Physics 211

Sections 1 & 70 Dr. Geoffrey Lovelace Fall 2012 Lecture 12 (10/04/12)

Lecture 12 outline

- Announcements
- Homework followup
- Class participation tutorial: second law

Announcements

- Homework
 - Homework #6: due Thursday 11:59PM
- Reading: for Thursday: through Sec. 5.5
- Office hours
 - 4PM-5PM today in MH-601B

Today

Sep 25	Exam 1
Sep 27	Laws of motion, HW #4 due
Oct 2	Free body diagrams
Oct 4	Free body diagrams, friction, HW #5 due
Oct 9	Work, introduction to energy
Oct 11	Energy, kinetic & potential energy, conservation of energy, HW #6 due
Oct 16	Conservation of energy
Oct 18	Linear momentum, conservation of linear momentum, HW #7 due
Oct 23	Exam 2
Oct 25	Conservation of momentum, collisