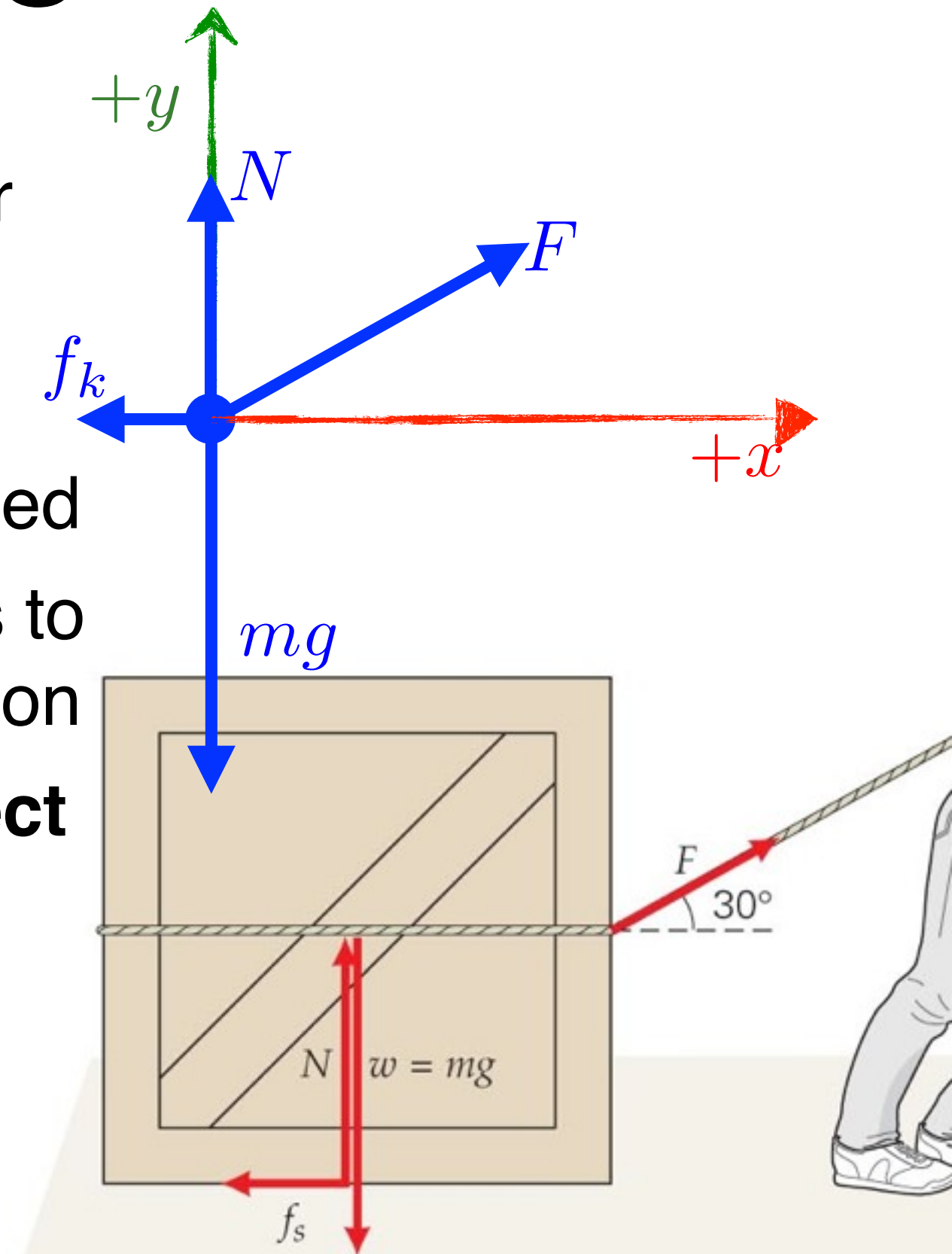
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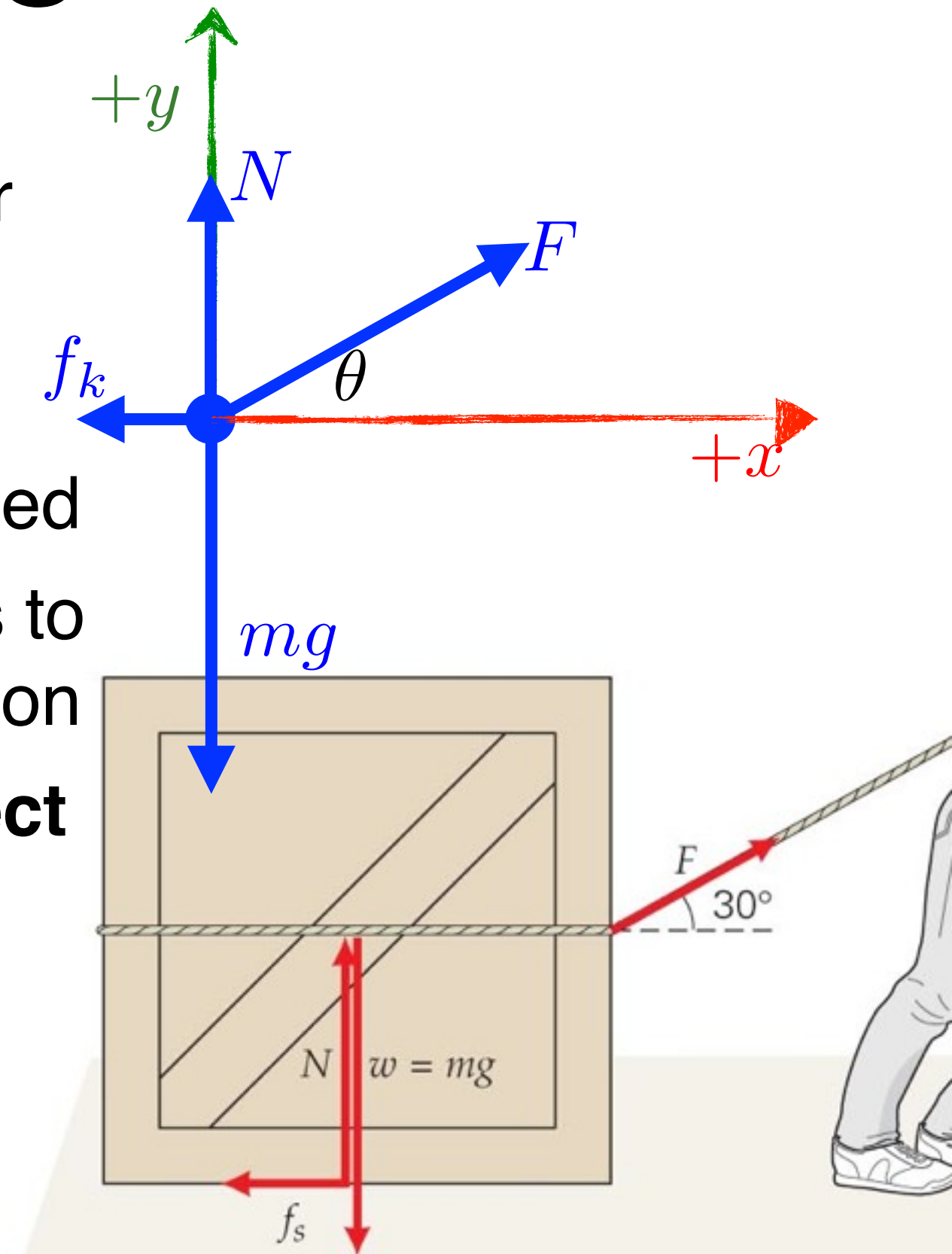
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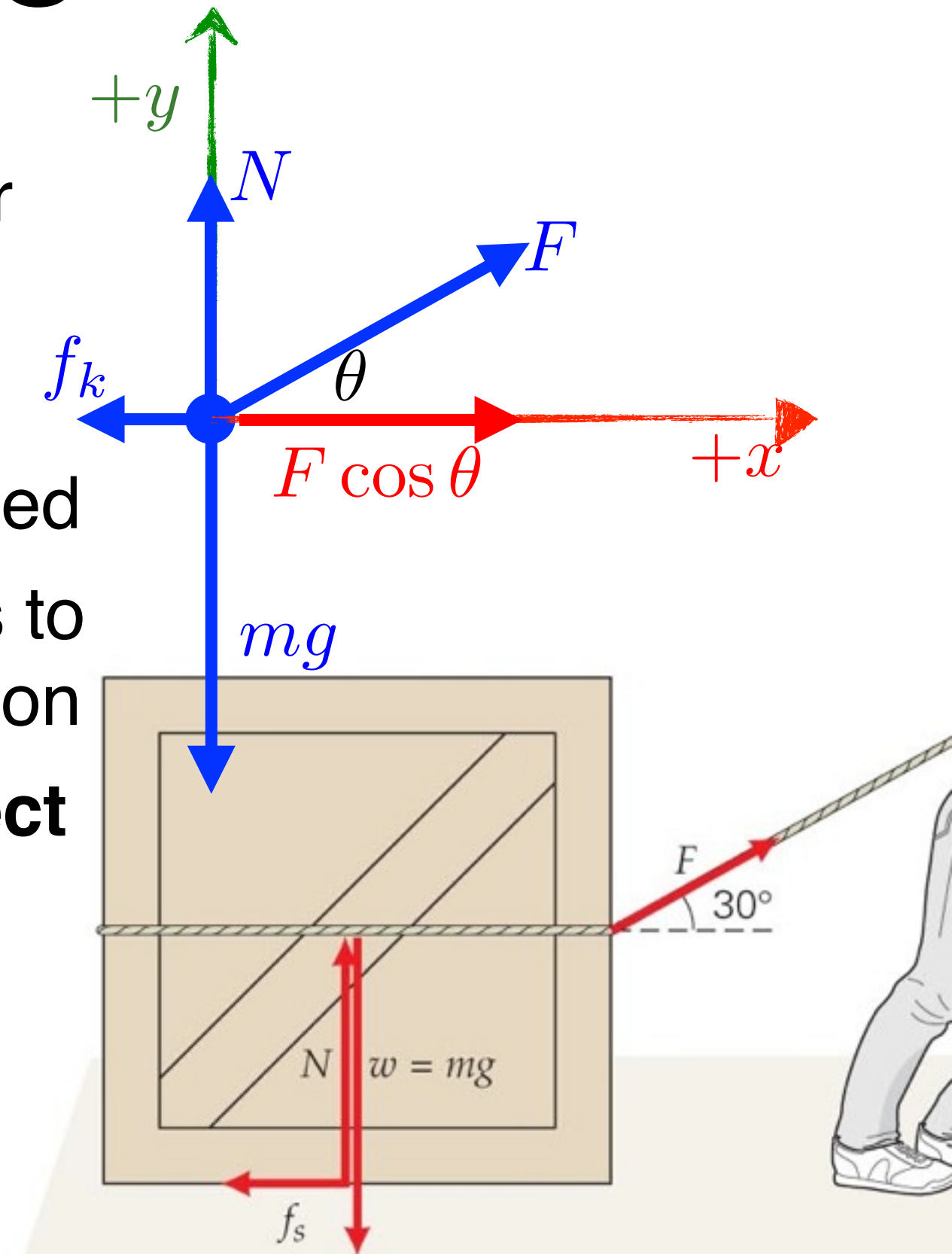
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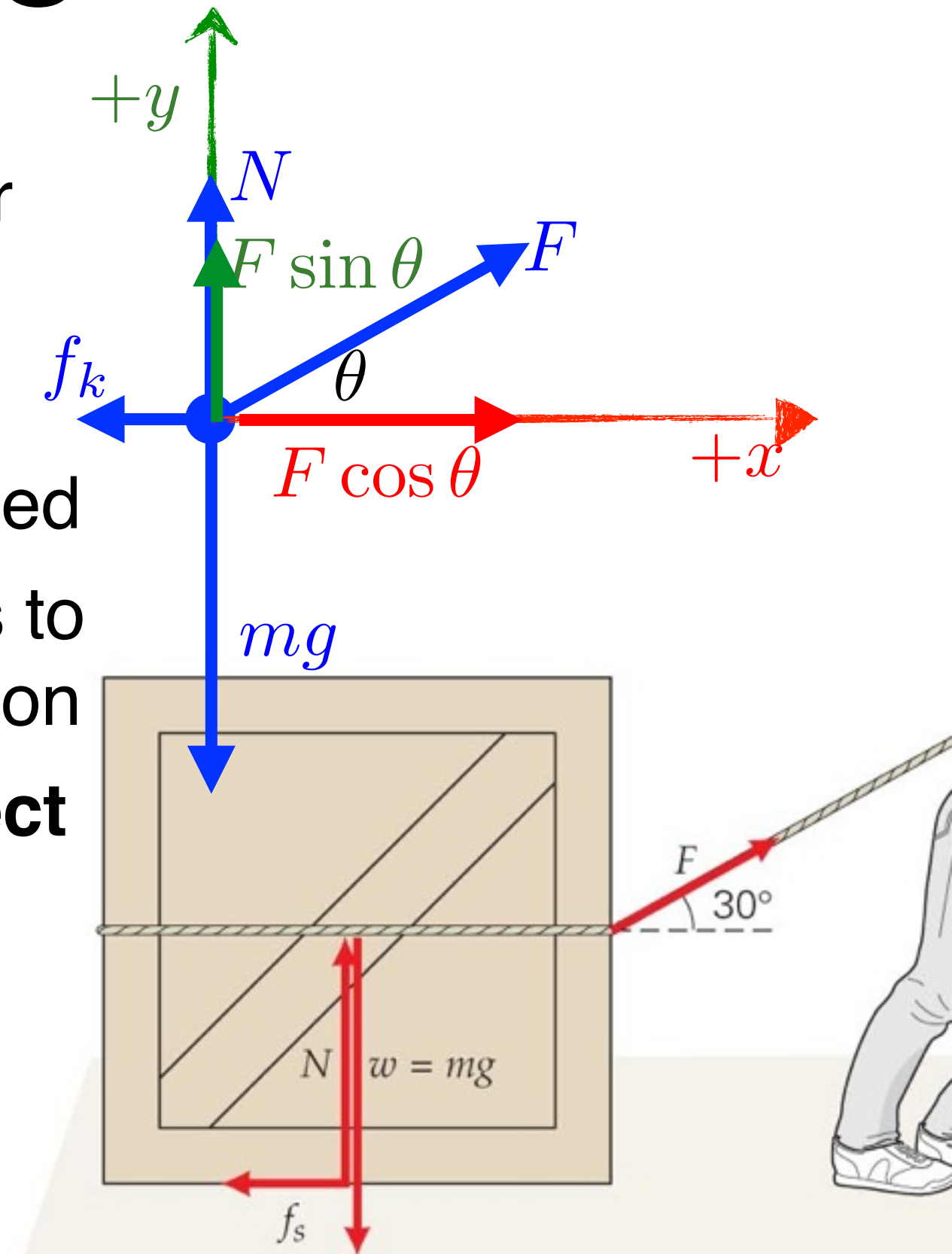
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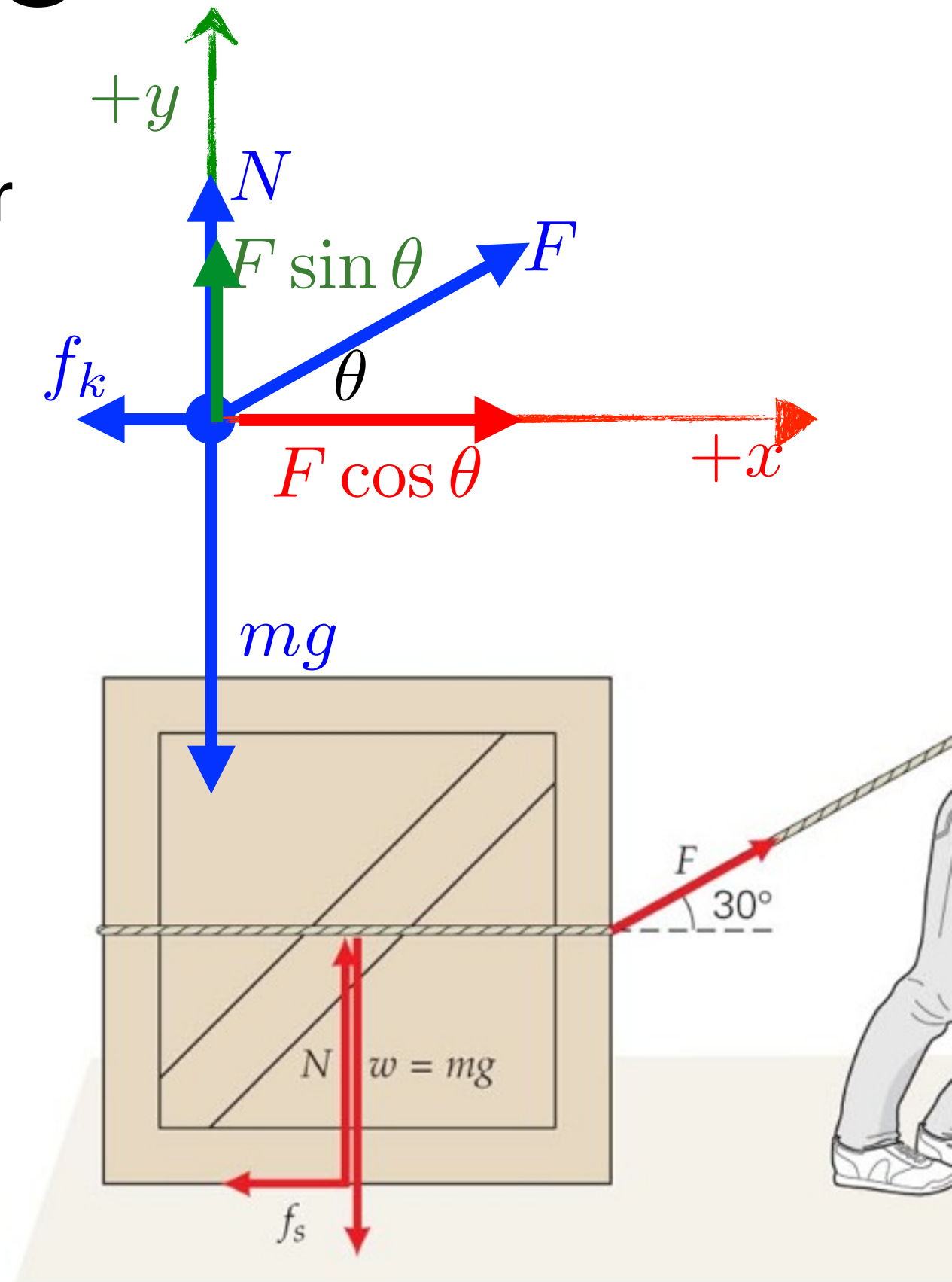
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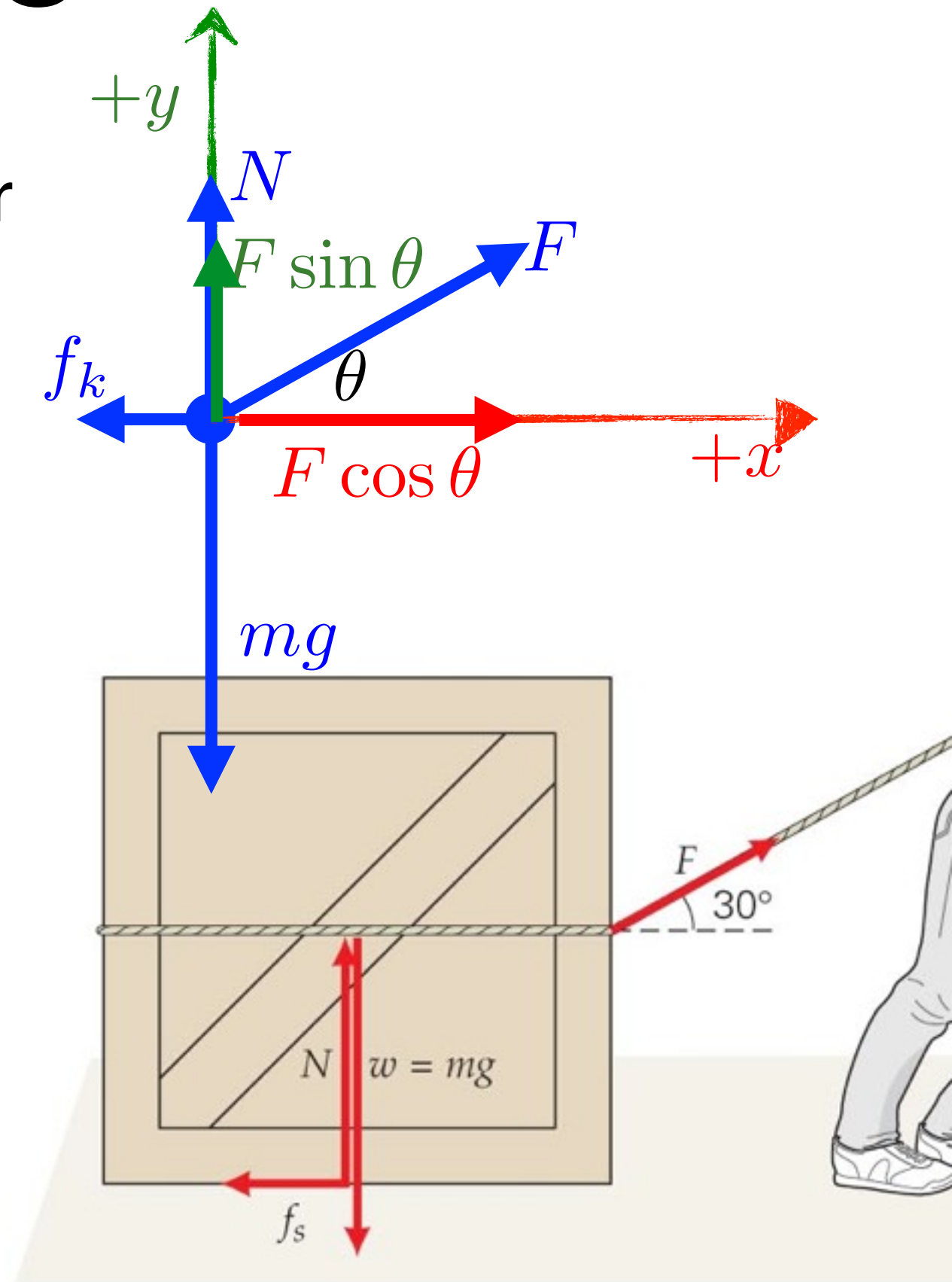
- Guide: how to apply  $F = ma$
- Draw a *separate* diagram for each object
- Use the horizontal and vertical free-body diagrams to compute the net forces for  $F = ma$



# Free-body diagrams

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$$F \cos \theta - f_k = ma_x$$

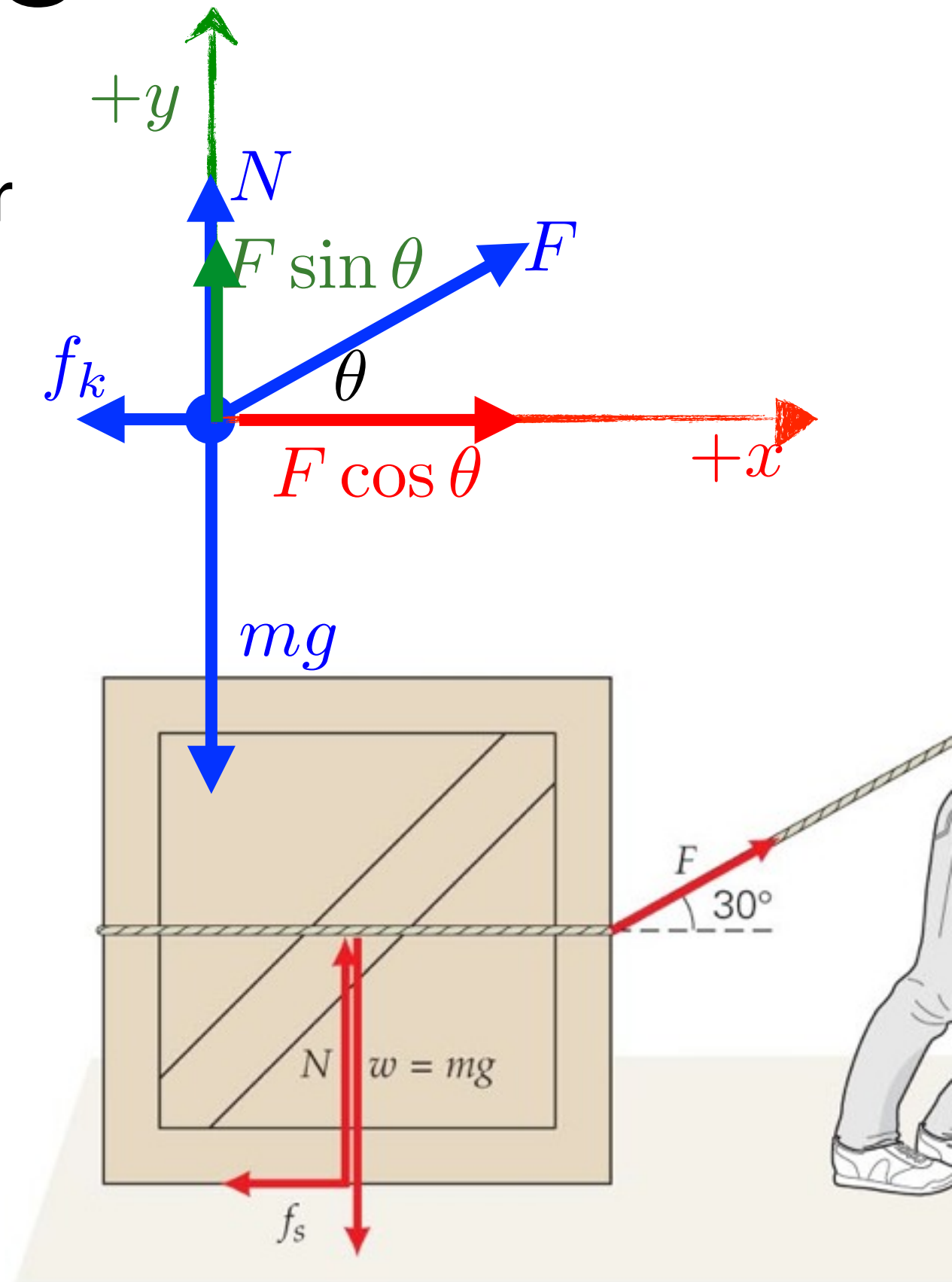


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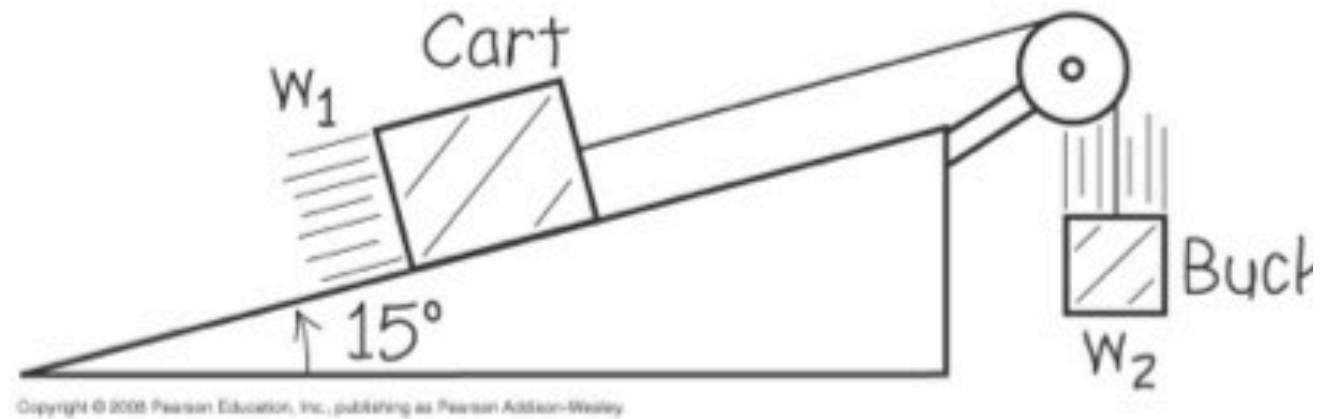
$$F \cos \theta - f_k = ma_x$$

$$F \sin \theta + N - mg = 0$$



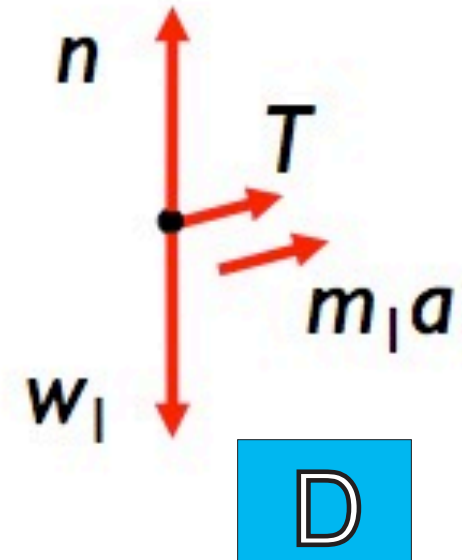
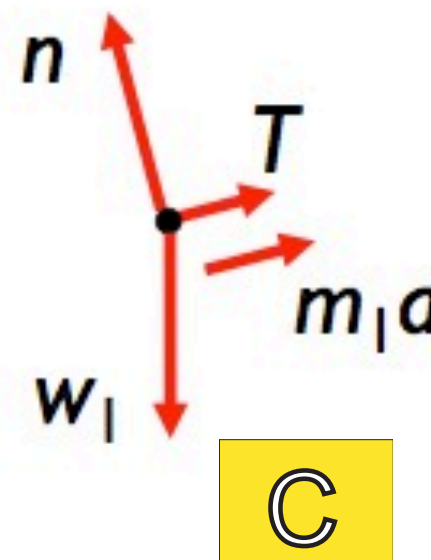
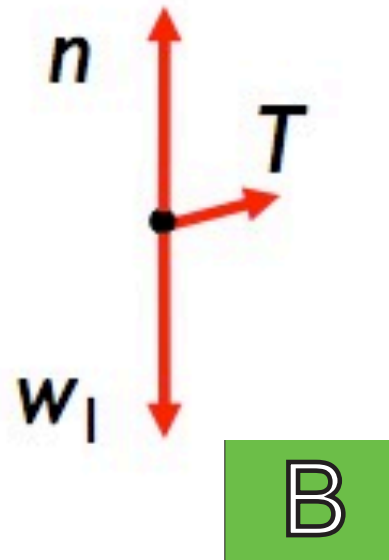
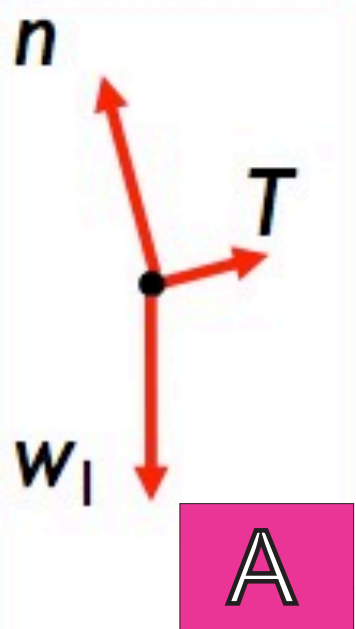
# Clicker question #41

A cart (weight  $w_1$ ) is attached by a lightweight cable to a bucket (weight  $w_2$ ) as shown. The ramp is frictionless.



When released, the cart accelerates up the ramp.

Which of the following is a *correct* free-body diagram for the cart?





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- Announcements
- Quantitative force examples
  - Free-body diagrams
  - Example: Atwood machine & ramp
- Friction & air resistance
  - How friction works
  - Example: friction
- Class participation

# Ex. 4.6

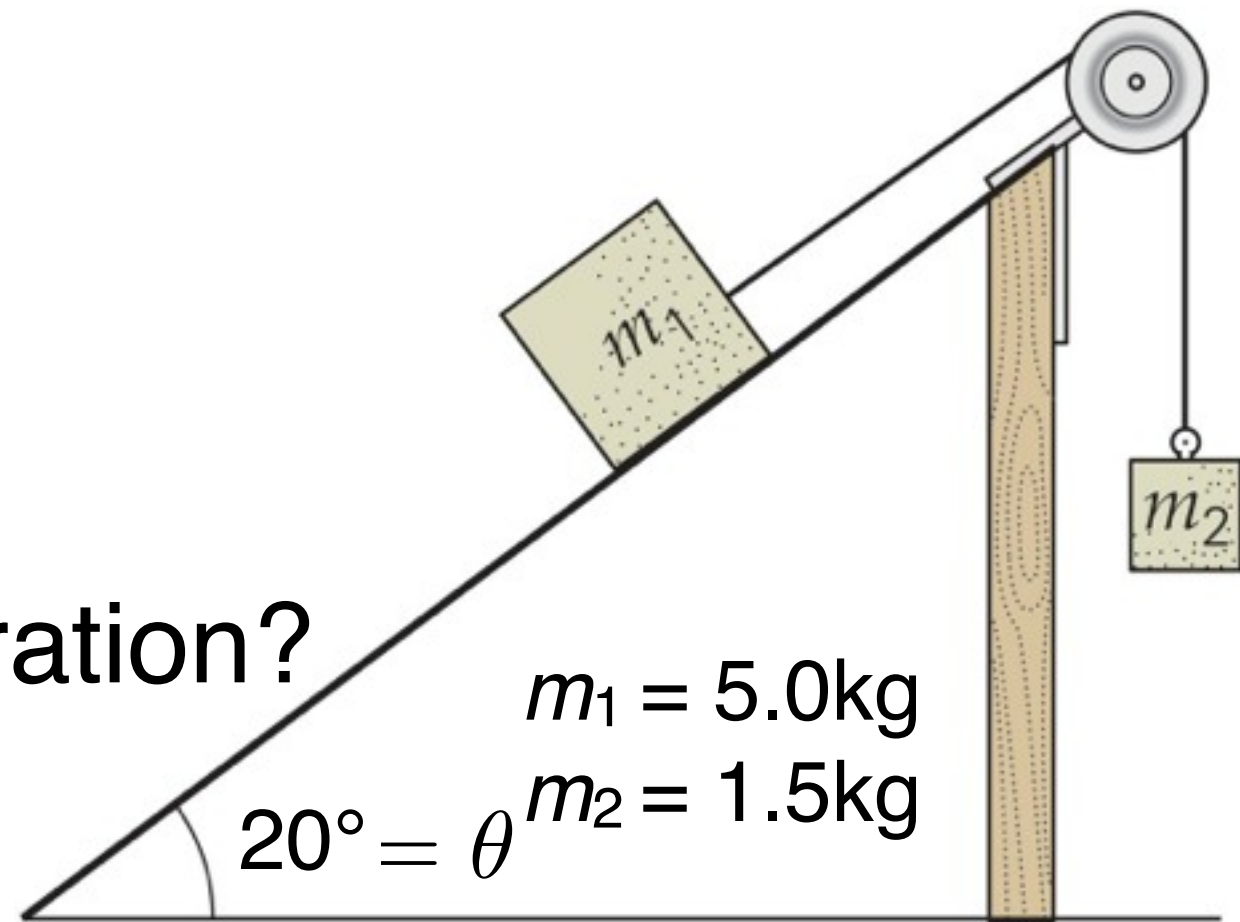
# Ex. 4.6

Acceleration?

$$m_1 = 5.0\text{kg}$$

$$m_2 = 1.5\text{kg}$$

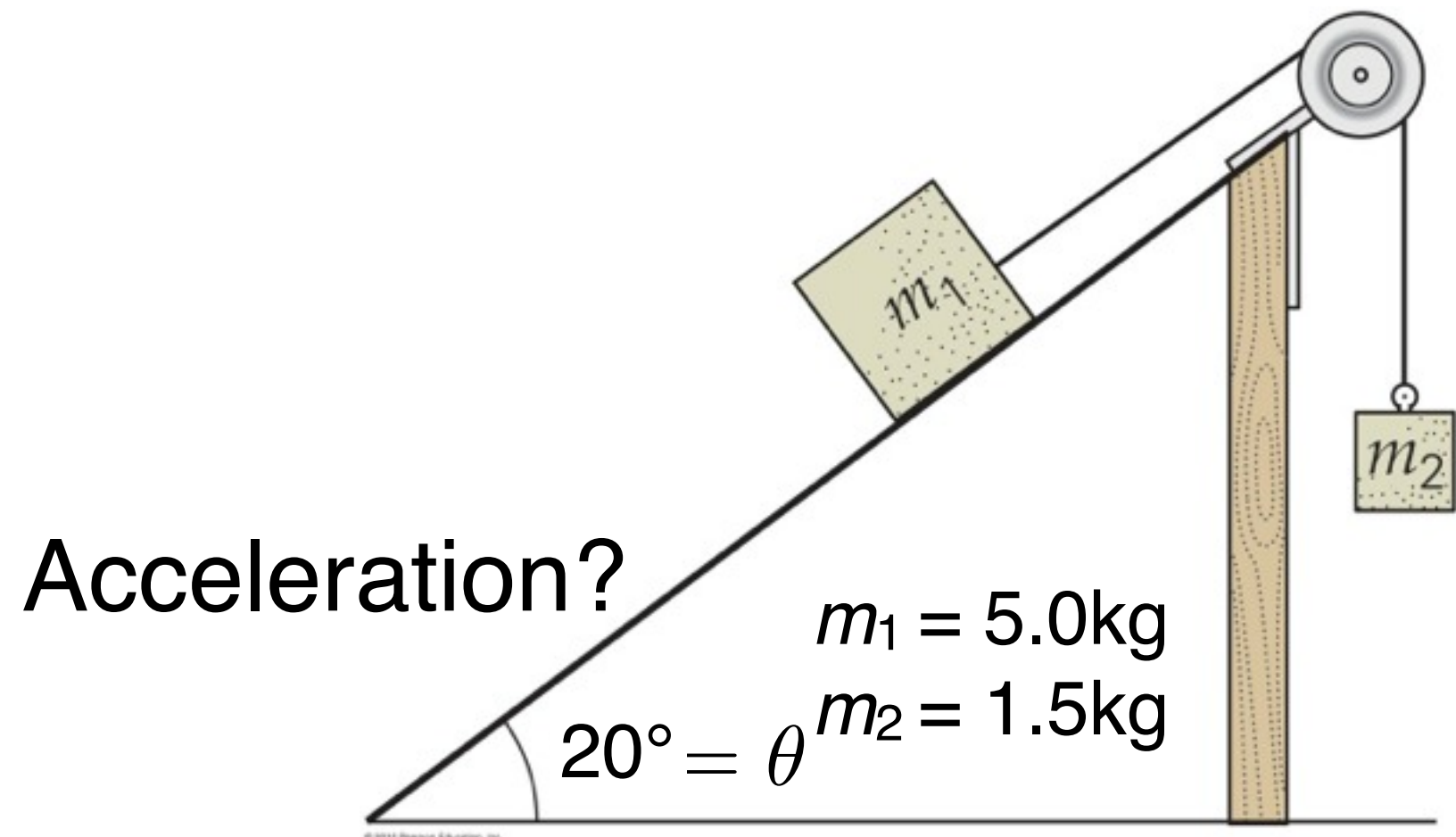
$$20^\circ = \theta$$





# Ex. 4.6

1. Read carefully



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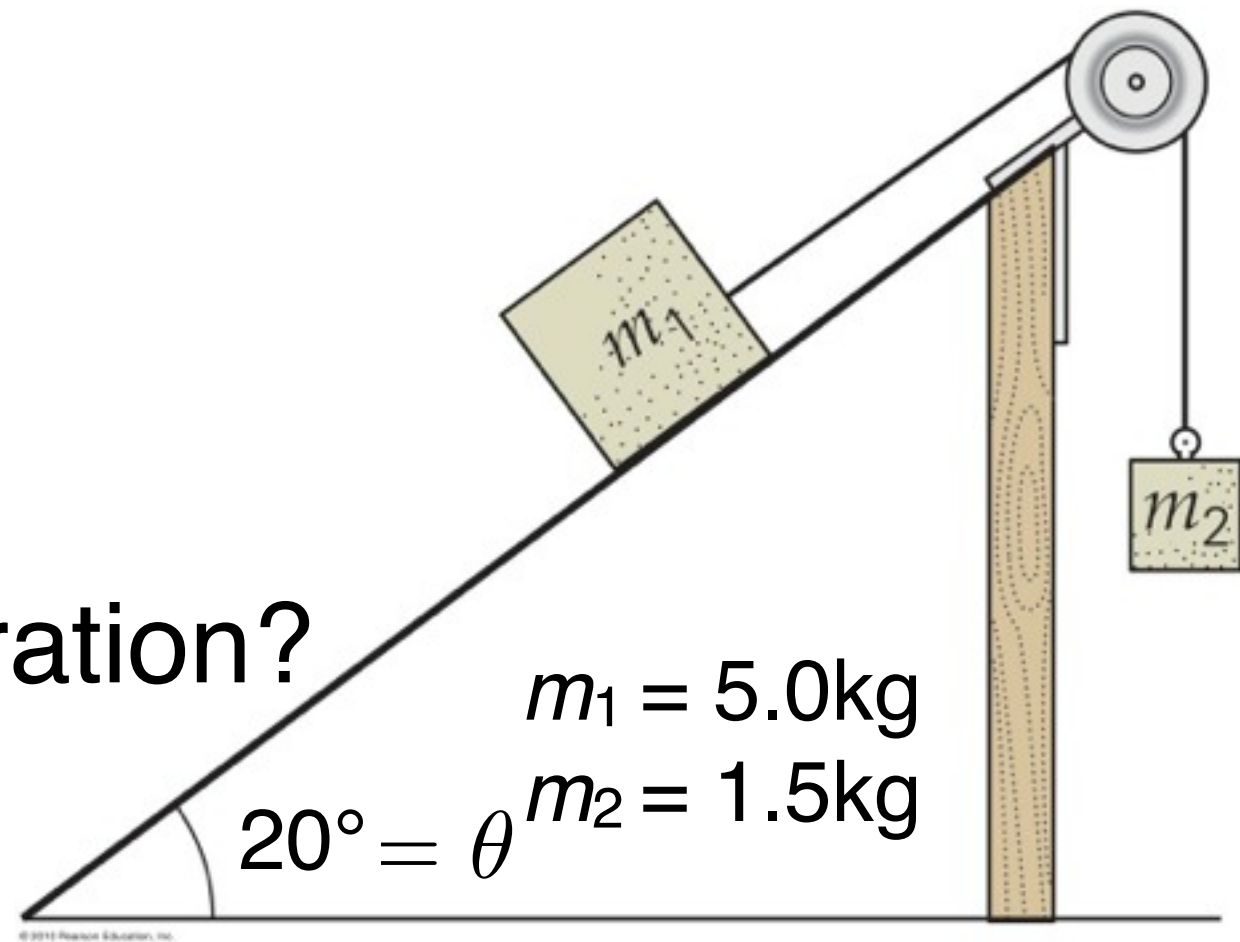
1. Read carefully
2. Draw a sketch = space diagram

Acceleration?

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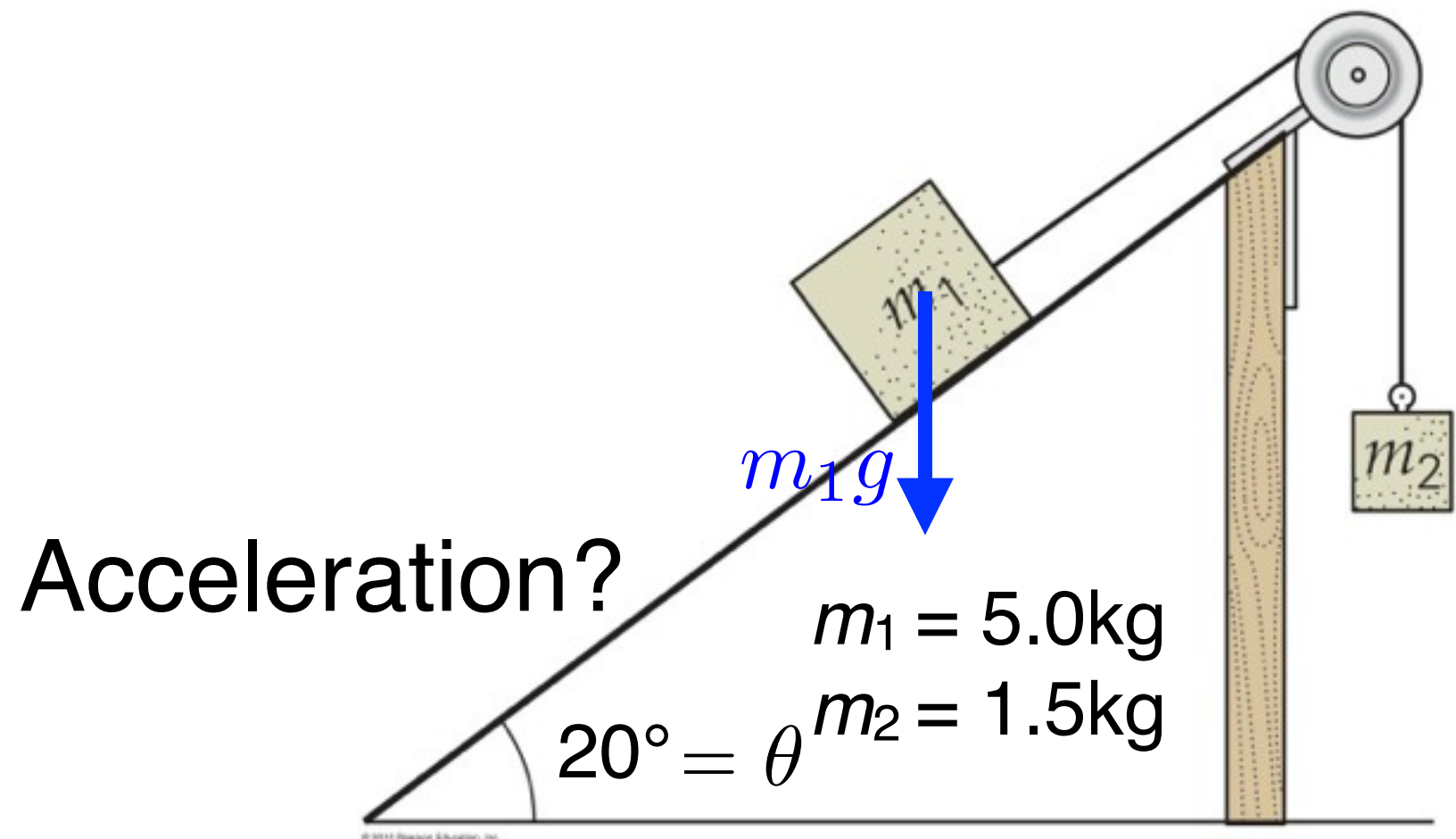
$$m_2 = 1.5\text{kg}$$

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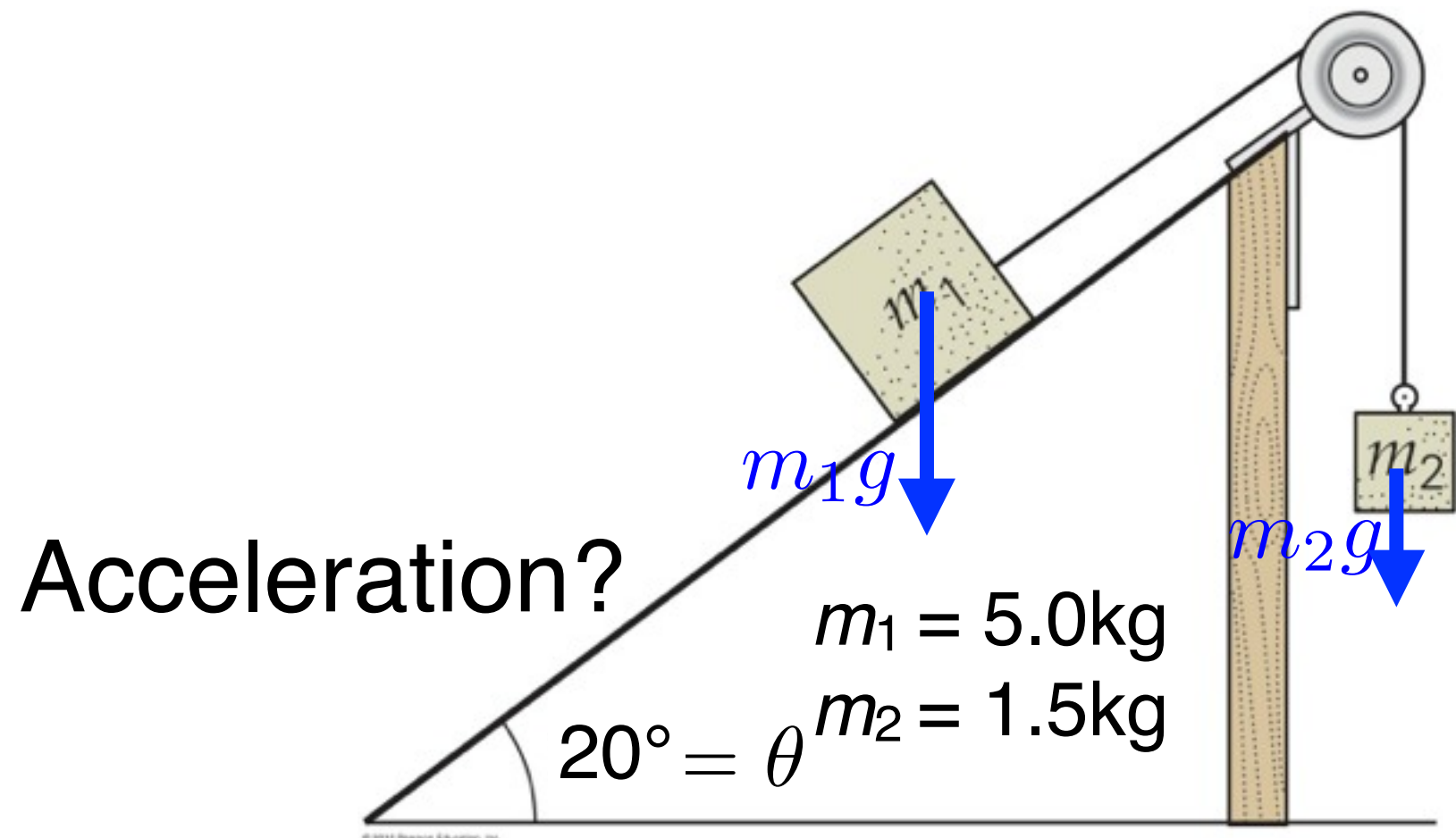
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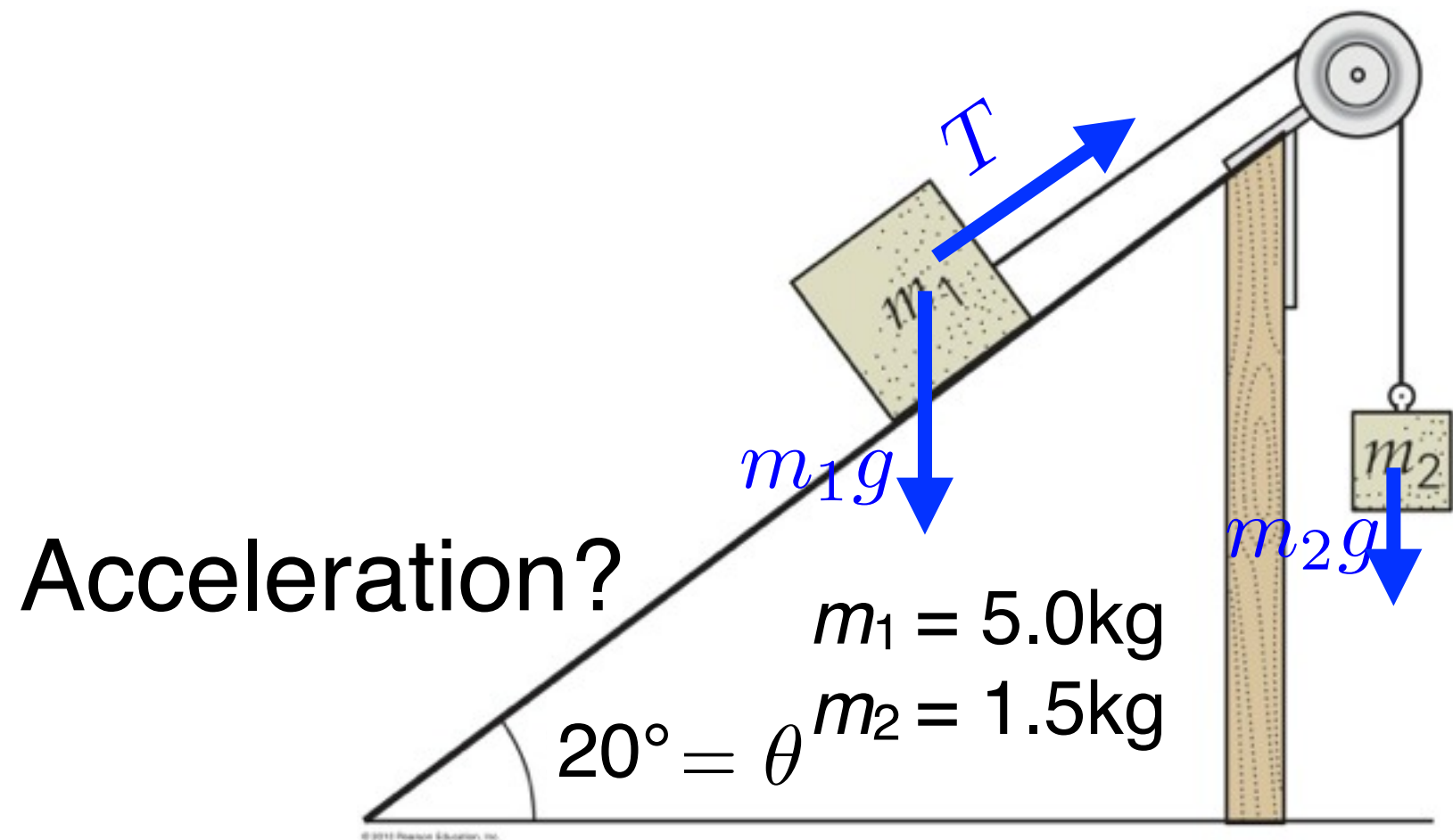
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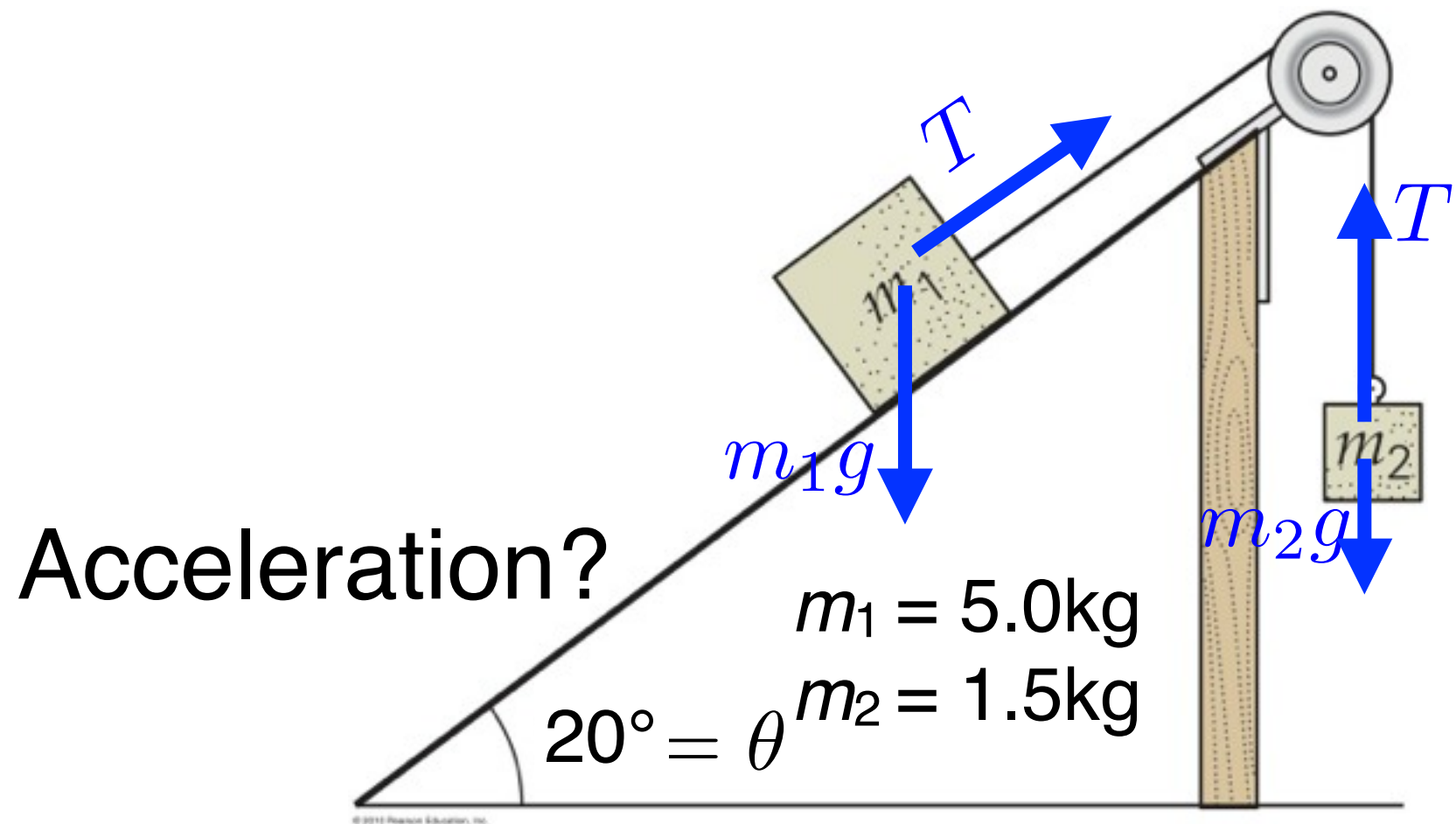
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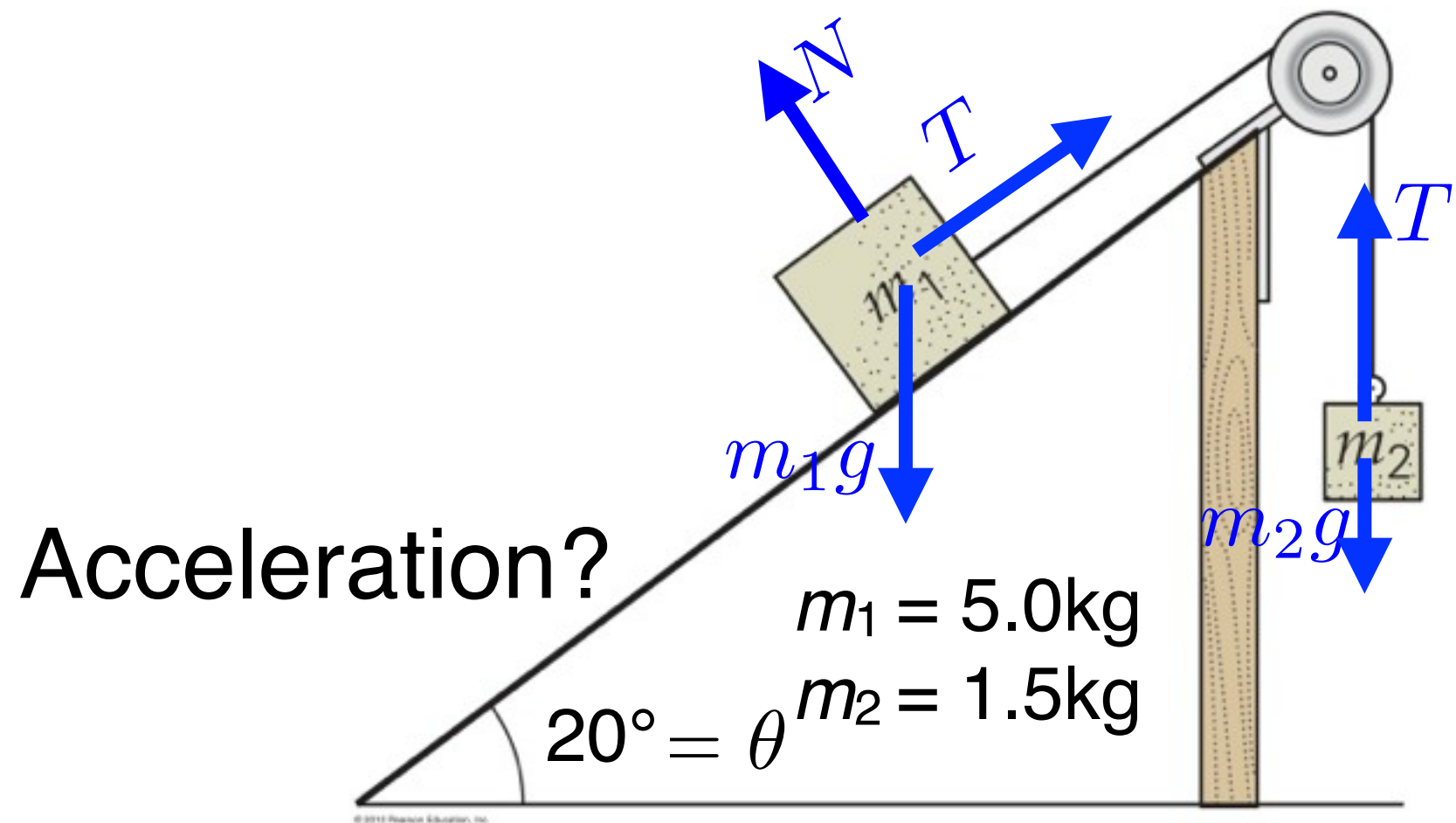
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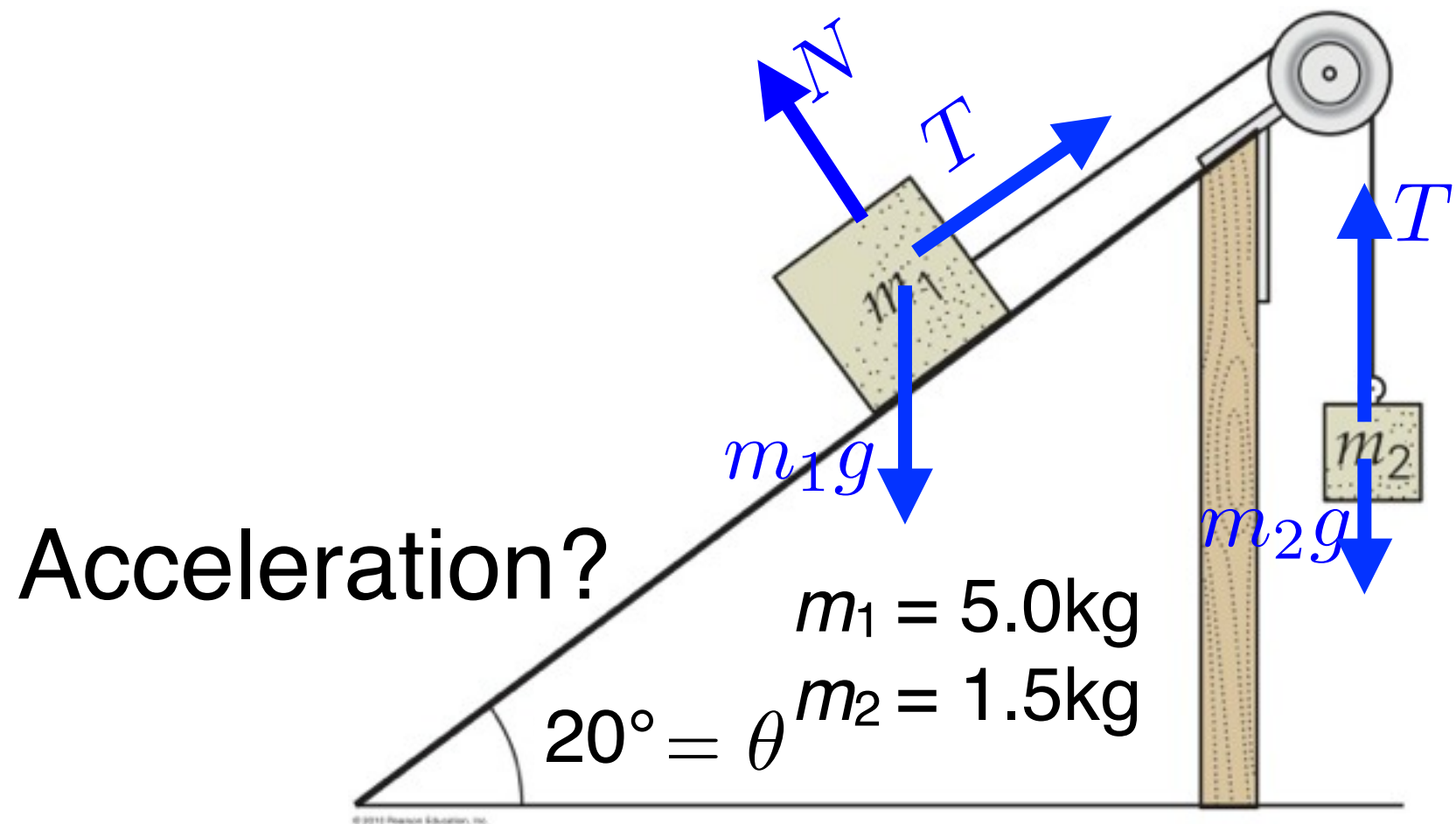
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1. Read carefully
2. Draw a sketch = space diagram



# Ex. 4.6

1. Read carefully
2. Draw a sketch = space diagram
3. Given? Goal?

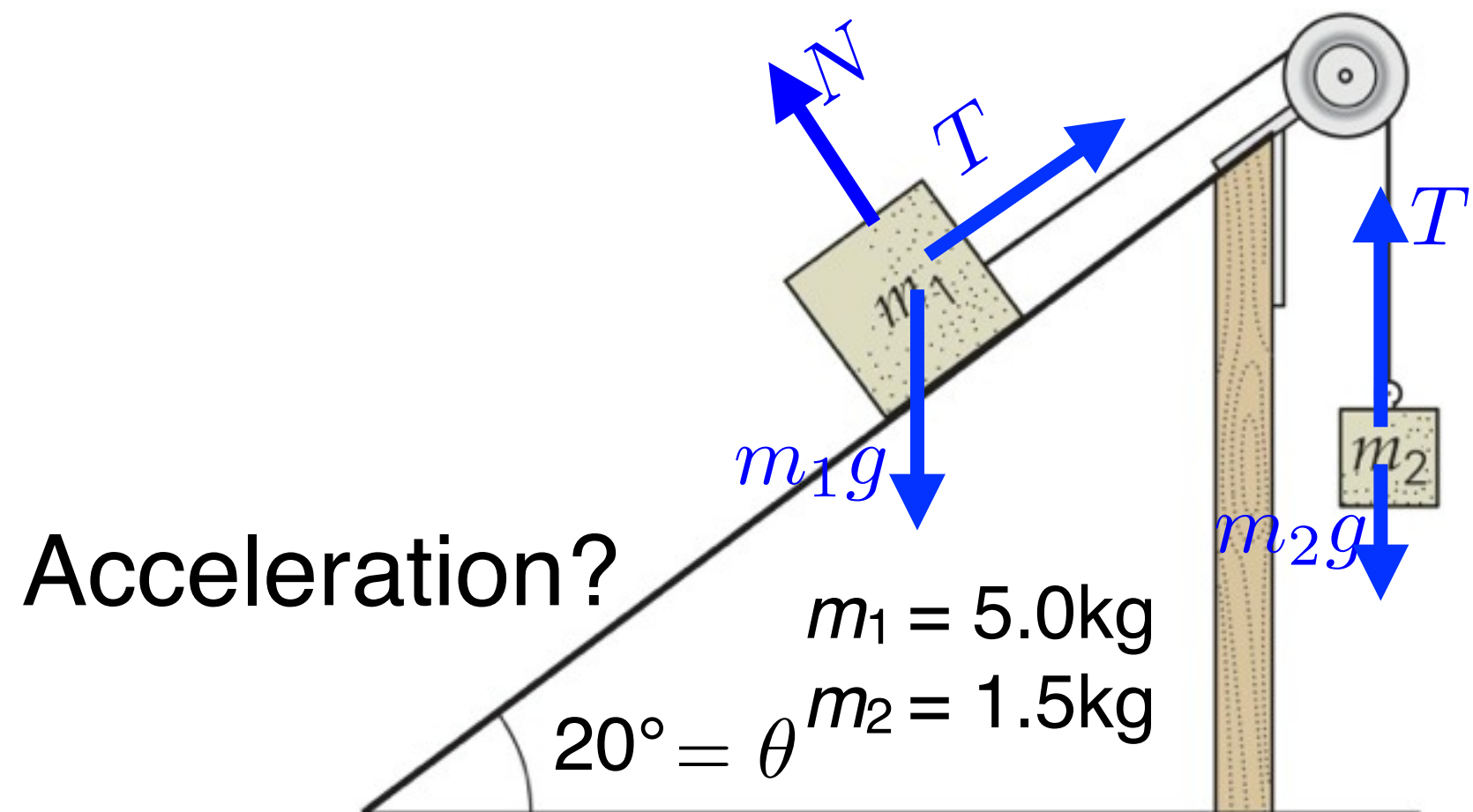




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Given:  $m_1$ ,  $m_2$ ,  $\theta$

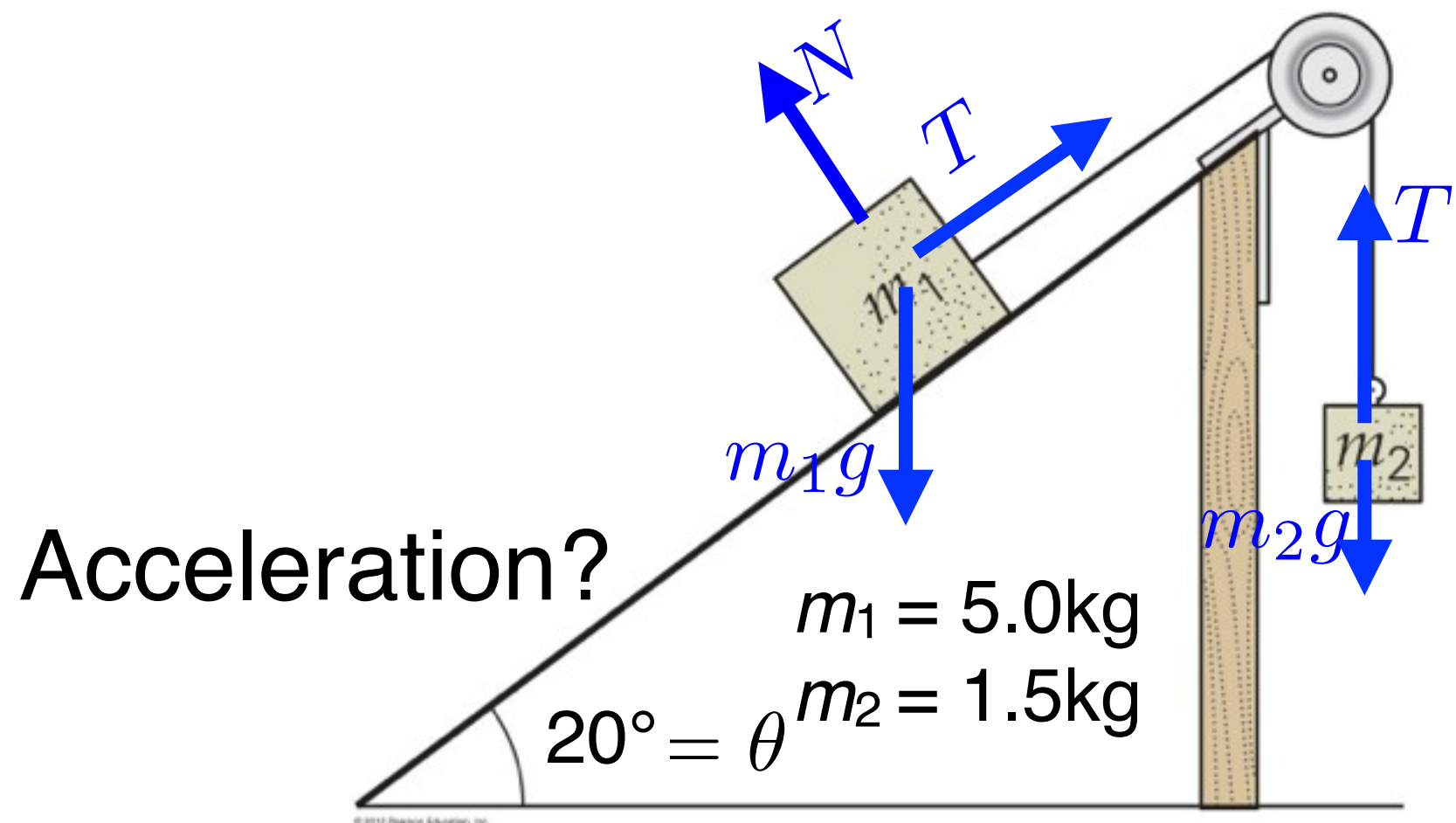
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# Ex. 4.6

Given:  $m_1, m_2, \theta$   
Goal:  $a$

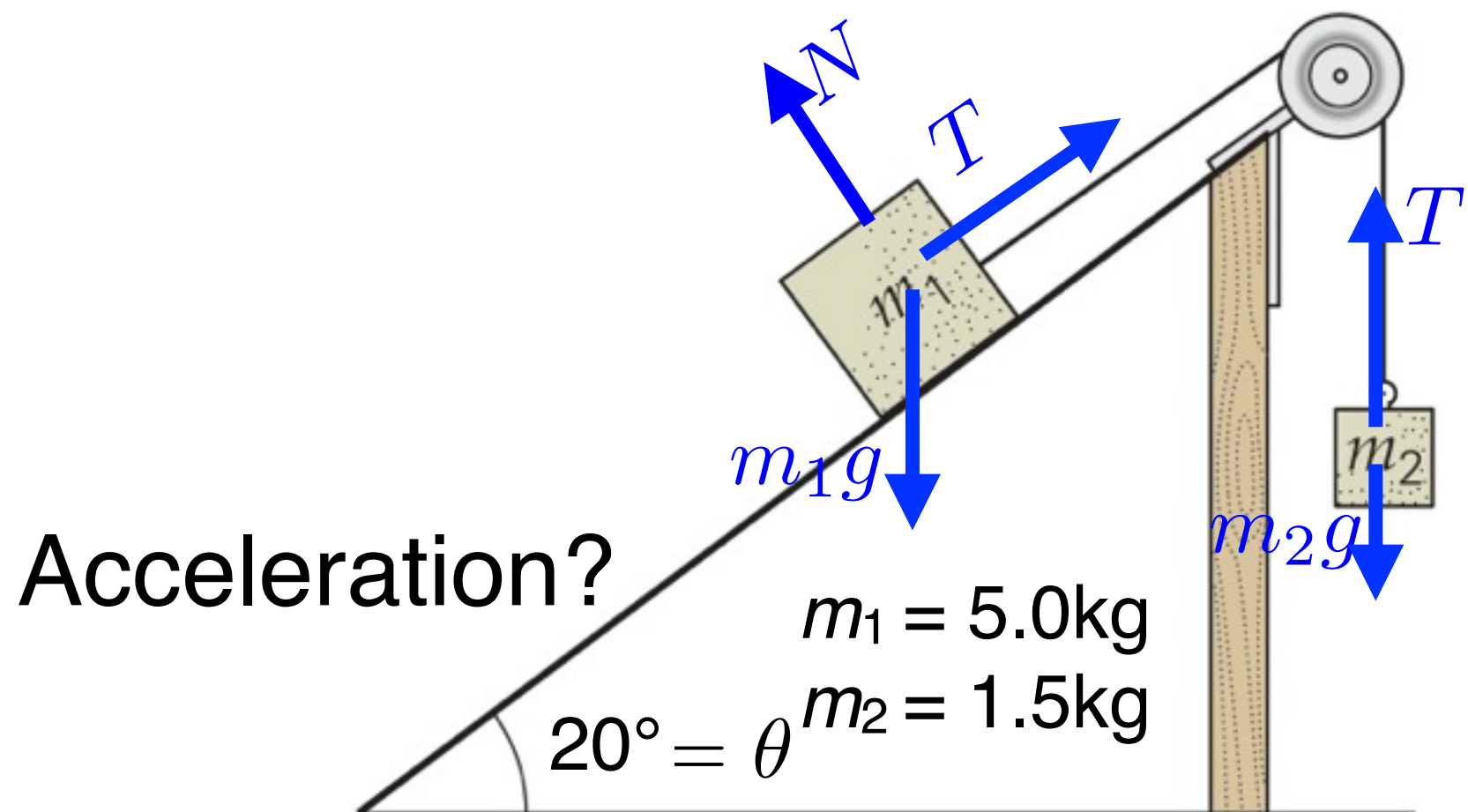
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Given:  $m_1, m_2, \theta$   
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4. Brainstorm: 2nd law problem

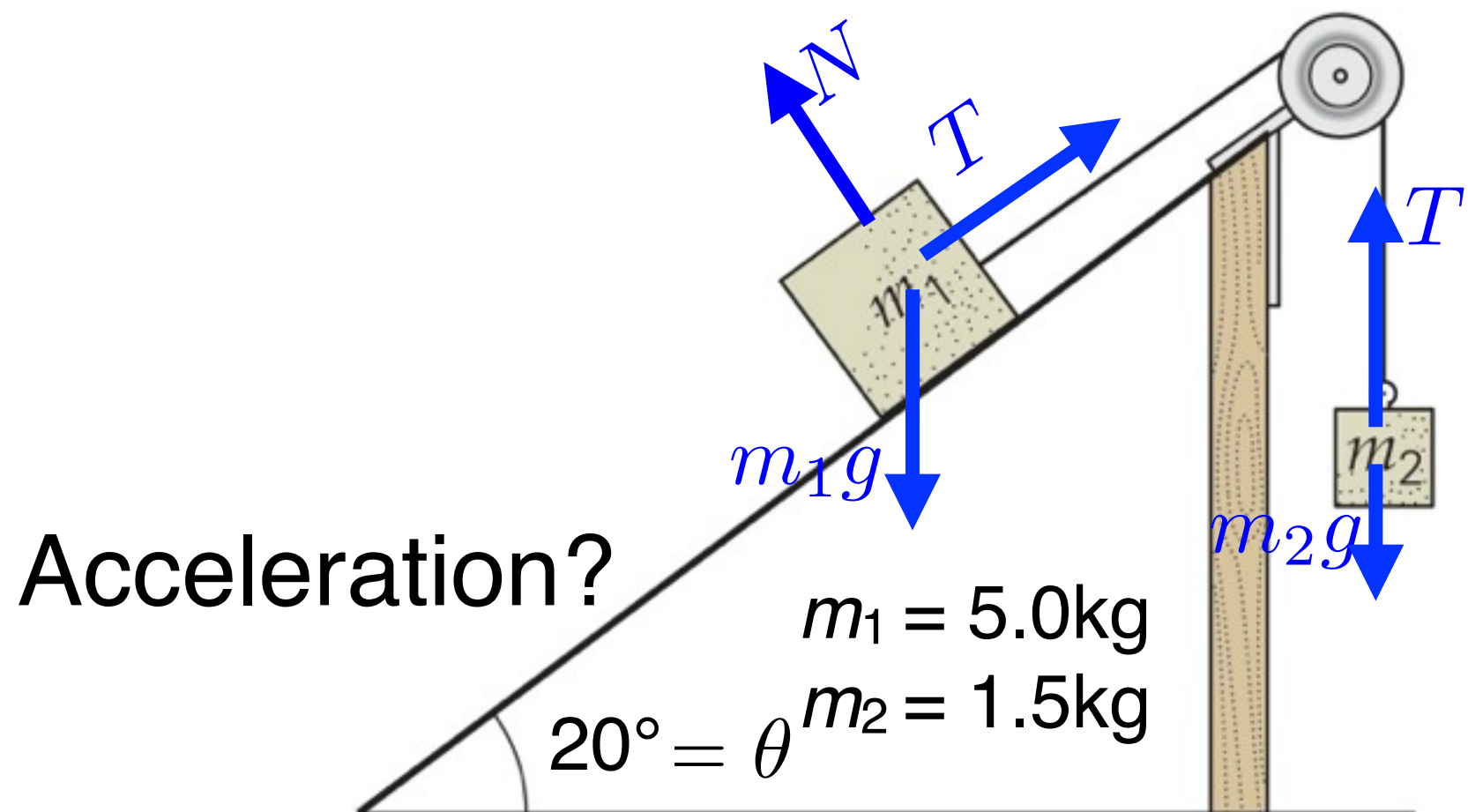


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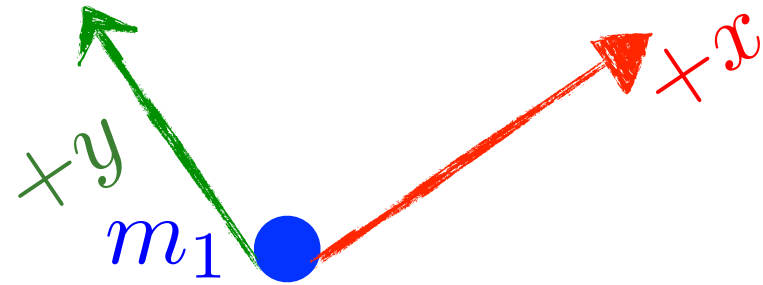
$m_1$  ●



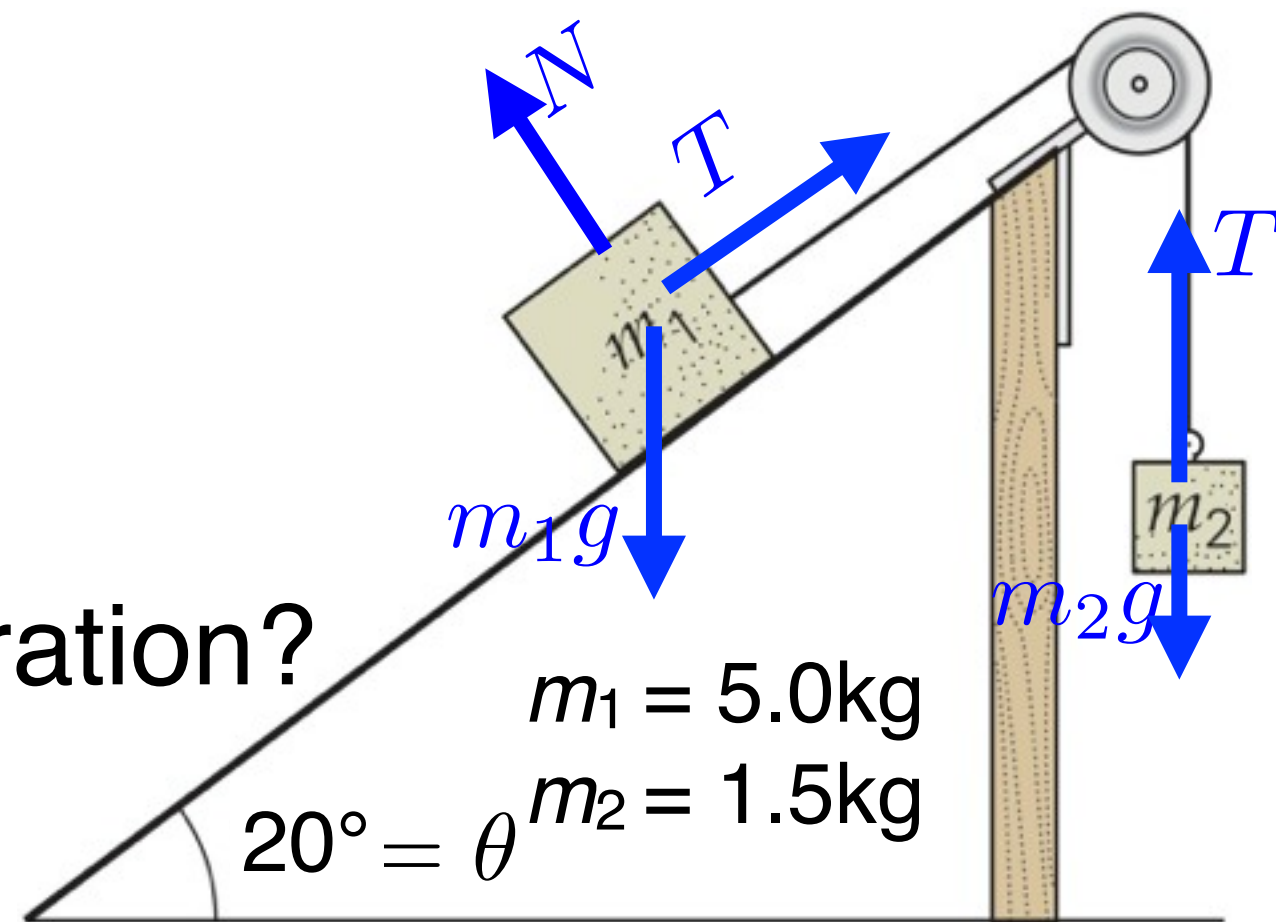
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  - 4a. For each body, draw a free-body diagram
    - i: draw axes: along accel., origin where forces applied



Acceleration?



$$m_1 = 5.0 \text{ kg}$$

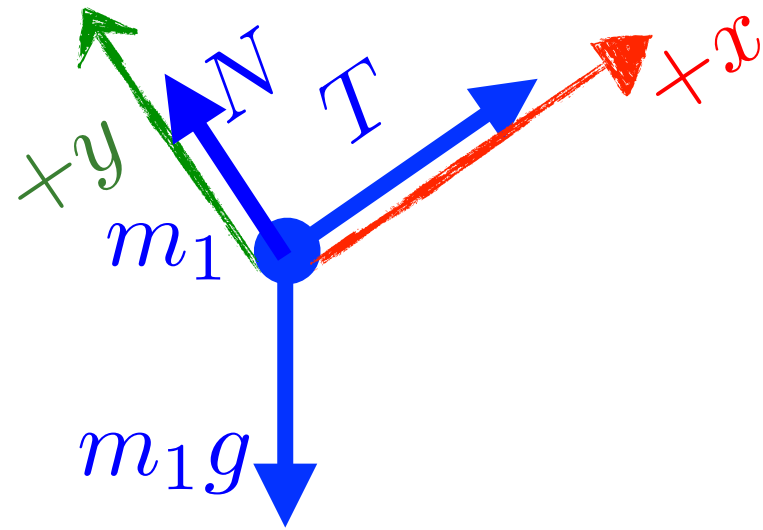
$$m_2 = 1.5 \text{ kg}$$

$$20^\circ = \theta$$

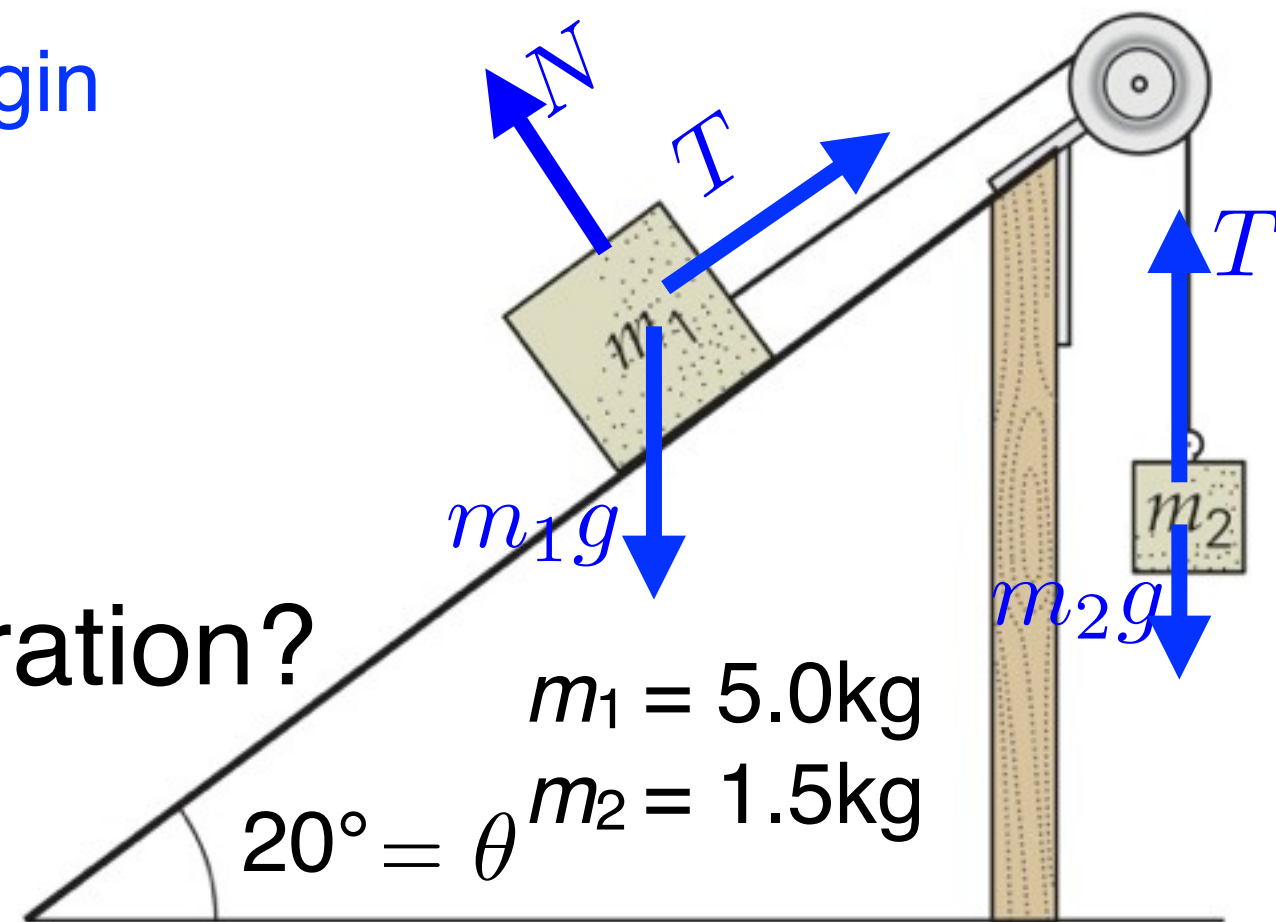
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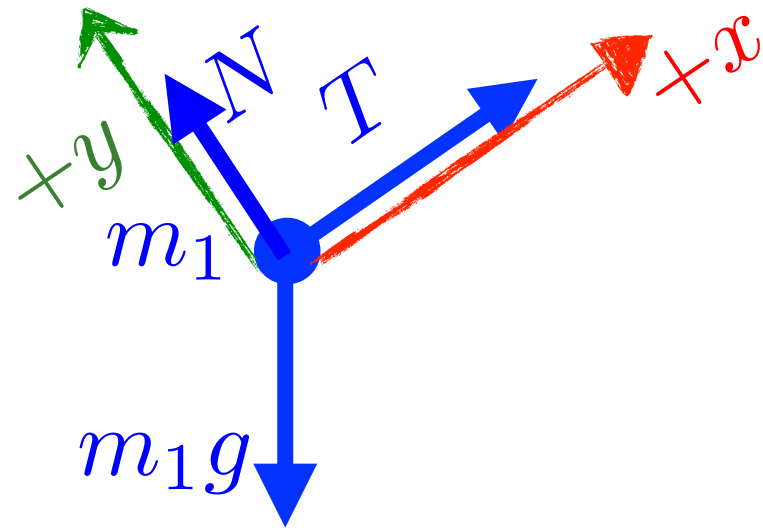
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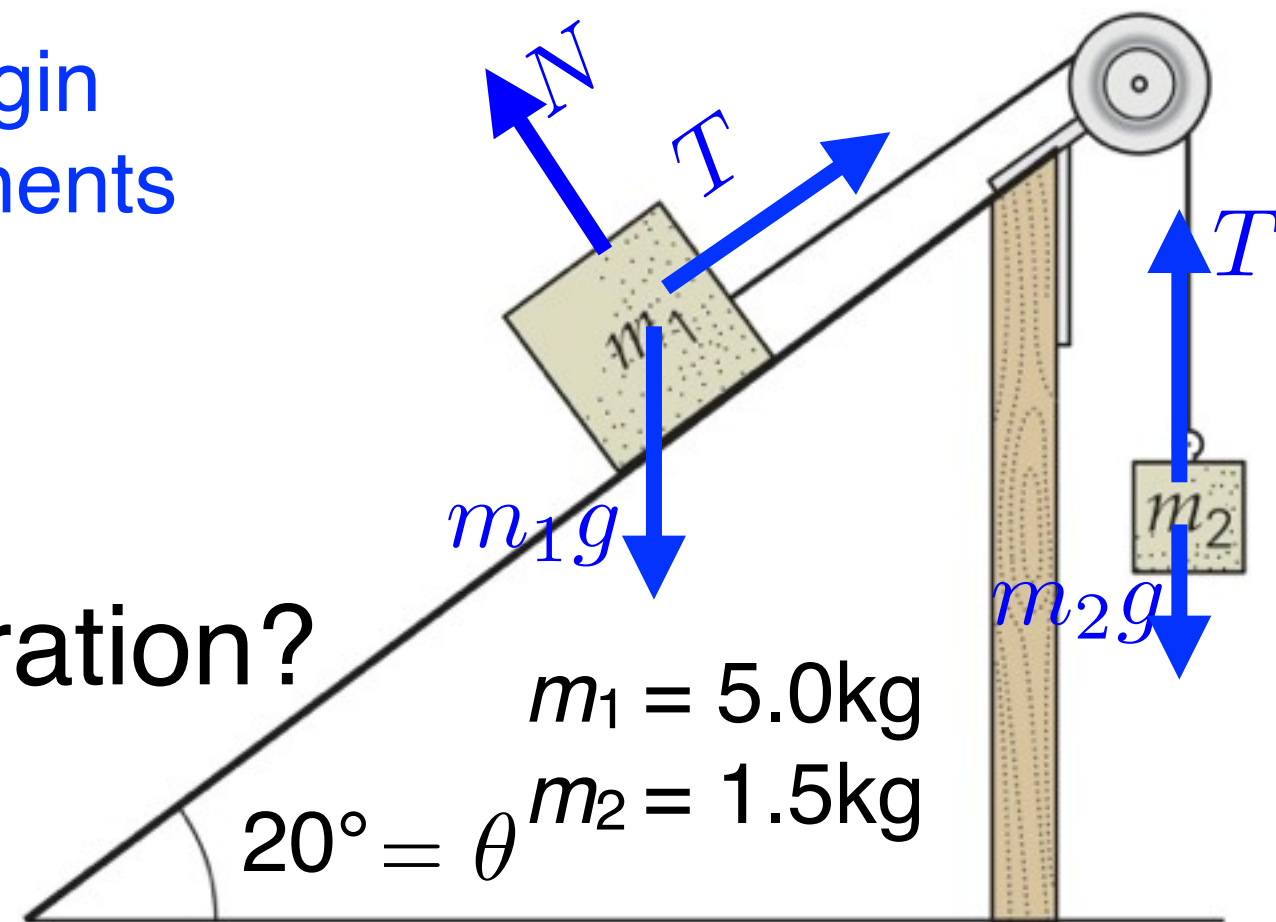
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    - iii: resolve forces into components



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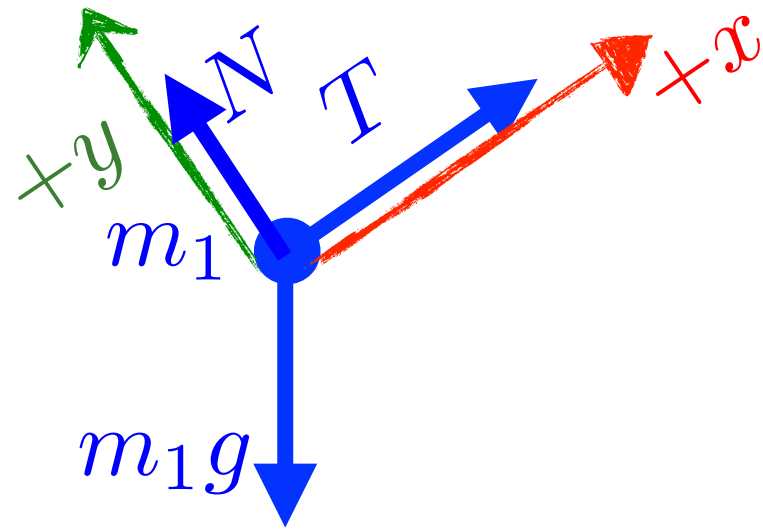
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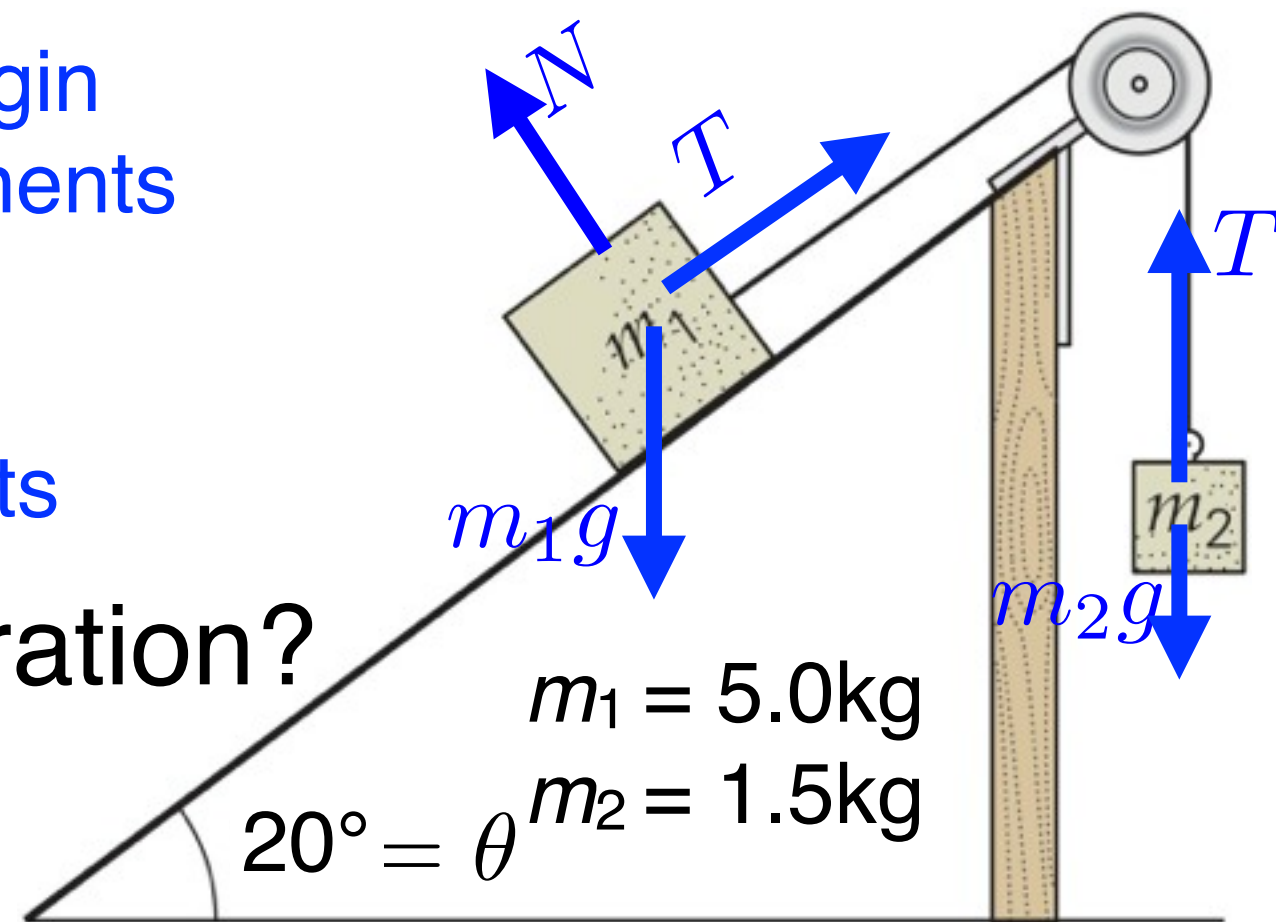
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    - iii: resolve forces into components
      - Use colors
      - OR draw new, separate diagrams for x,y components



Acceleration?

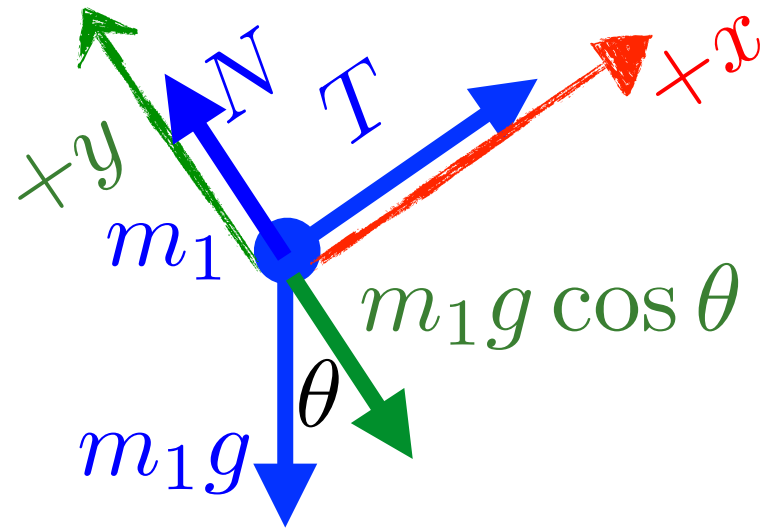




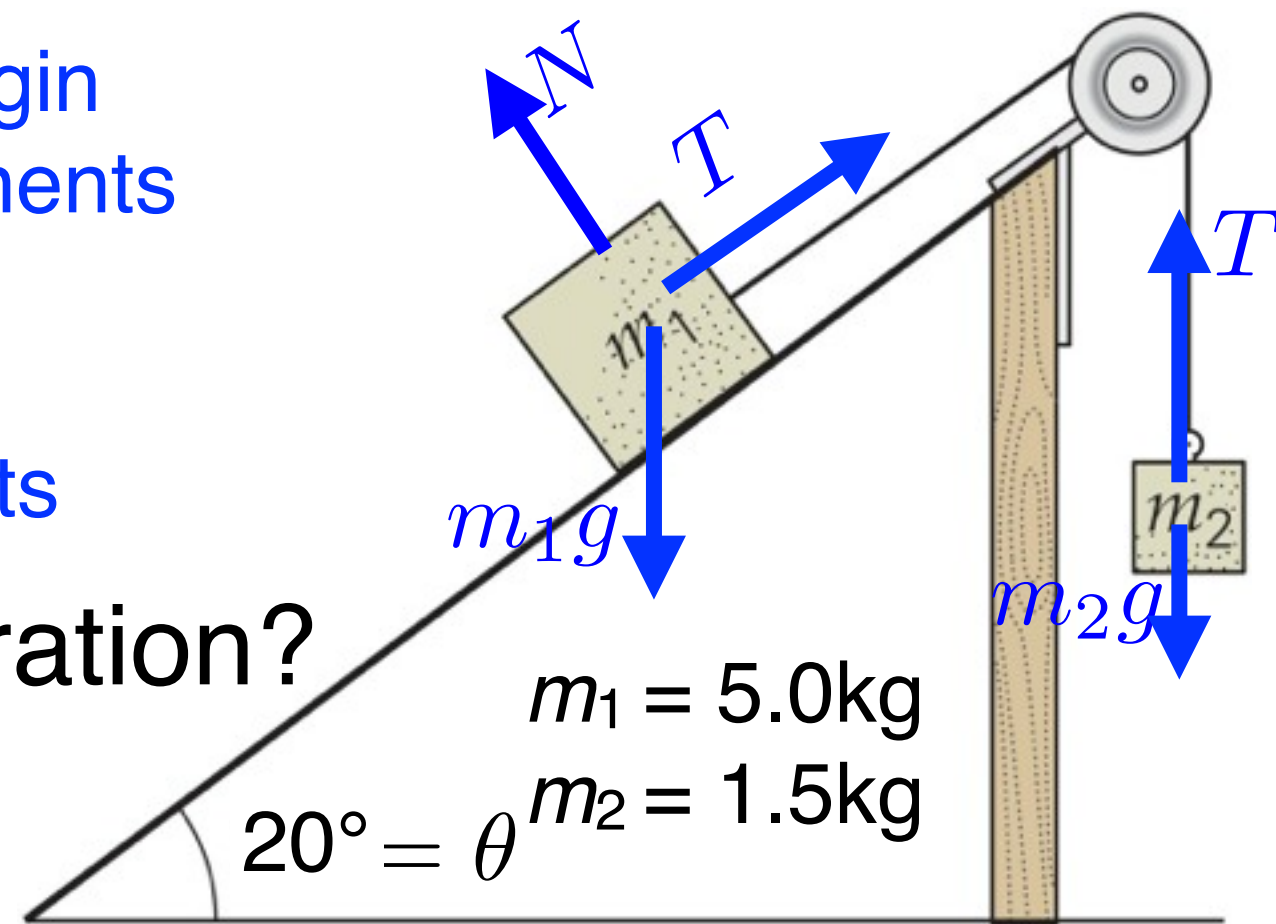
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    - i: draw axes: along accel., origin where forces applied
    - ii: draw force vectors from origin
    - iii: resolve forces into components
      - Use colors
      - OR draw new, separate diagrams for x,y components



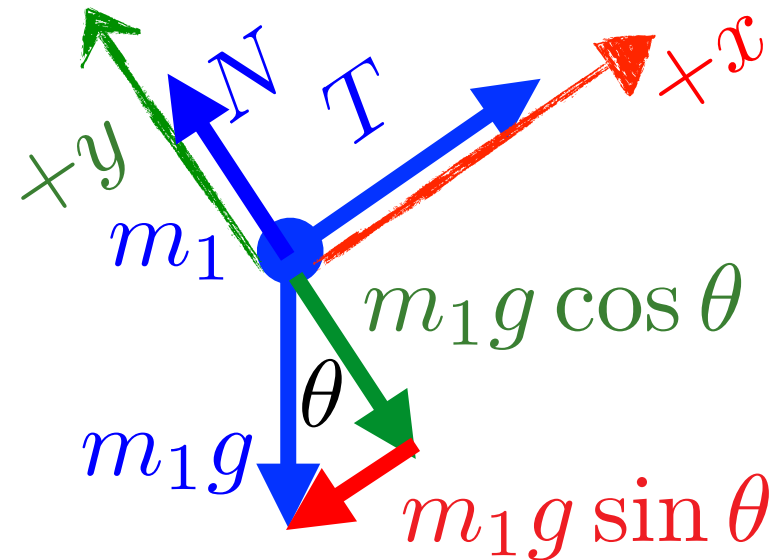
Acceleration?



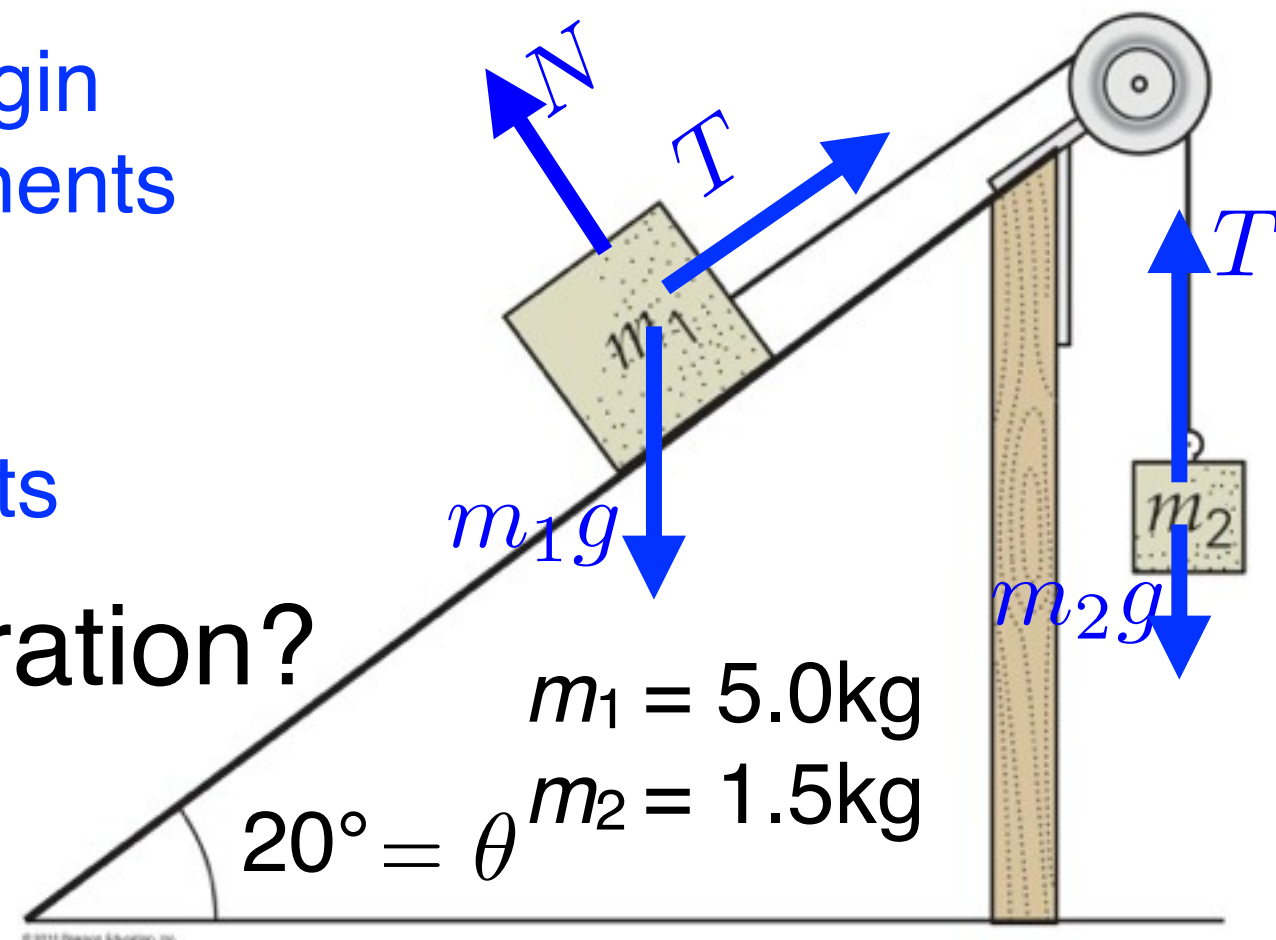
# Ex. 4.6

Given:  $m_1, m_2, \theta$   
Goal:  $a$

1. Read carefully
2. Draw a sketch = space diagram
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  - 4a. For each body, draw a free-body diagram
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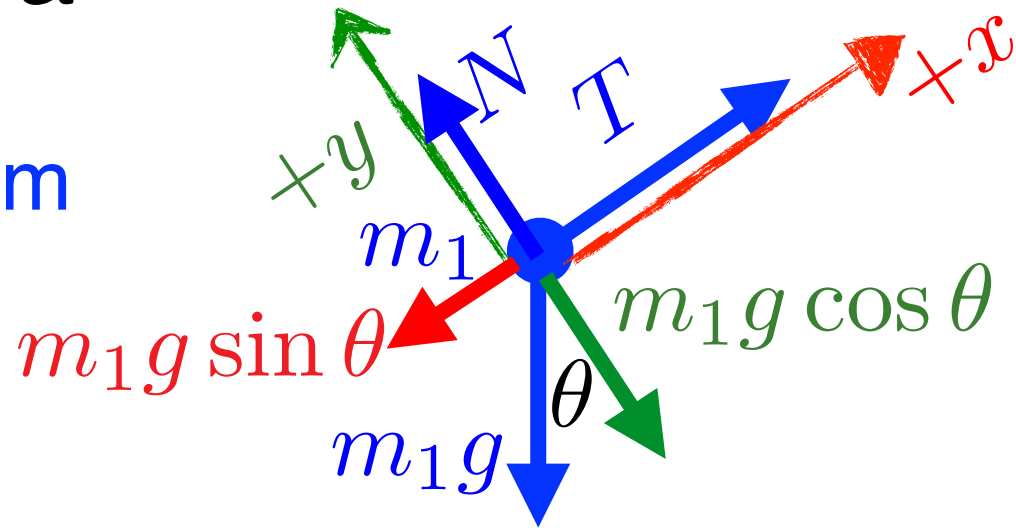
Acceleration?



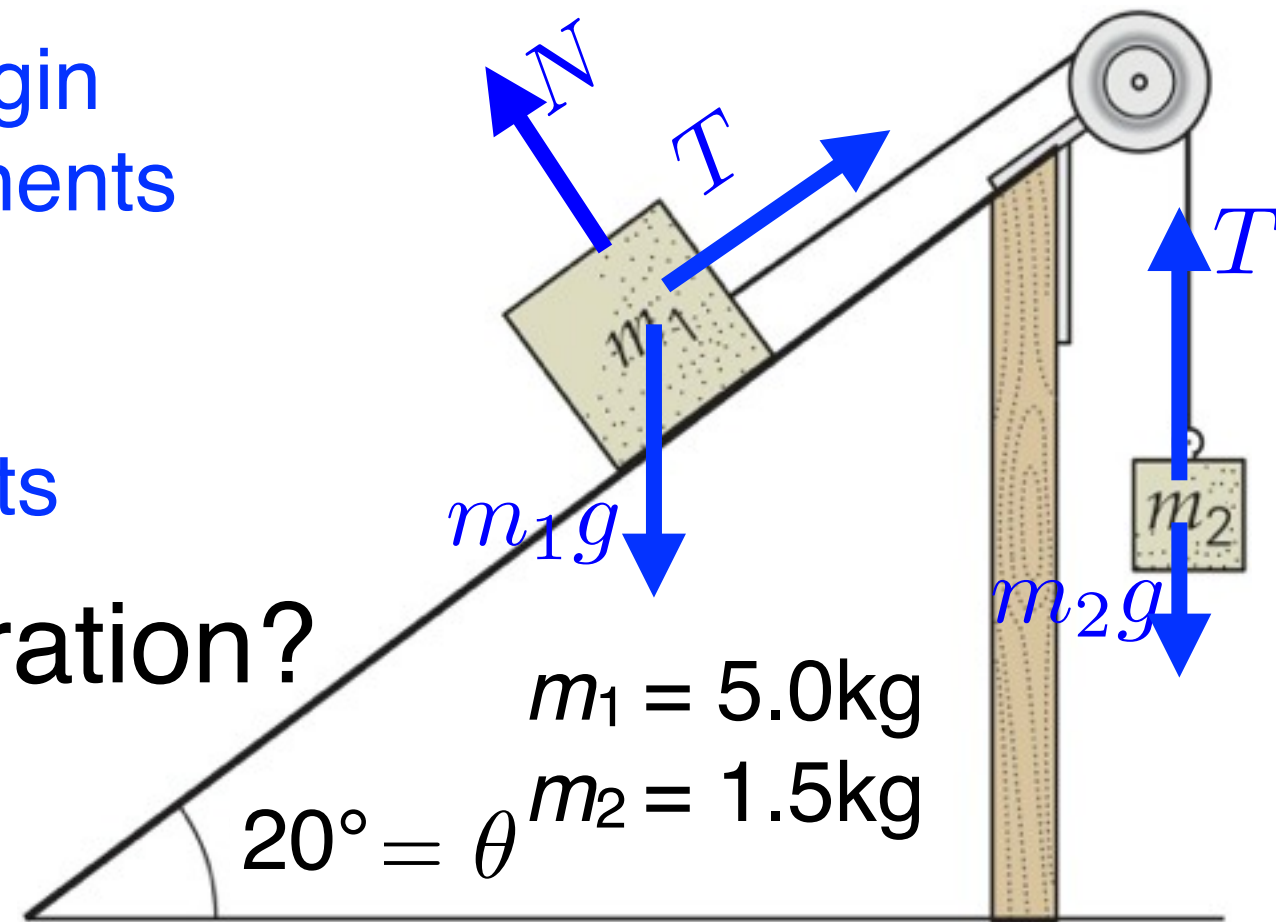
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Goal:  $a$

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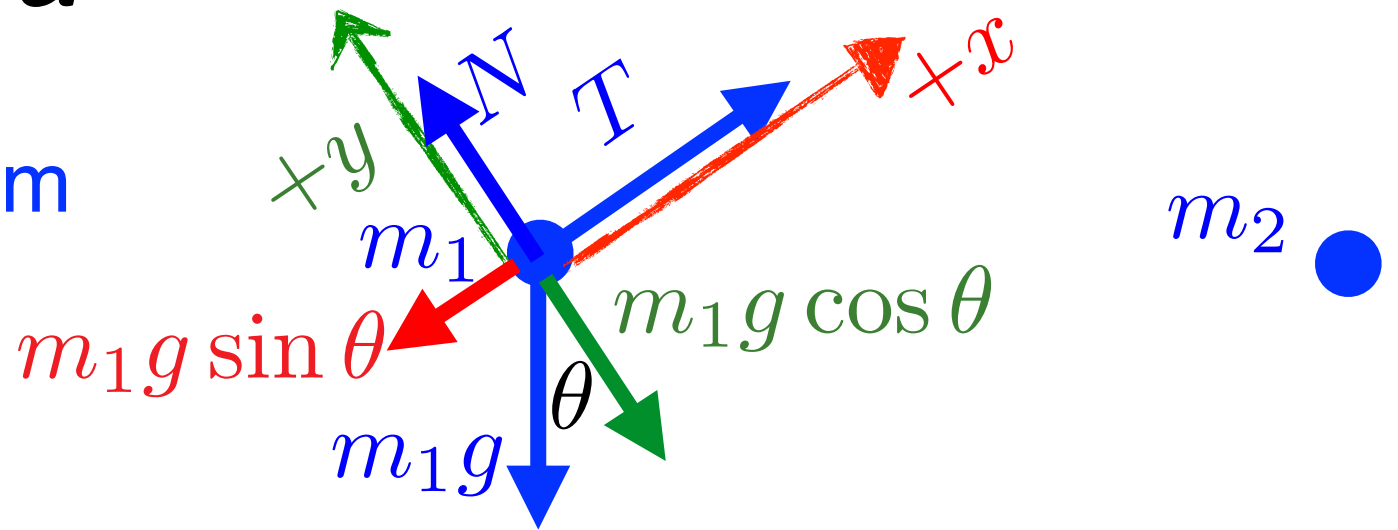
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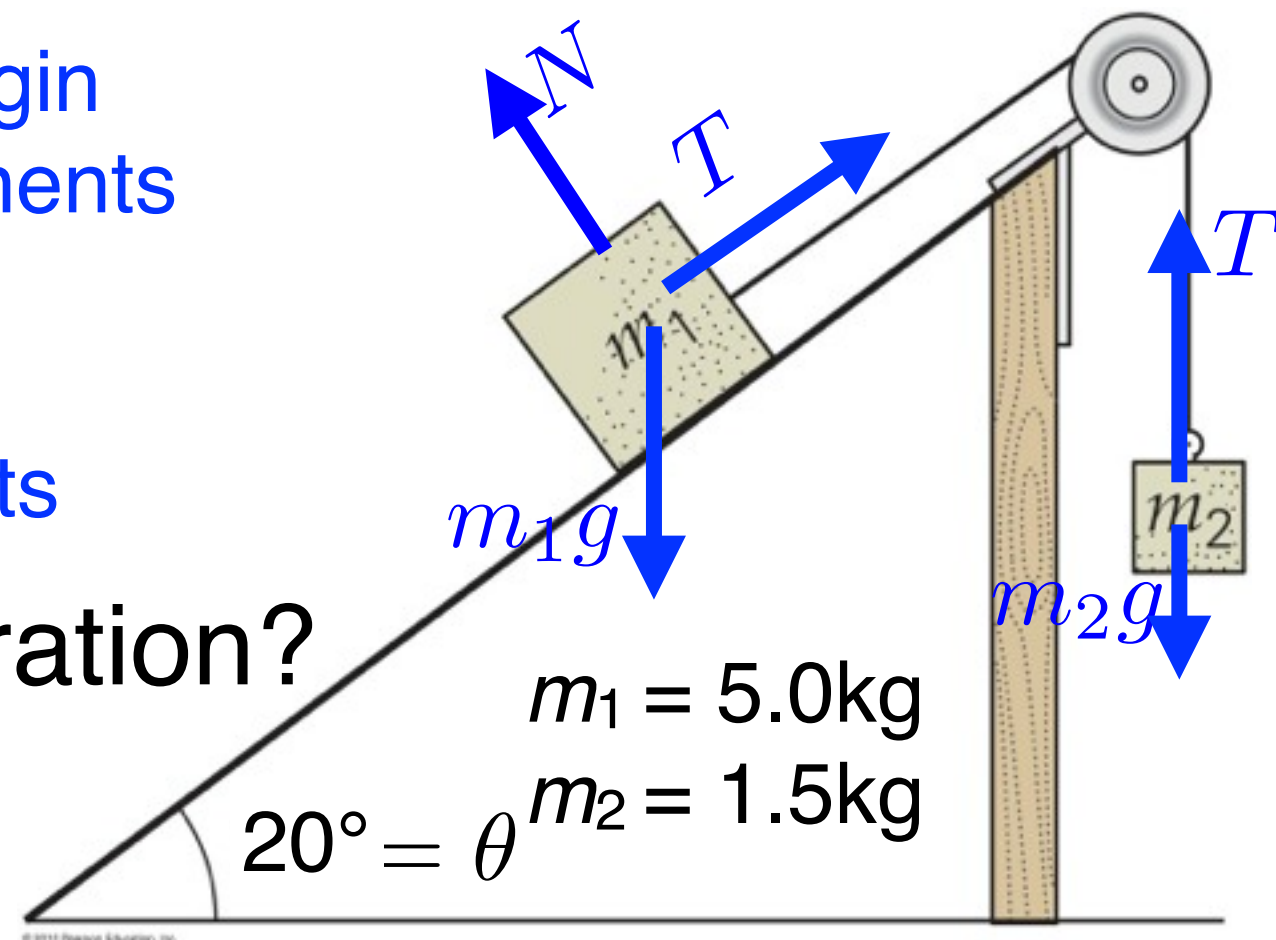
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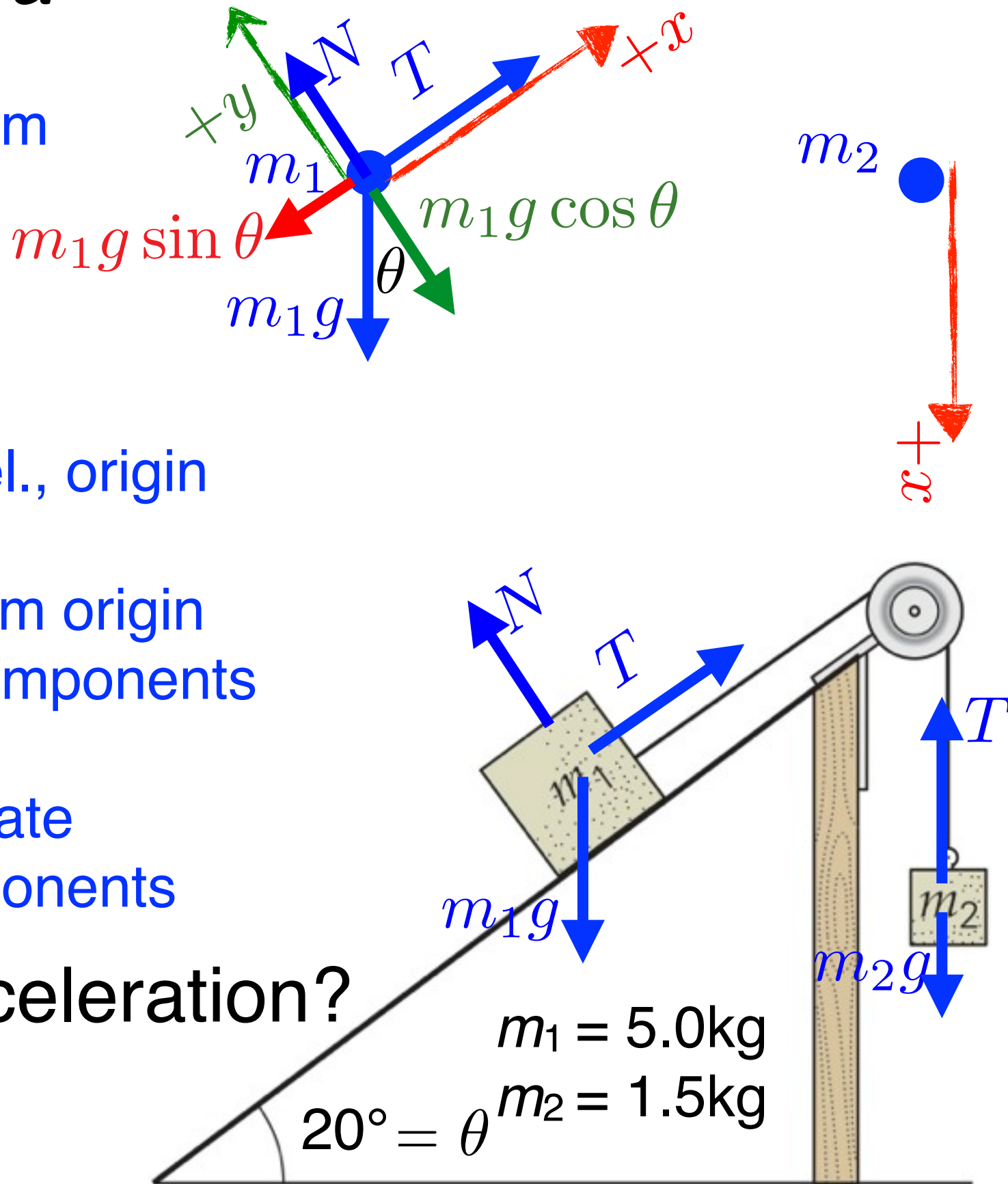
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Goal:  $a$

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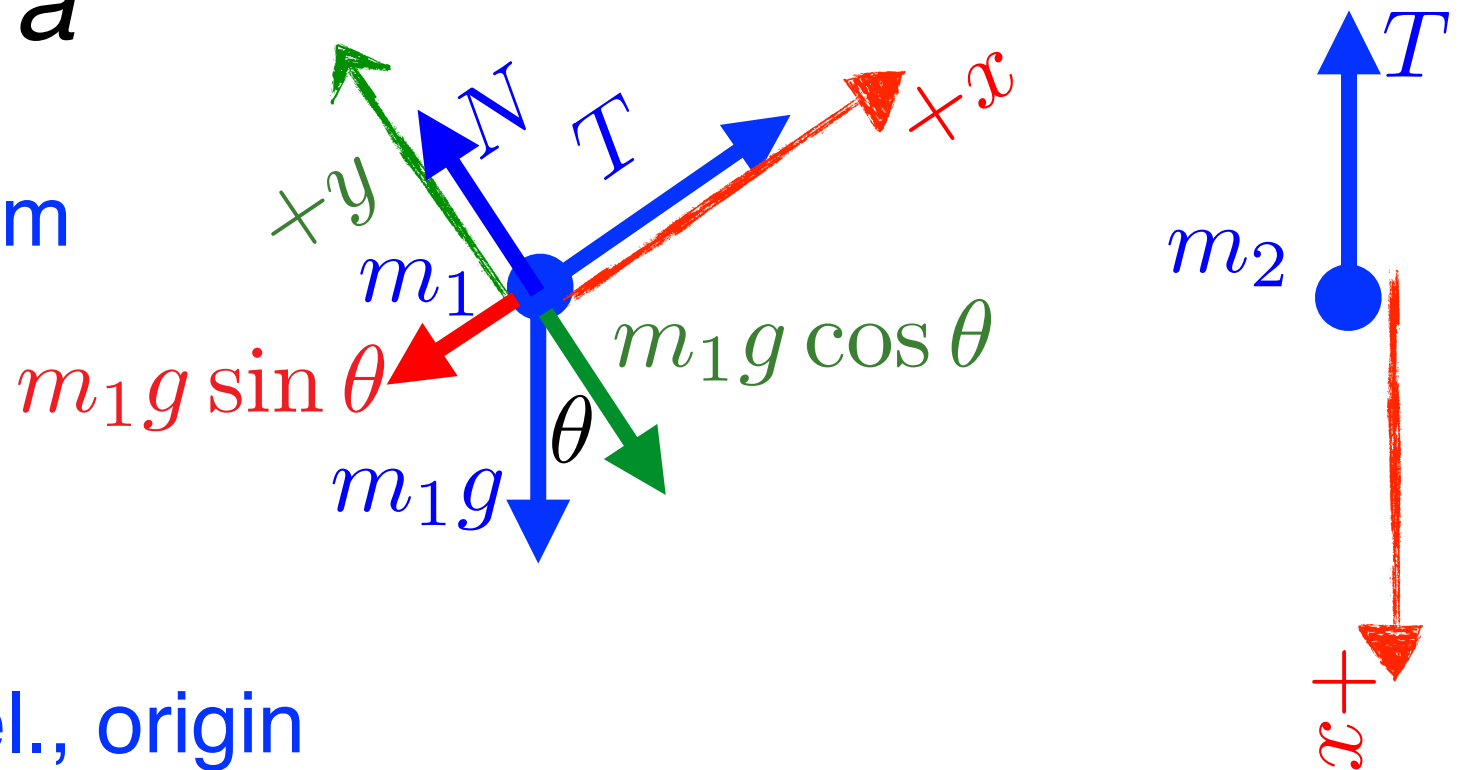
Acceleration?



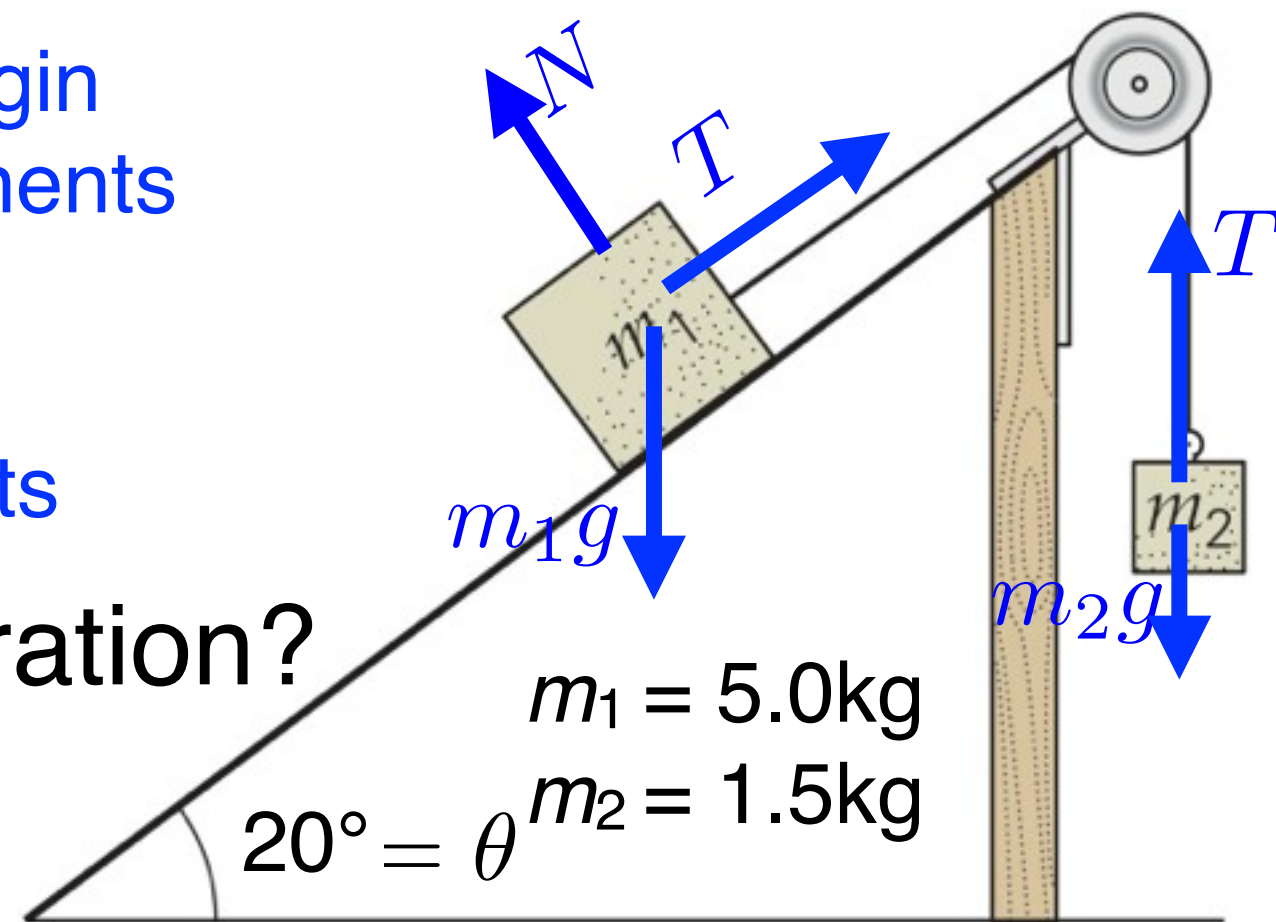
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Goal:  $a$

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Acceleration?



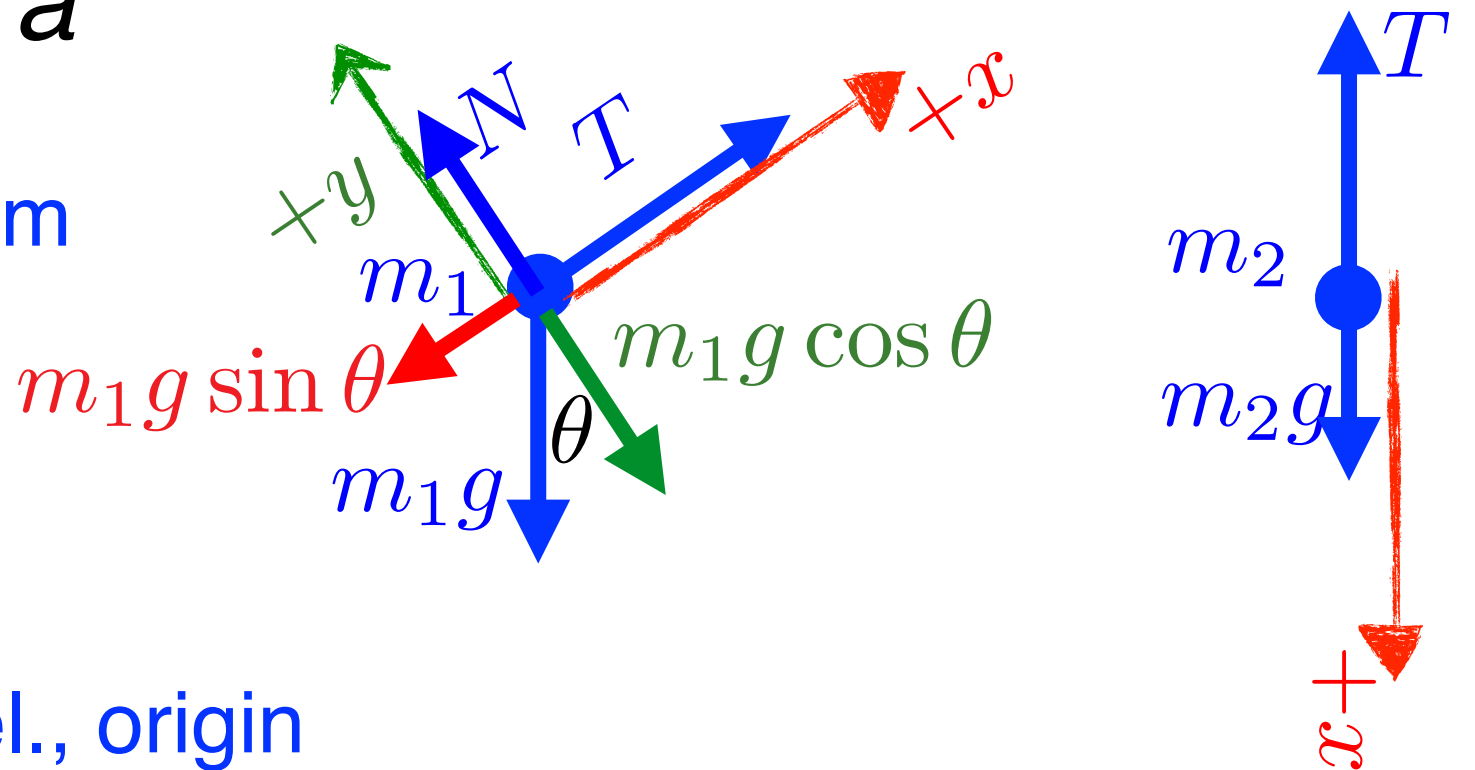
$$m_1 = 5.0\text{kg}$$

$$m_2 = 1.5\text{kg}$$

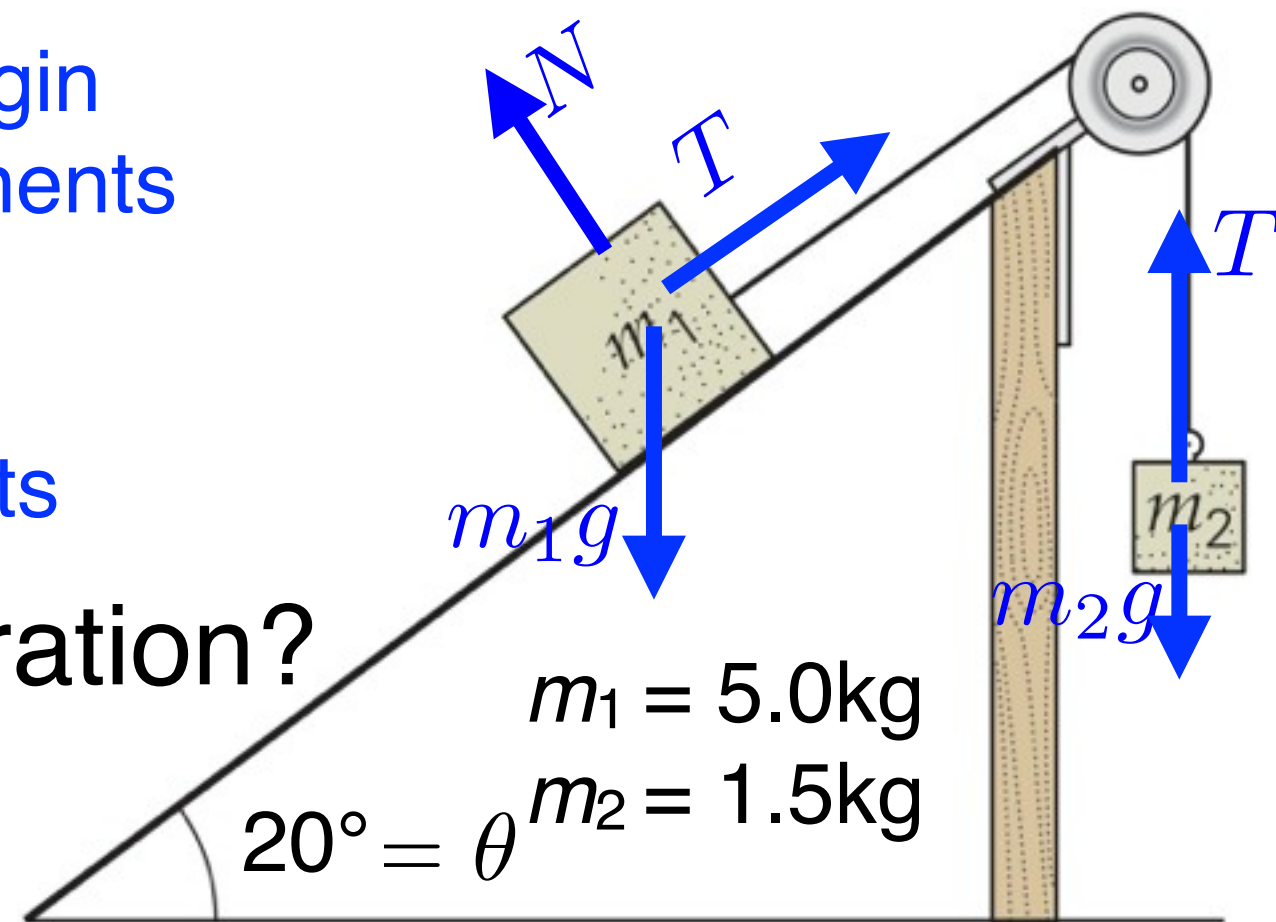
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Acceleration?



$$m_1 = 5.0\text{kg}$$

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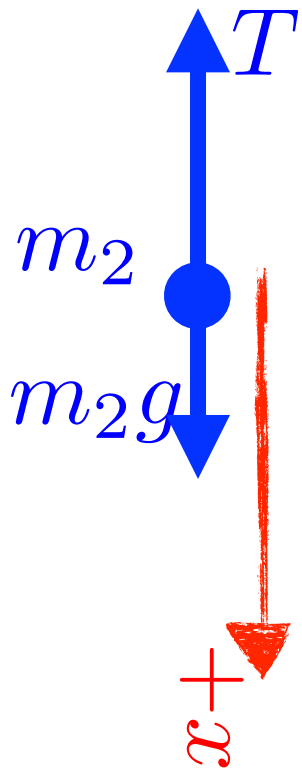
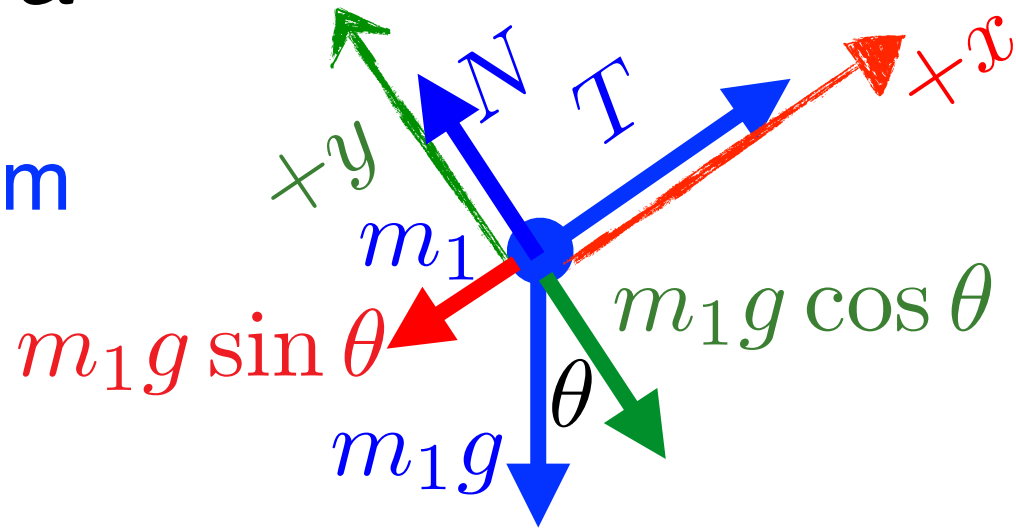
# Ex. 4.6



# Ex. 4.6

Given:  $m_1, m_2, \theta$   
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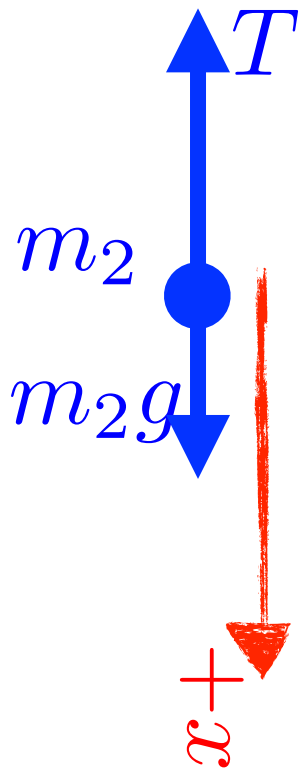
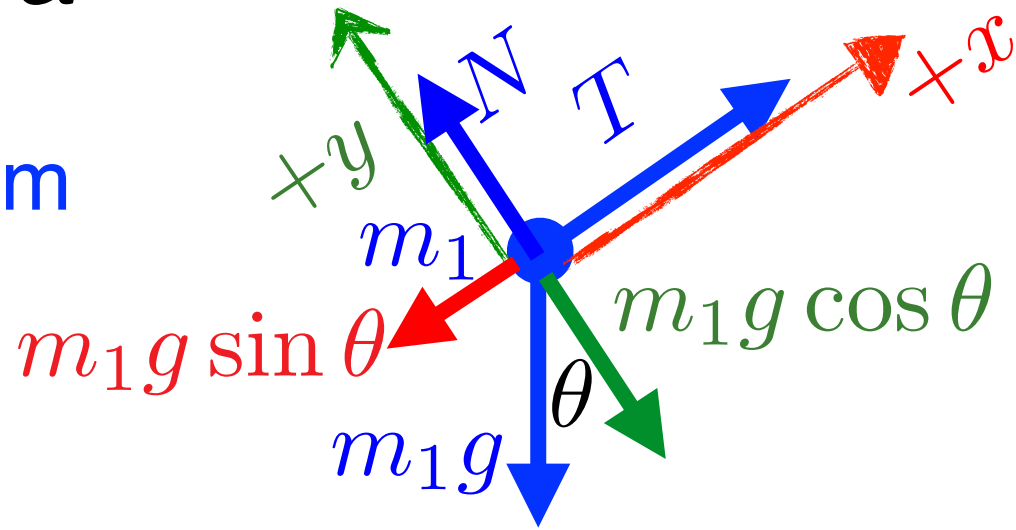
1. Read carefully
2. Draw a sketch = space diagram
3. Given? Goal?
4. Brainstorm: 2nd law problem
  - 4a. For each body, draw a free-body diagram



# Ex. 4.6

Given:  $m_1, m_2, \theta$   
Goal:  $a$

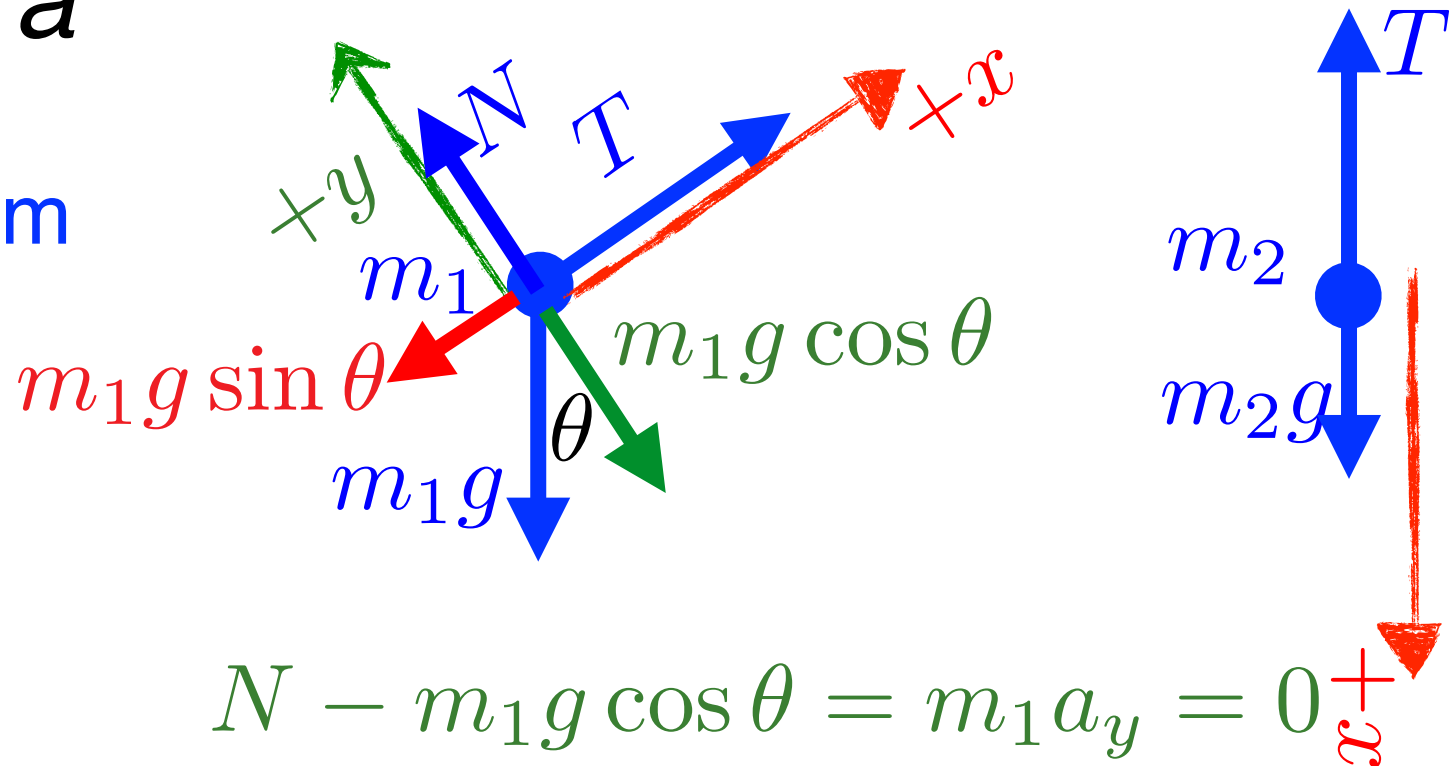
1. Read carefully
2. Draw a sketch = space diagram
3. Given? Goal?
4. Brainstorm: 2nd law problem
  - 4a. For each body, draw a free-body diagram
  - 4b. Apply Newton's 2nd law



# Ex. 4.6

Given:  $m_1, m_2, \theta$   
Goal:  $a$

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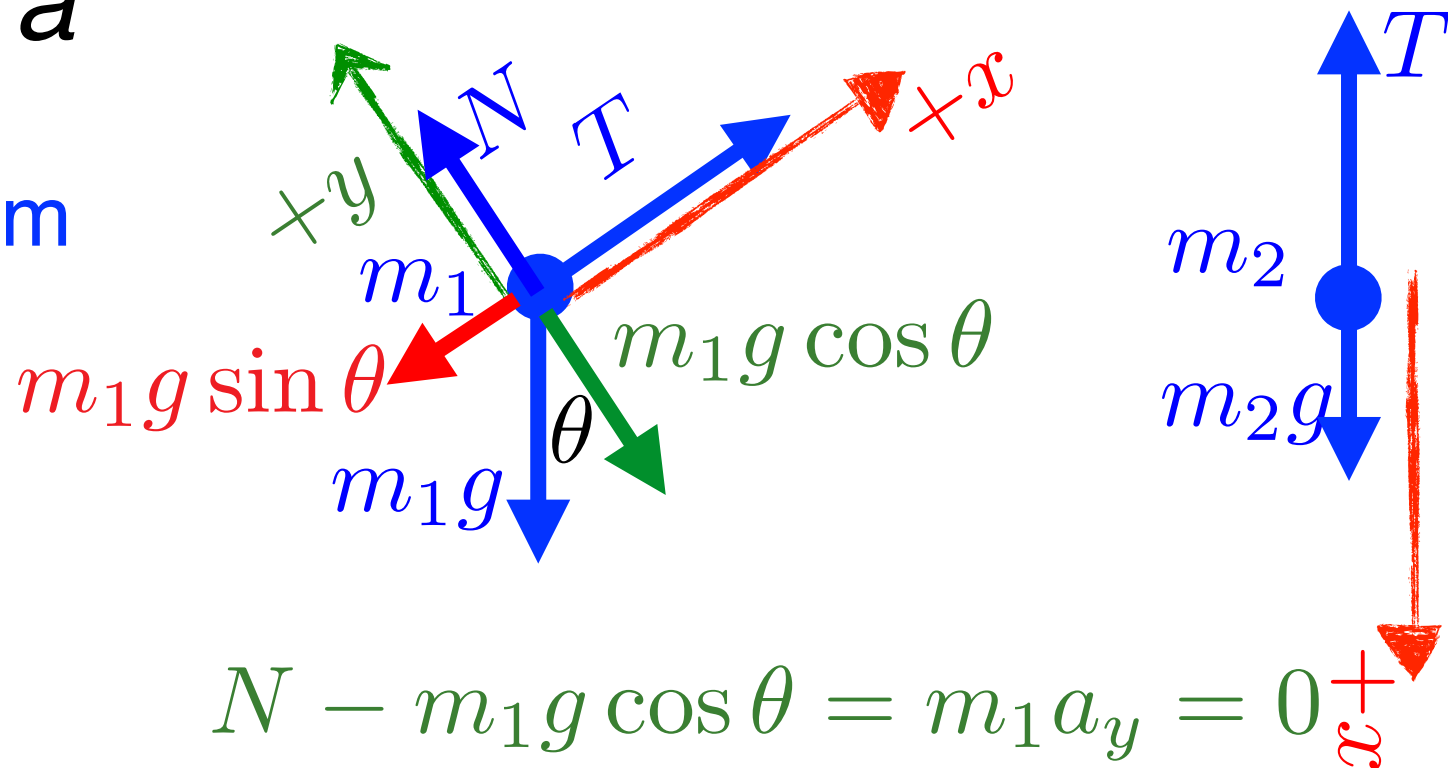


# Ex. 4.6

Given:  $m_1, m_2, \theta$

Goal:  $a$

1. Read carefully
2. Draw a sketch = space diagram
3. Given? Goal?
4. Brainstorm: 2nd law problem
  - 4a. For each body, draw a free-body diagram
  - 4b. Apply Newton's 2nd law



$$N - m_1 g \cos \theta = m_1 a_y = 0$$

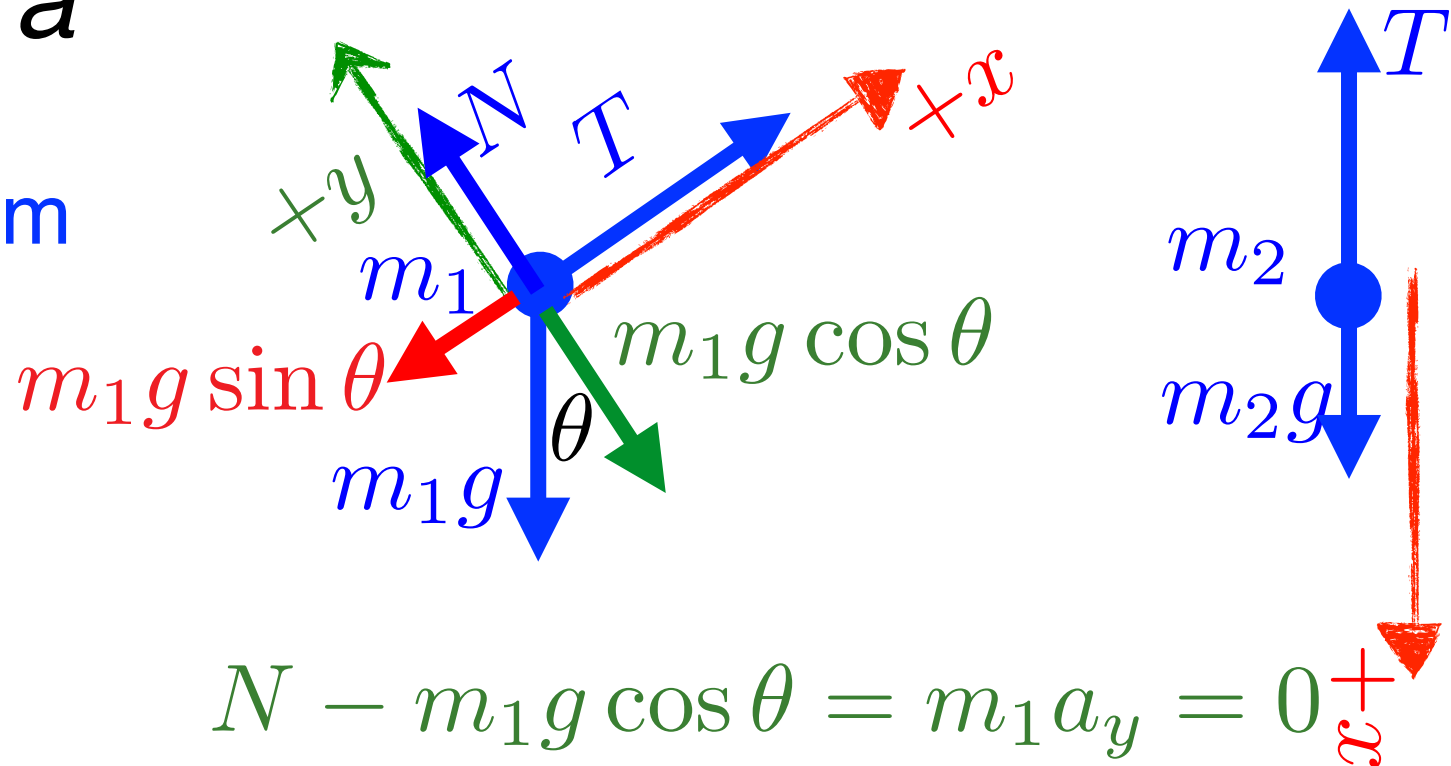
$$T - m_1 g \sin \theta = m_1 a_x = m_1 a$$

# Ex. 4.6

Given:  $m_1, m_2, \theta$

Goal:  $a$

1. Read carefully
2. Draw a sketch = space diagram
3. Given? Goal?
4. Brainstorm: 2nd law problem
  - 4a. For each body, draw a free-body diagram
  - 4b. Apply Newton's 2nd law



$$T - m_1 g \sin \theta = m_1 a_x = m_1 a$$
$$m_2 g - T = m_2 a_x = m_2 a$$

# Ex. 4.6

Given:  $m_1, m_2, \theta$

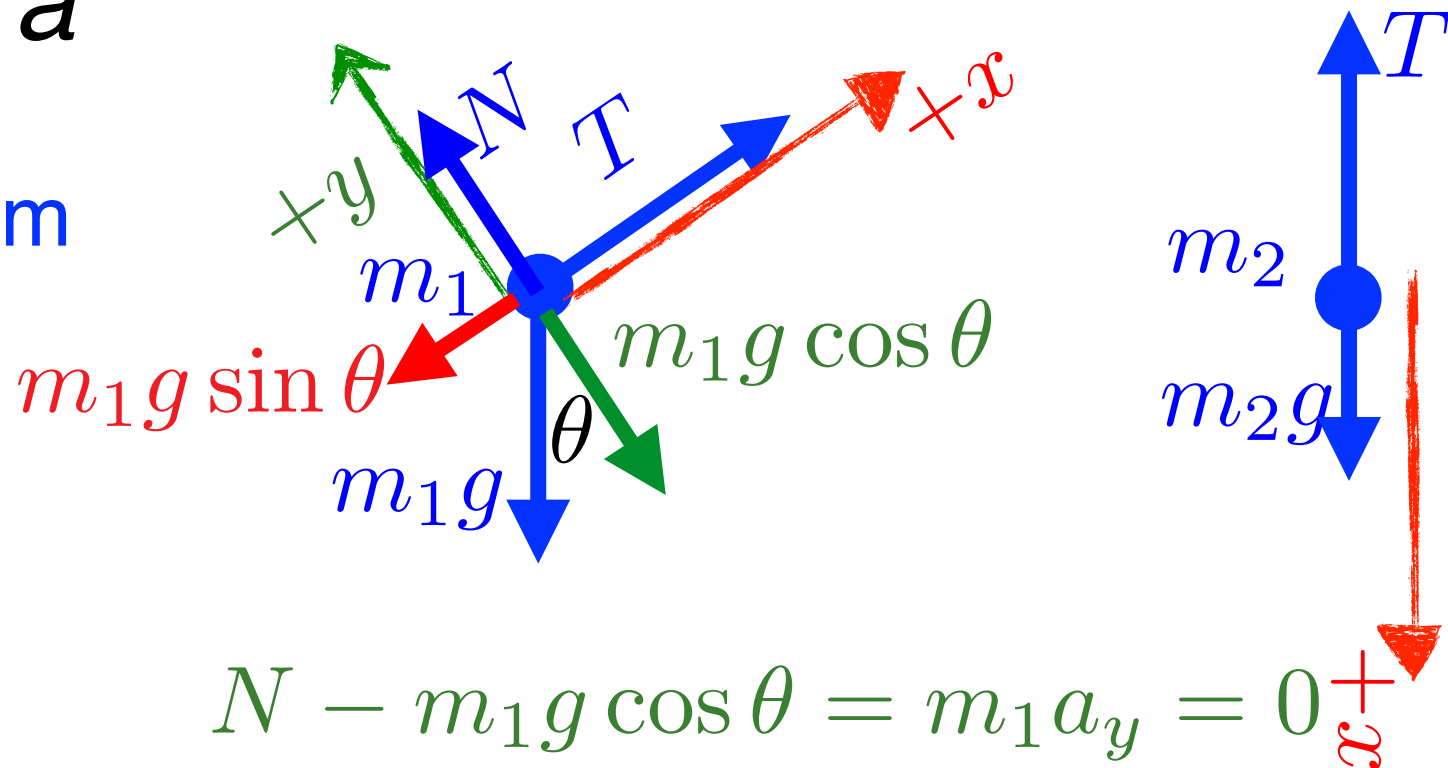
Goal:  $a$

1. Read carefully
2. Draw a sketch = space diagram
3. Given? Goal?
4. Brainstorm: 2nd law problem

4a. For each body, draw a free-body diagram

4b. Apply Newton's 2nd law

*Note: if const. force, constant acceleration kinematic equations also apply*



$$N - m_1 g \cos \theta = m_1 a_y = 0$$

$$T - m_1 g \sin \theta = m_1 a_x = m_1 a$$
$$m_2 g - T = m_2 a_x = m_2 a$$

# Ex. 4.6

Given:  $m_1, m_2, \theta$

Goal:  $a$

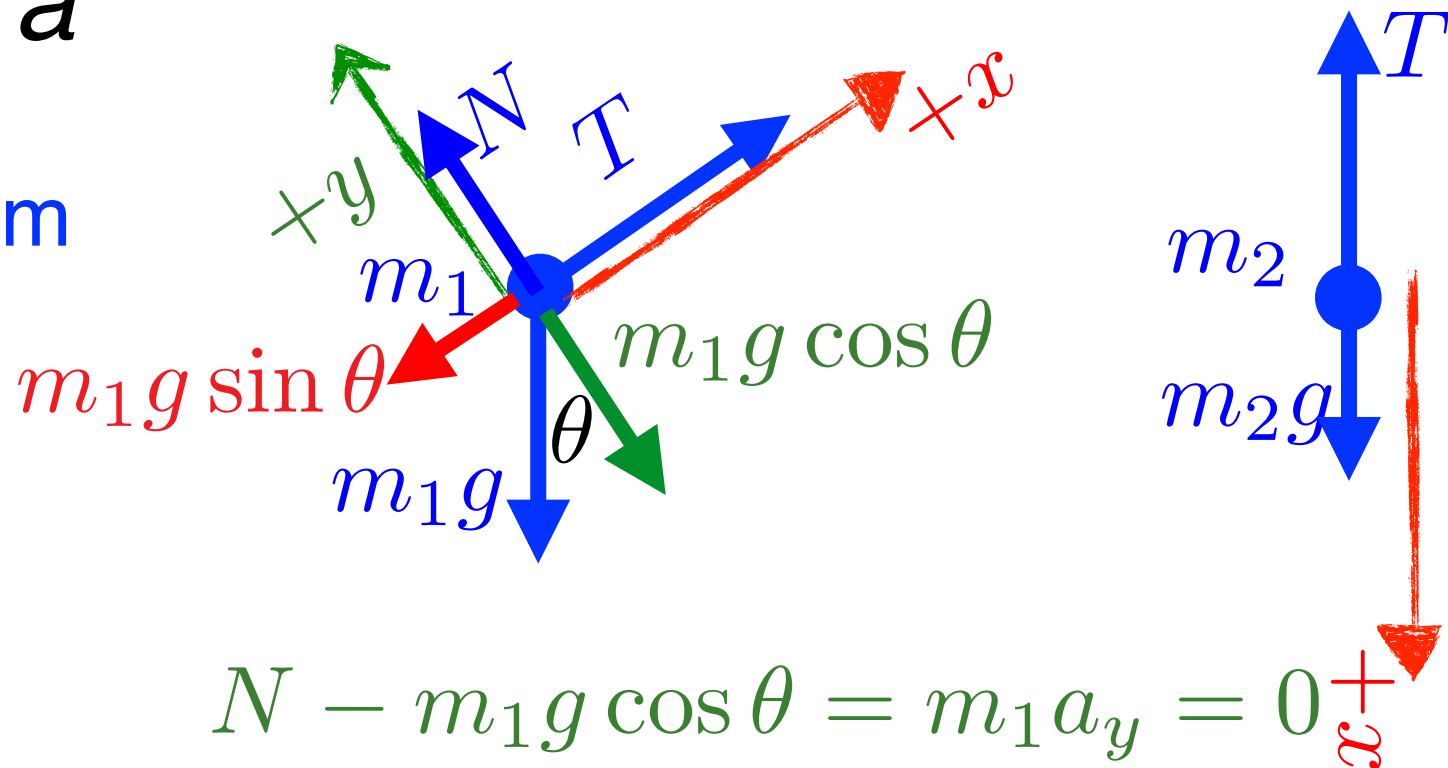
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4. Brainstorm: 2nd law problem

4a. For each body, draw a free-body diagram

4b. Apply Newton's 2nd law

*Note: if const. force, constant acceleration kinematic equations also apply*

5. Calculate



$$N - m_1 g \cos \theta = m_1 a_y = 0 \quad \uparrow$$

$$T - m_1 g \sin \theta = m_1 a_x = m_1 a$$
$$m_2 g - T = m_2 a_x = m_2 a$$

# Ex. 4.6

Given:  $m_1, m_2, \theta$

Goal:  $a$

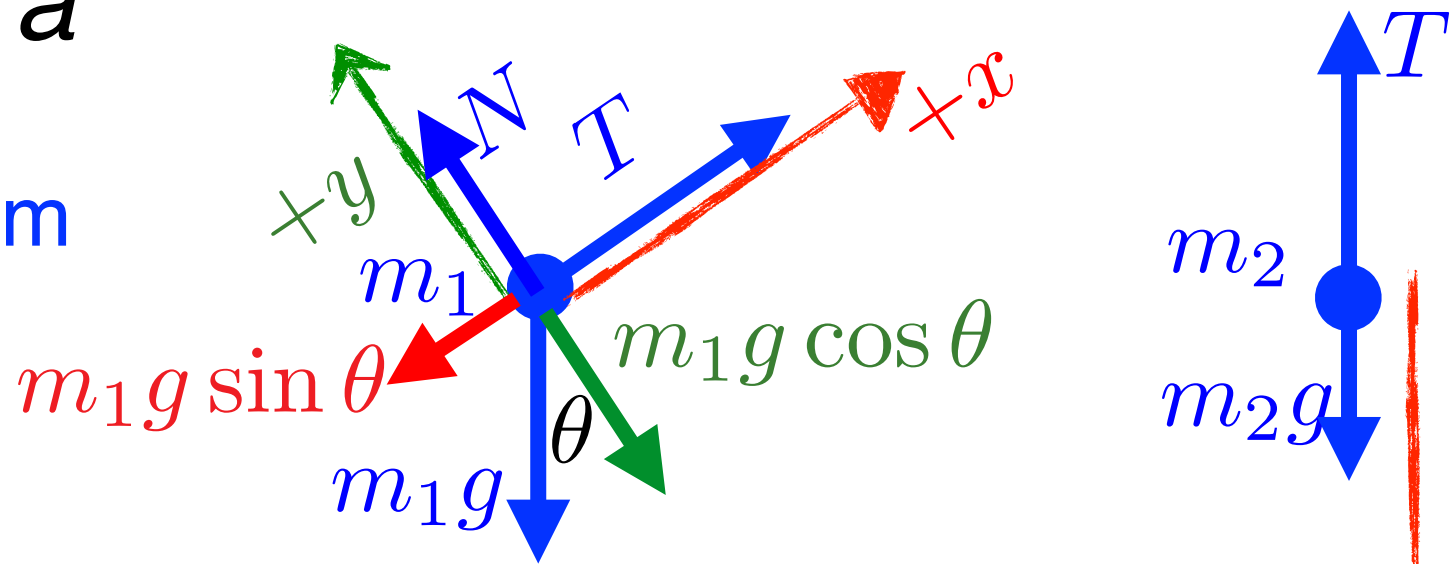
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4a. For each body, draw a free-body diagram

4b. Apply Newton's 2nd law

*Note: if const. force, constant acceleration kinematic equations also apply*

5. Calculate



$$N - m_1 g \cos \theta = m_1 a_y = 0 \quad \uparrow$$

$$N = m_1 g \cos \theta$$

$$T - m_1 g \sin \theta = m_1 a_x = m_1 a$$

$$m_2 g - T = m_2 a_x = m_2 a$$



# Ex. 4.6

Given:  $m_1, m_2, \theta$

Goal:  $a$

1. Read carefully
2. Draw a sketch = space diagram
3. Given? Goal?
4. Brainstorm: 2nd law problem

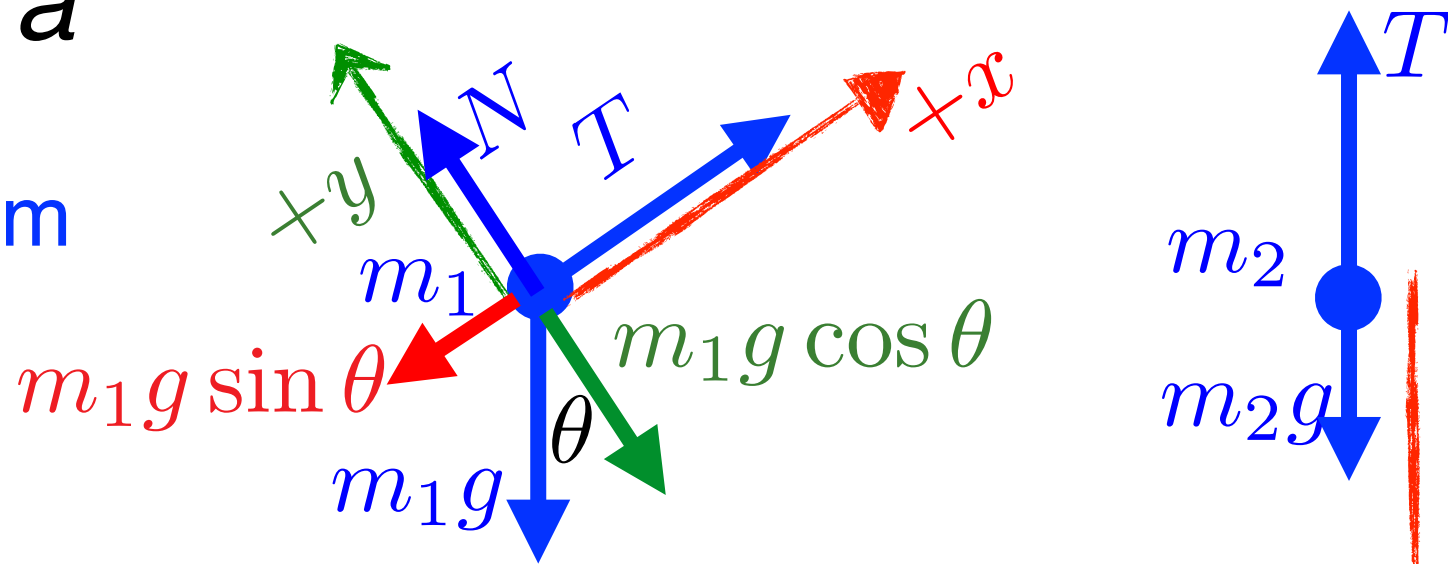
4a. For each body, draw a free-body diagram

4b. Apply Newton's 2nd law

*Note: if const. force, constant acceleration kinematic equations also apply*

5. Calculate

$$T = m_1(a + g \sin \theta)$$



$$N - m_1 g \cos \theta = m_1 a_y = 0$$

$$N = m_1 g \cos \theta$$

$$T - m_1 g \sin \theta = m_1 a_x = m_1 a$$

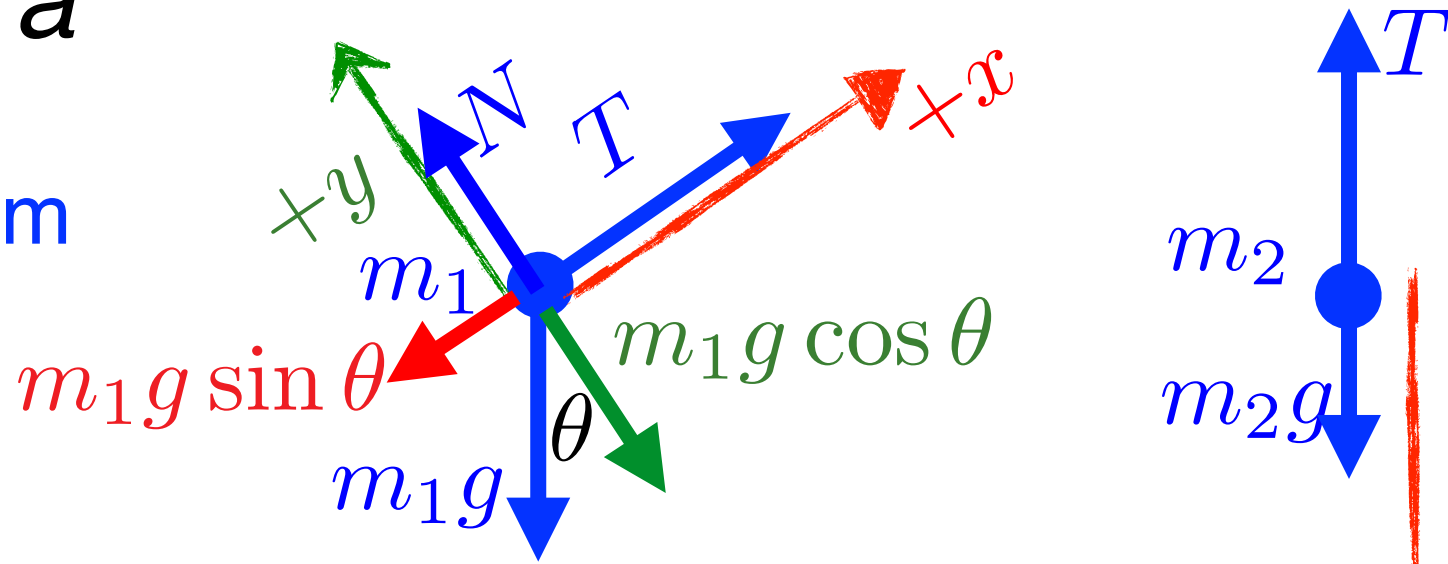
$$m_2 g - T = m_2 a_x = m_2 a$$

# Ex. 4.6

Given:  $m_1, m_2, \theta$   
Goal:  $a$

1. Read carefully
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4. Brainstorm: 2nd law problem
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*Note: if const. force, constant acceleration kinematic equations also apply*
5. Calculate



$$N - m_1 g \cos \theta = m_1 a_y = 0$$

$$N = m_1 g \cos \theta$$

$$T - m_1 g \sin \theta = m_1 a_x = m_1 a$$

$$m_2 g - T = m_2 a_x = m_2 a$$

$$T = m_1 (a + g \sin \theta) \quad T = m_2 (g - a)$$

# Ex. 4.6

Given:  $m_1, m_2, \theta$

Goal:  $a$

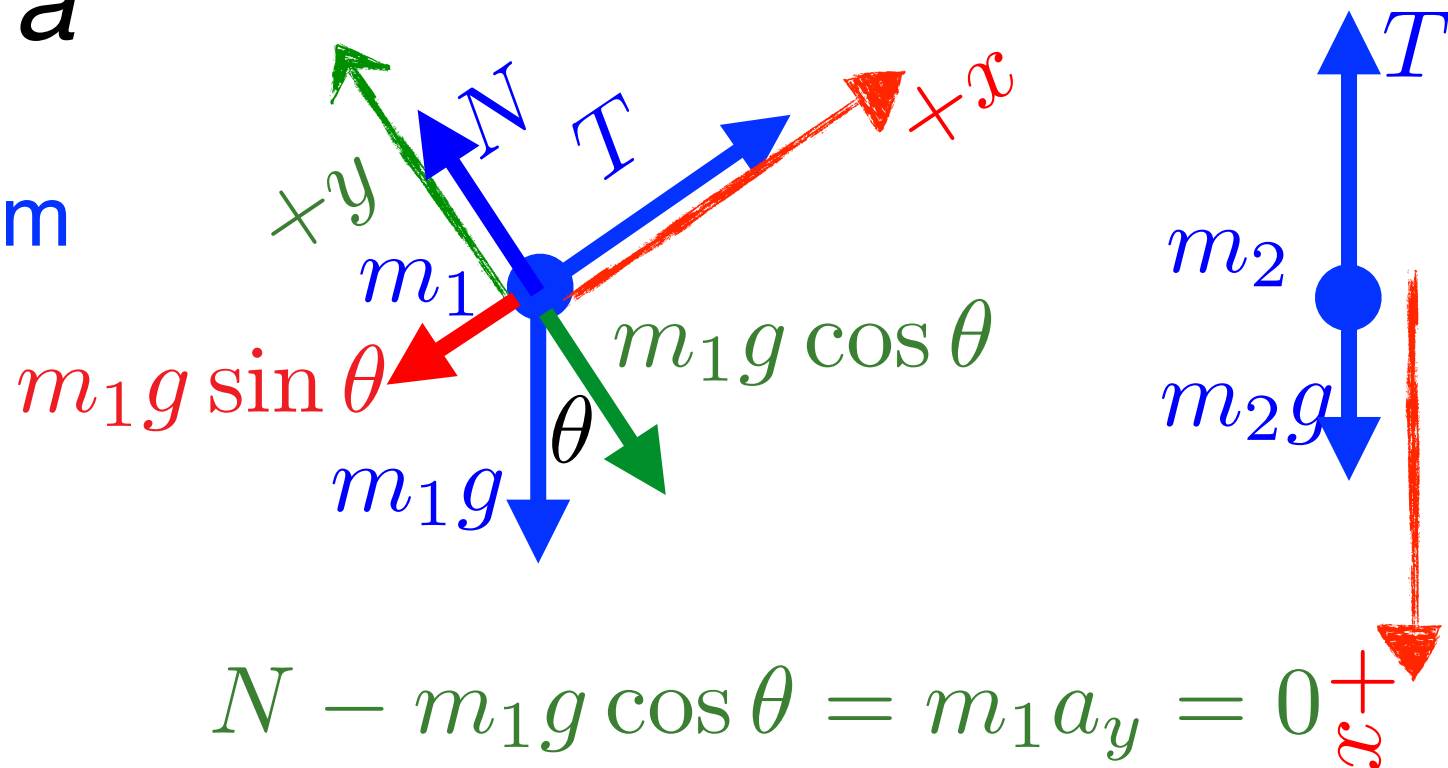
1. Read carefully
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4. Brainstorm: 2nd law problem

4a. For each body, draw a free-body diagram

4b. Apply Newton's 2nd law

*Note: if const. force, constant acceleration kinematic equations also apply*

5. Calculate



$$N - m_1 g \cos \theta = m_1 a_y = 0$$

$$N = m_1 g \cos \theta$$

$$T - m_1 g \sin \theta = m_1 a_x = m_1 a$$

$$m_2 g - T = m_2 a_x = m_2 a$$

$$T = m_1 (a + g \sin \theta) \quad T = m_2 (g - a)$$

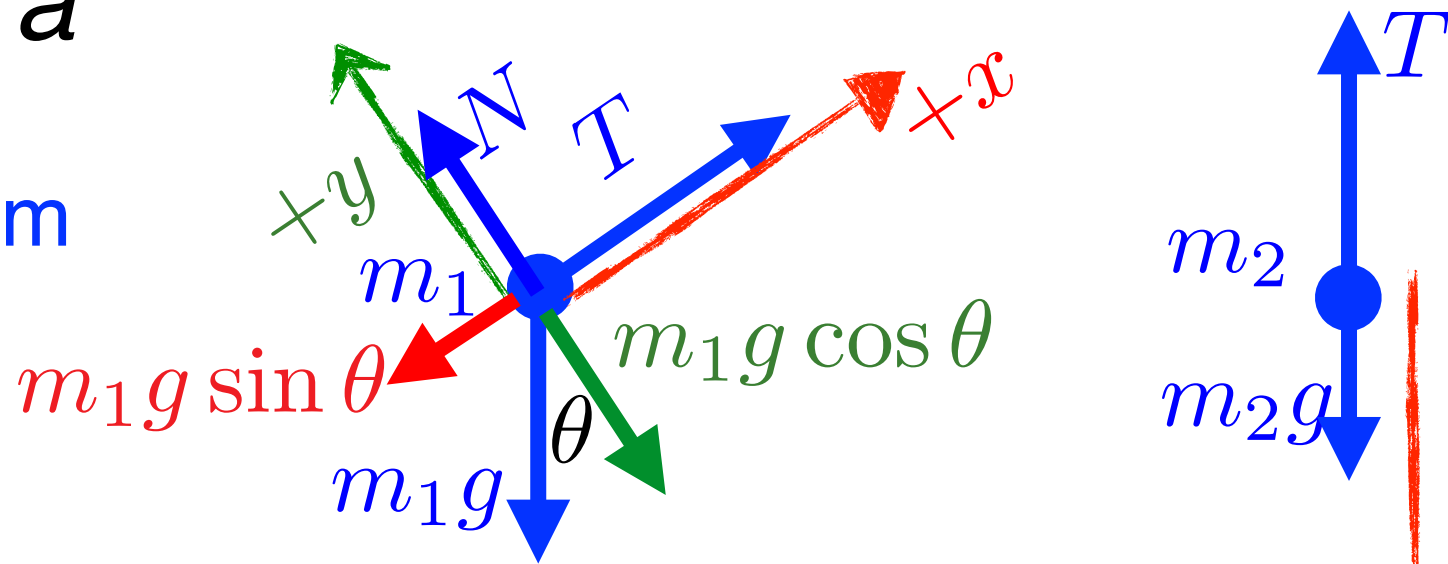
$$m_1 a + m_1 g \sin \theta = m_2 g - m_2 a$$

# Ex. 4.6

Given:  $m_1, m_2, \theta$   
Goal:  $a$

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*Note: if const. force, constant acceleration kinematic equations also apply*
5. Calculate



$$N - m_1 g \cos \theta = m_1 a_y = 0$$

$$N = m_1 g \cos \theta$$

$$T - m_1 g \sin \theta = m_1 a_x = m_1 a$$

$$m_2 g - T = m_2 a_x = m_2 a$$

$$T = m_1 (a + g \sin \theta) \quad T = m_2 (g - a)$$

$$m_1 a + m_1 g \sin \theta = m_2 g - m_2 a$$

$$(m_1 + m_2) a = g (m_2 - m_1 \sin \theta)$$

# Ex. 4.6

Given:  $m_1, m_2, \theta$   
Goal:  $a$

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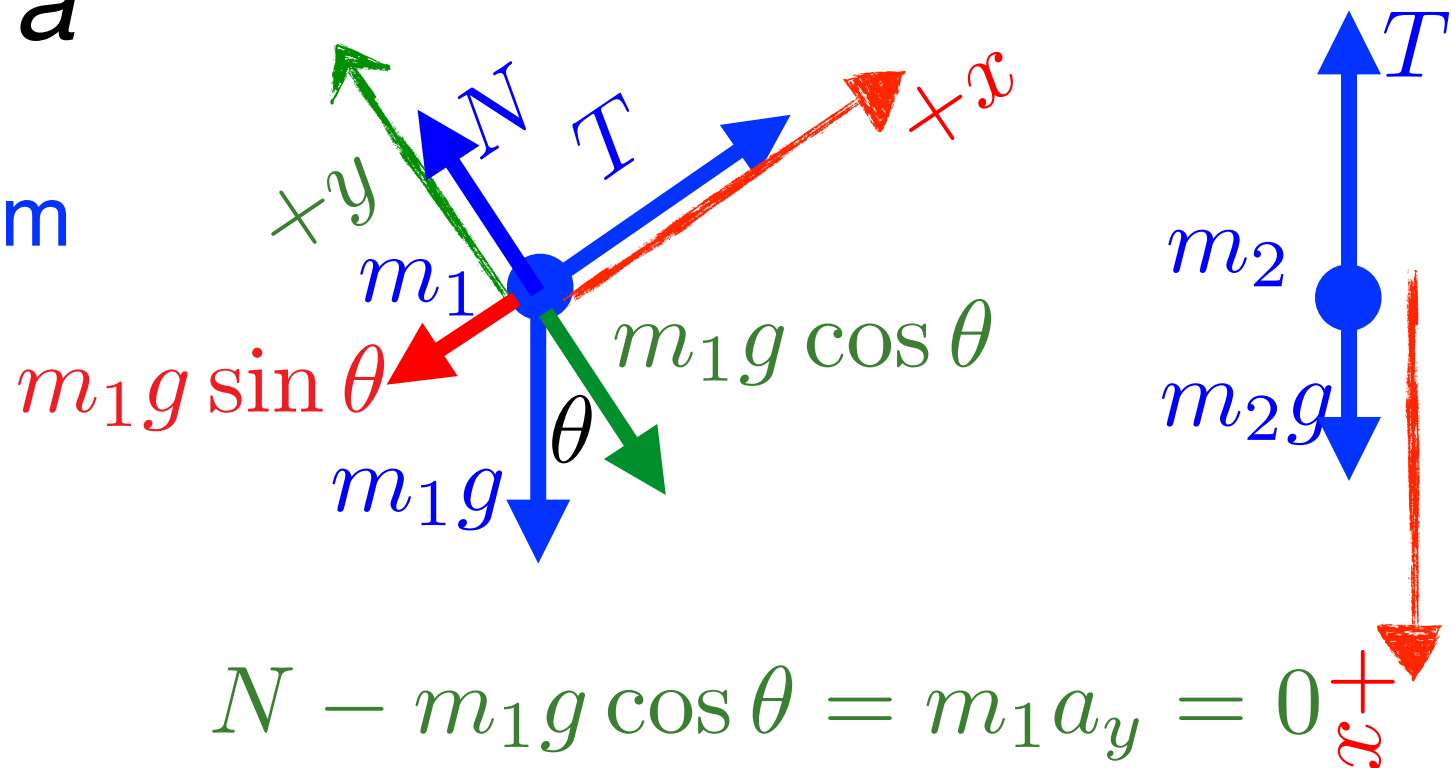
*Note: if const. force, constant acceleration kinematic equations also apply*

5. Calculate

$$T = m_1(a + g \sin \theta) \quad T = m_2(g - a)$$

$$m_1 a + m_1 g \sin \theta = m_2 g - m_2 a$$

$$(m_1 + m_2)a = g(m_2 - m_1 \sin \theta)$$



$$N - m_1 g \cos \theta = m_1 a_y = 0$$

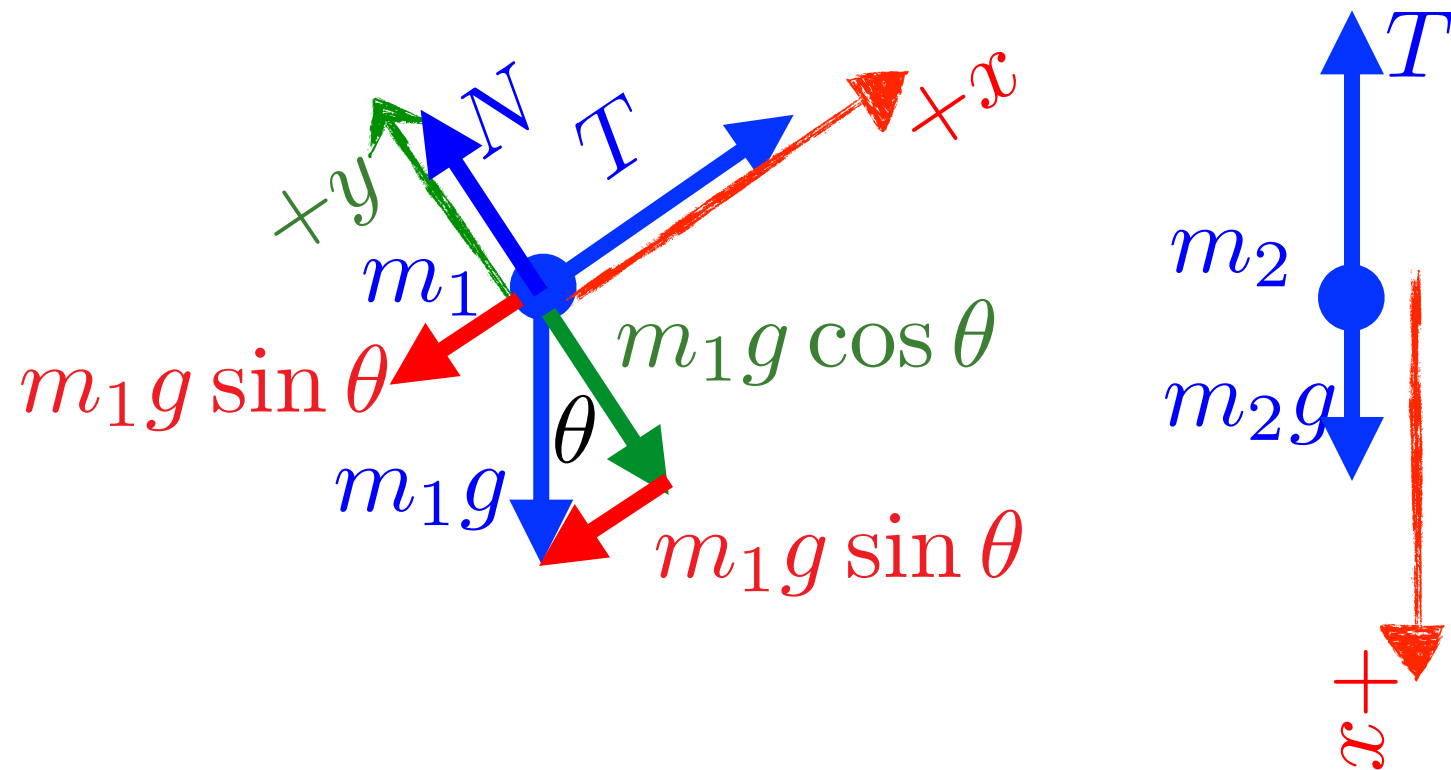
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$$m_2 g - T = m_2 a_x = m_2 a$$

$$a = g \frac{m_2 - m_1 \sin \theta}{m_1 + m_2}$$

# Ex. 4.6

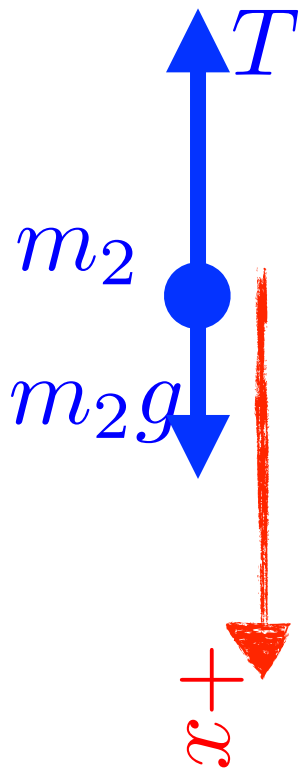
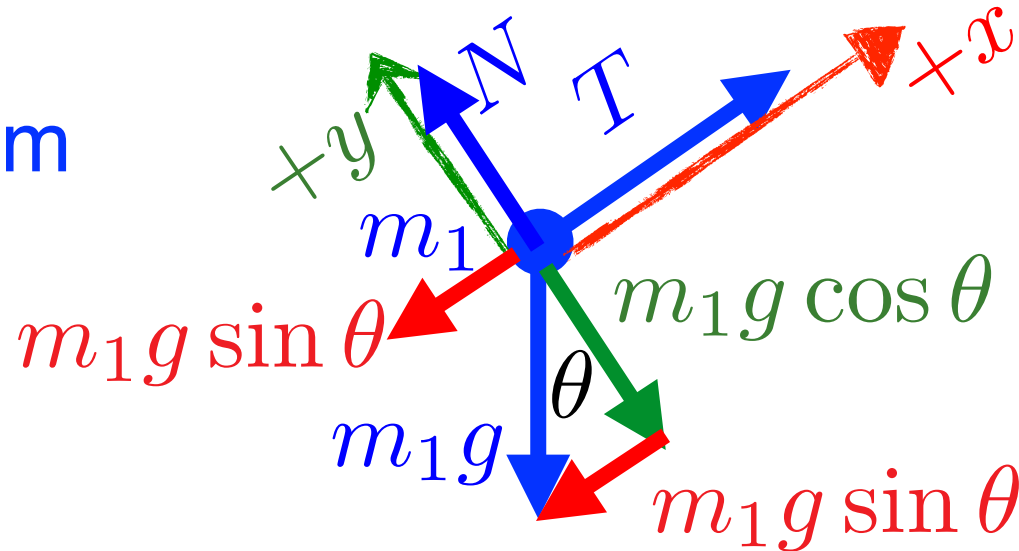


$$a = g \frac{m_2 - m_1 \sin \theta}{m_1 + m_2}$$

# Ex. 4.6

Given:  $m_1, m_2, \theta$   
Goal:  $a$

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  - 4a. For each body, draw a free-body diagram
  - 4b. Apply Newton's 2nd law
5. Calculate
6. Plug in numbers

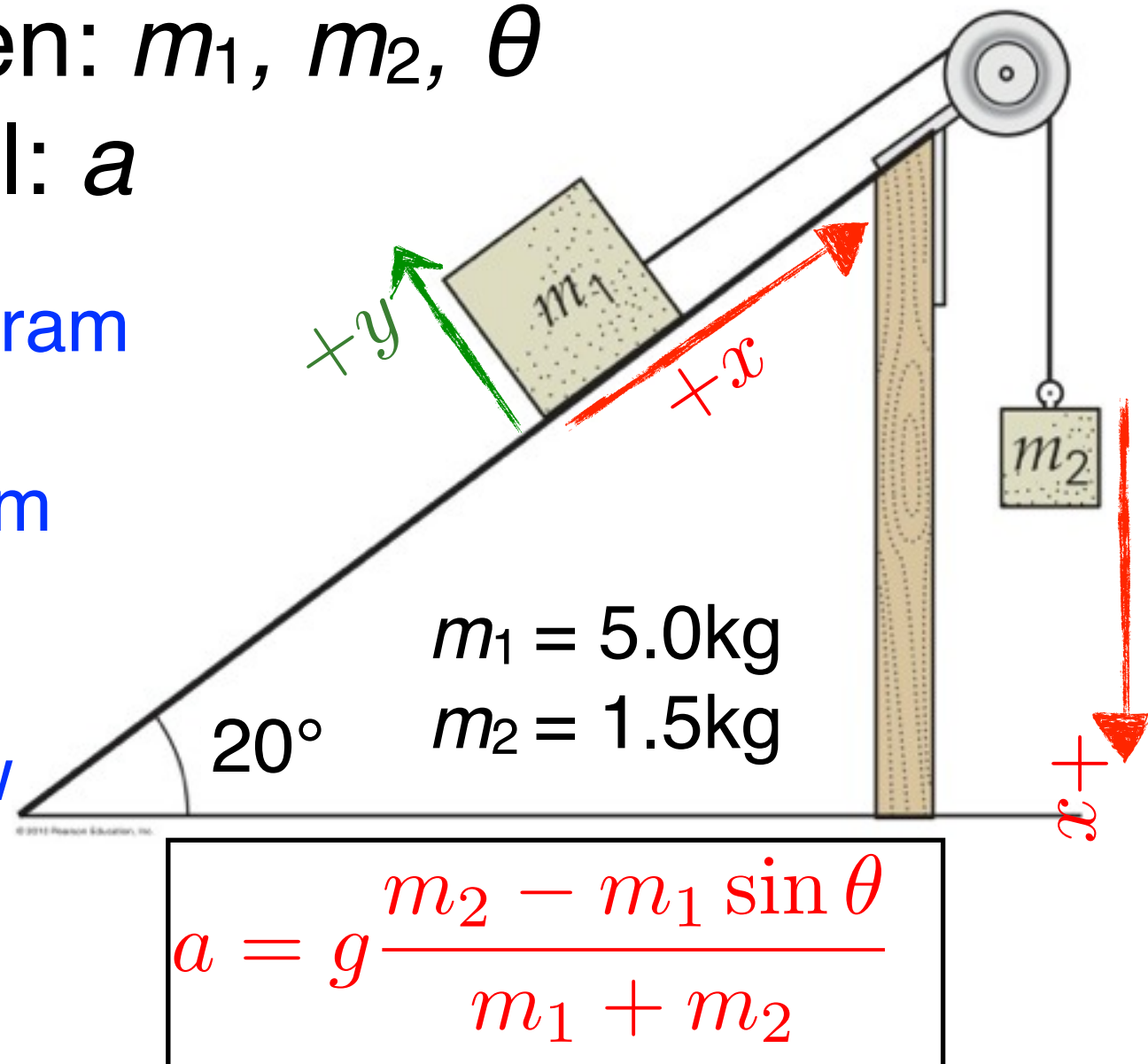


$$a = g \frac{m_2 - m_1 \sin \theta}{m_1 + m_2}$$

# Ex. 4.6

Given:  $m_1, m_2, \theta$   
Goal:  $a$

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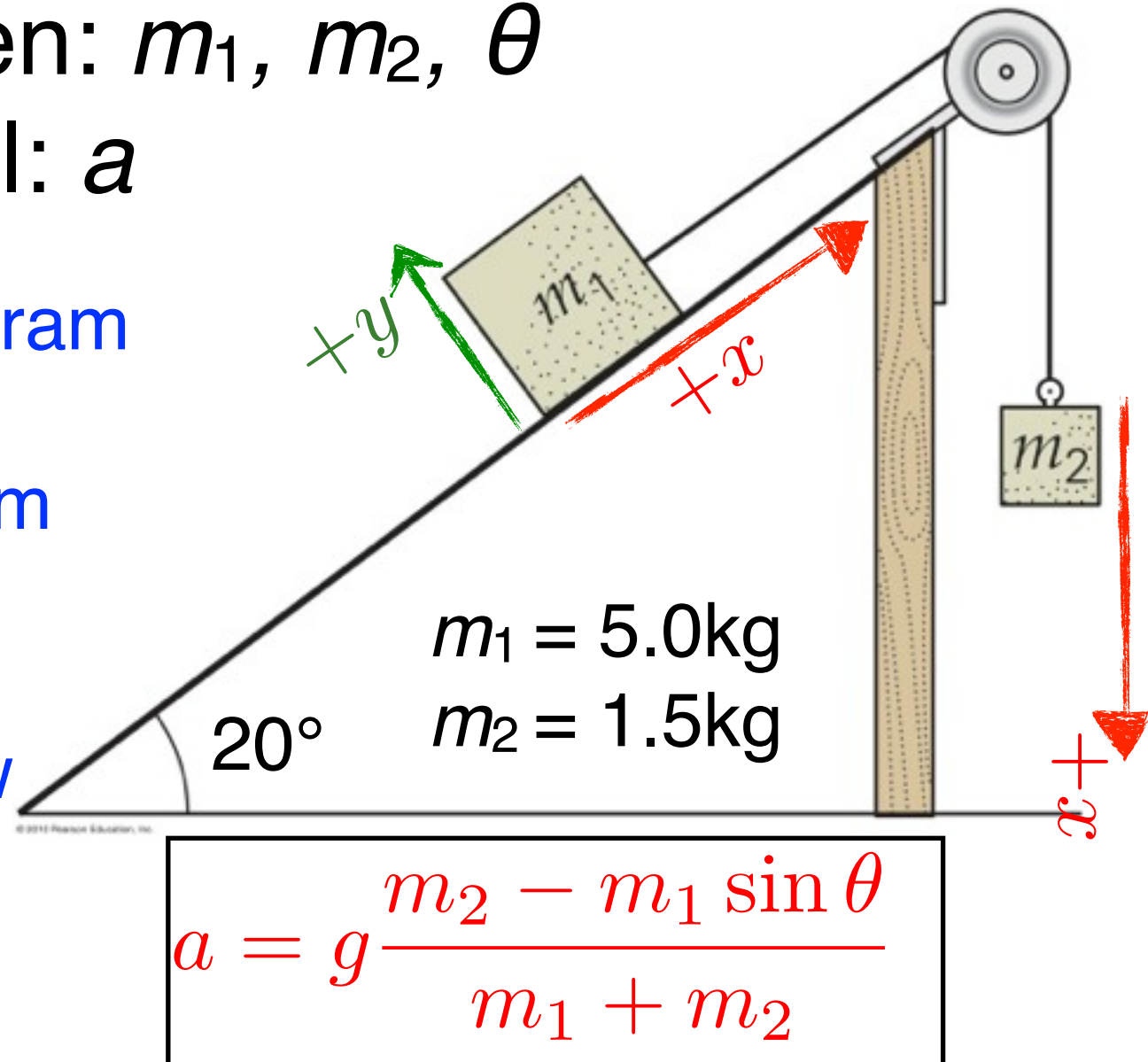




# Ex. 4.6

Given:  $m_1, m_2, \theta$   
Goal:  $a$

1. Read carefully
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  - 4a. For each body, draw a free-body diagram
  - 4b. Apply Newton's 2nd law
5. Calculate
6. Plug in numbers

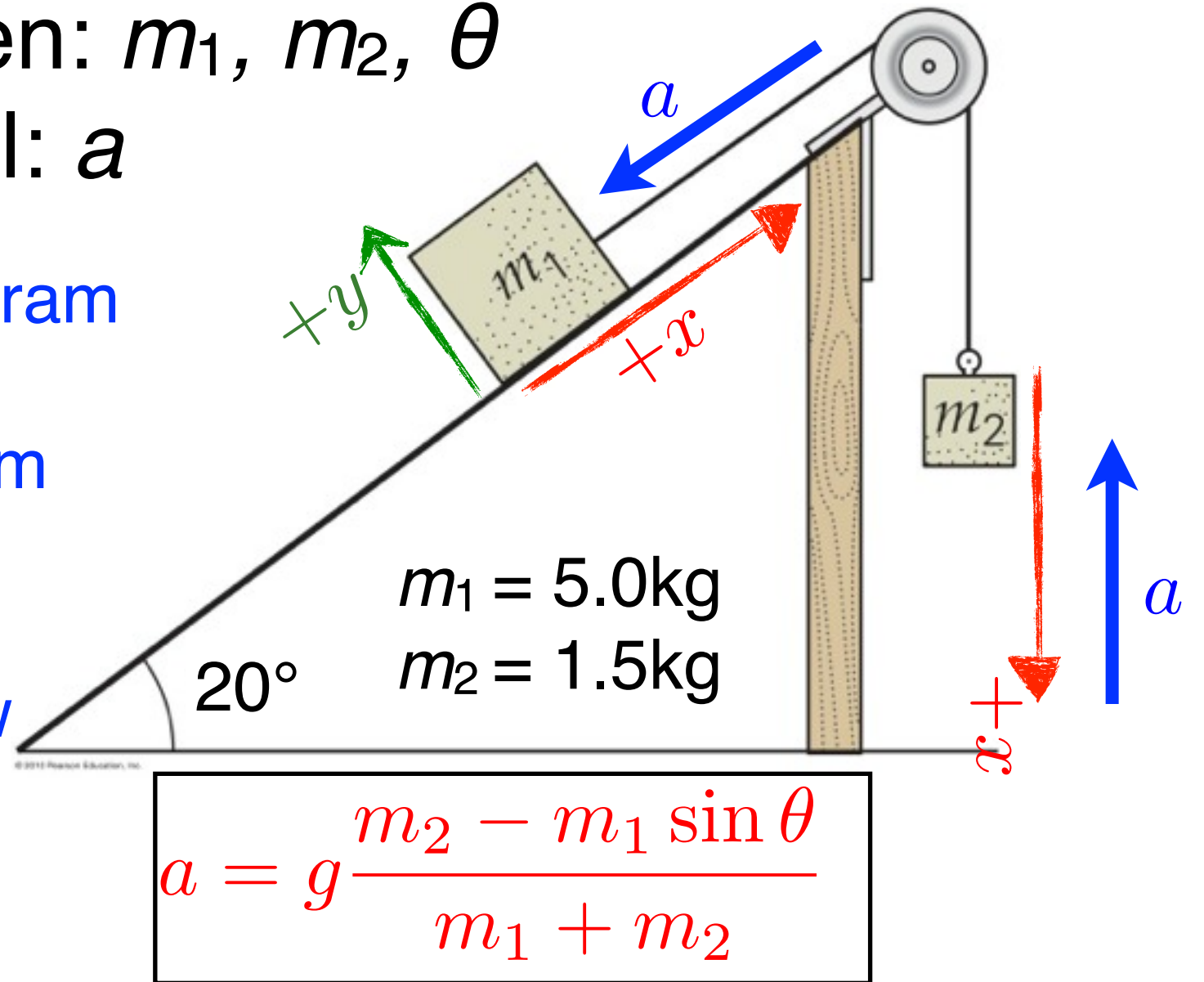


$$a = (9.8 \text{ m/s}^2) \frac{1.5 \text{ kg} - (5 \text{ kg}) \sin(20^\circ)}{1.5 \text{ kg} + 5 \text{ kg}} = -0.32 \text{ m/s}^2$$

# Ex. 4.6

Given:  $m_1, m_2, \theta$   
Goal:  $a$

1. Read carefully
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5. Calculate
6. Plug in numbers

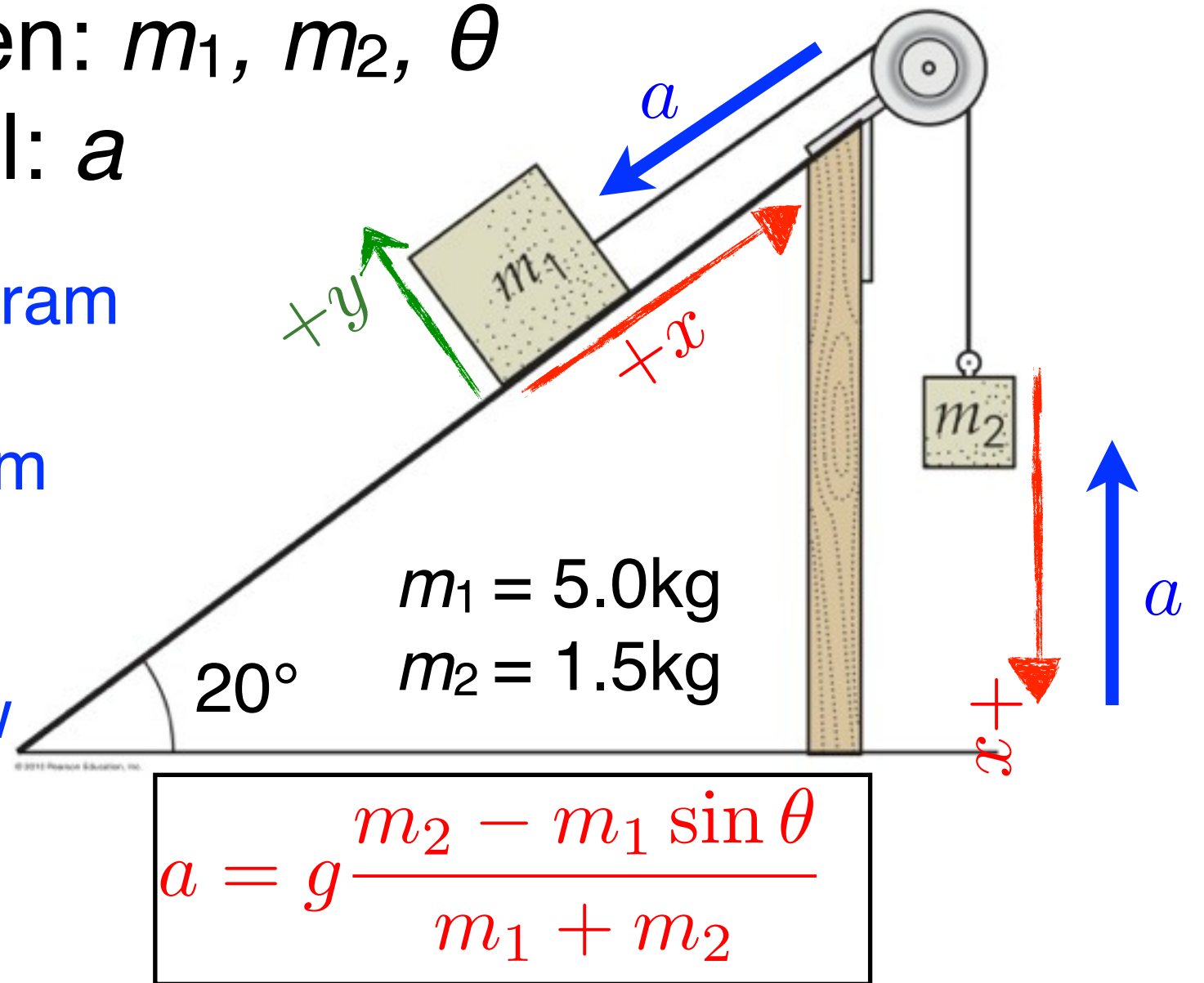


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# Ex. 4.6

Given:  $m_1, m_2, \theta$   
Goal:  $a$

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3. Given? Goal?
4. Brainstorm: 2nd law problem
  - 4a. For each body, draw a free-body diagram
  - 4b. Apply Newton's 2nd law
5. Calculate
6. Plug in numbers
7. Is answer reasonable?



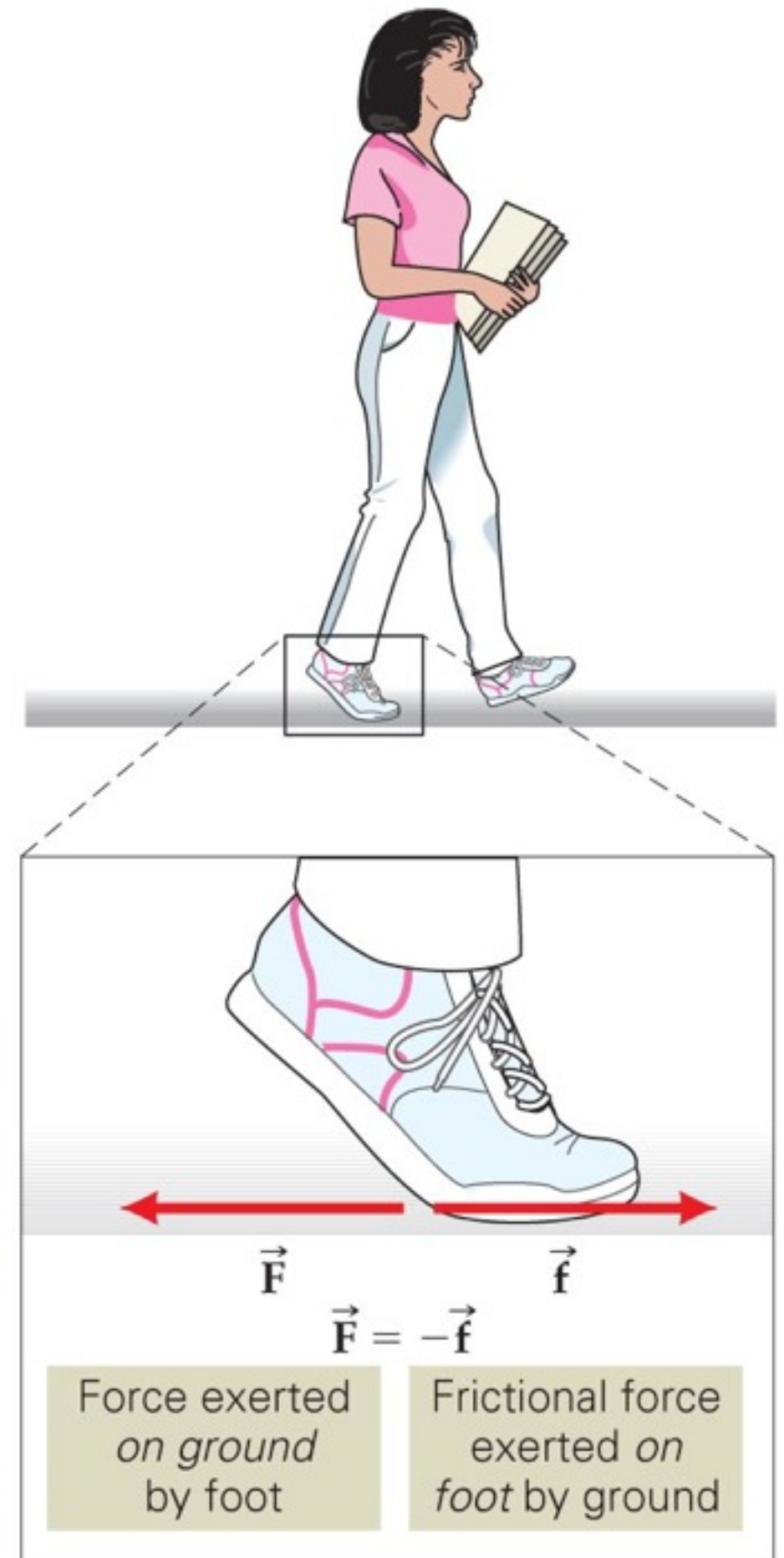
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# Lecture 11 outline

- Announcements
- Quantitative force examples
  - Free-body diagrams
  - Example: Atwood machine & ramp
- Friction & air resistance
  - How friction works
  - Example: friction
- Class participation

# Friction

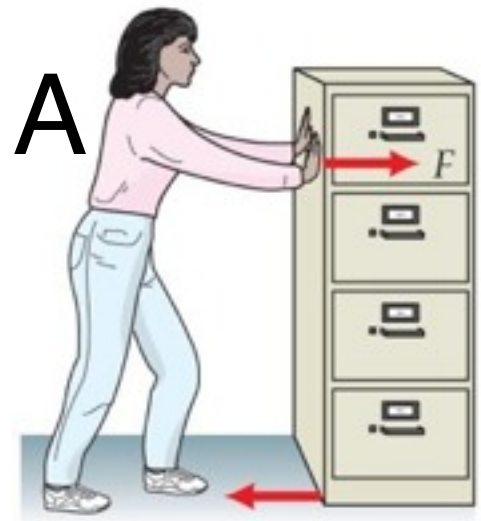
- Friction = force resisting motion when 2 materials are in contact
- Friction between solid surfaces
  - Origin: surfaces are rough (microscopically)
  - “High spots” on the surface temporarily bond



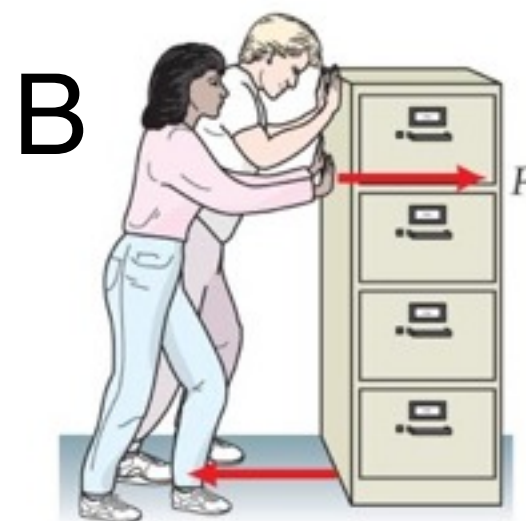


# Types of friction

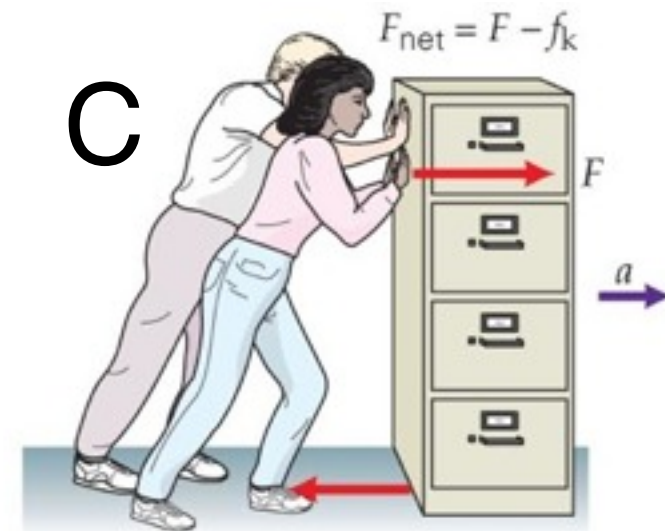
- Static: no relative motion of the surfaces
- Kinetic (“sliding”): surfaces slide



$$f_s < \mu_s N$$

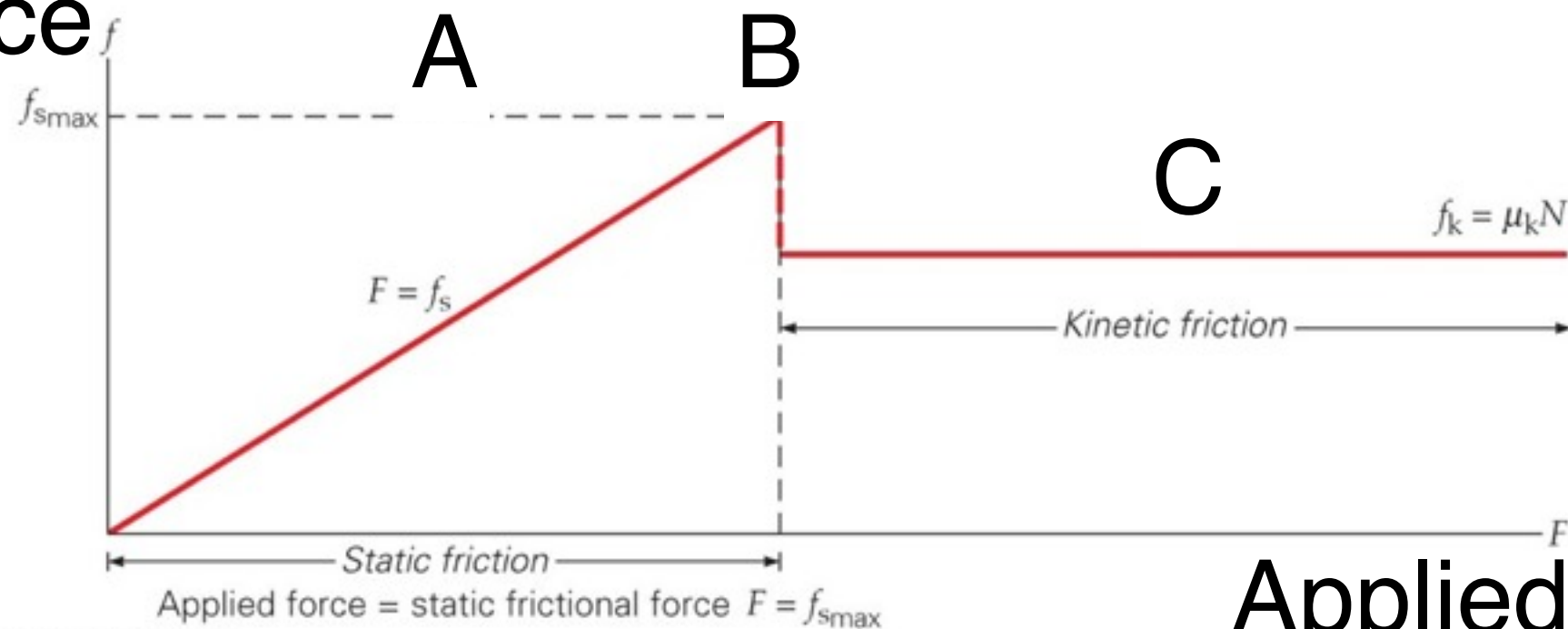


$$f_{s\max} = \mu_s N$$



$$f_k = \mu_k N$$

Friction force



Applied force

# Clicker question #42

## Question 4.19 Friction

A box sits in a pickup truck on a frictionless truck bed. When the truck accelerates forward, the box slides off the back of the truck because:

- ☒ A the force from the rushing air pushed it off
- ☐ B the force of friction pushed it off
- ☐ C no net force acted on the box
- ☐ D truck went into reverse by accident
- ☐ none of the above

# Clicker question #43

## Question 4.22 Will It Budge?

A box of **weight 100 N** is at rest on a floor where  $\mu_s = 0.4$ . A rope is attached to the box and pulled horizontally with tension  $T = 30 \text{ N}$ . Which way does the box move?

A

moves to the left

B

moves to the right

C

moves up

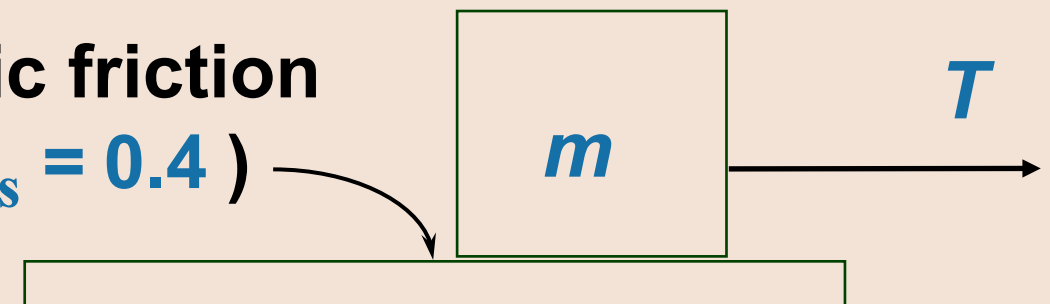
D

moves down

the box does not move

Static friction

( $\mu_s = 0.4$ )





# Clicker question #45

## Question 4.21 Going Sledding

Your little sister wants you to give her a ride on her sled. On level ground, what is the easiest way to accomplish this?

A

pushing her from behind [1]

B

pulling her from the front [2]

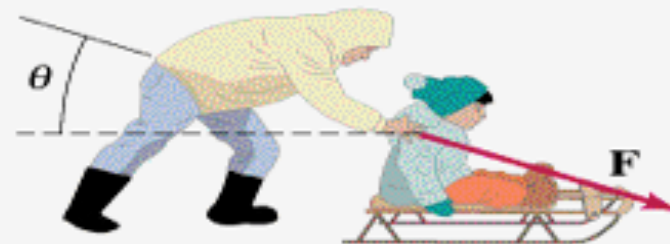
C

both [1] and [2] are equivalent

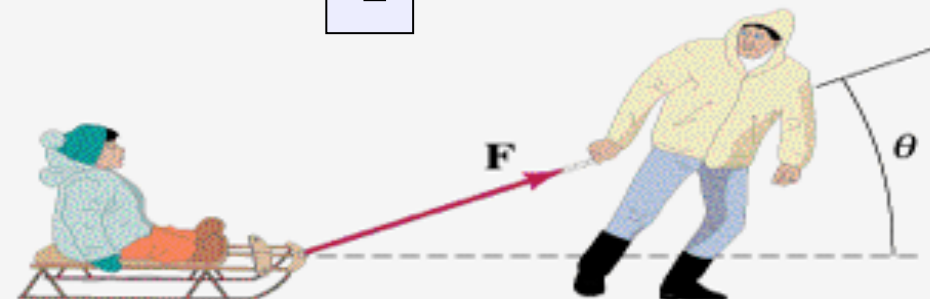
D

it is impossible to move the sled

tell her to get out and walk



1



2

# Class participation #10

- 0. Name
- 1. Draw a free-body diagram for example from the textbook:
  - A car is sliding through a puddle. Superman arrives at the last moment and tries to stop the car.
  - Hint: list **all** of the forces acting on the car. Then draw the diagram.



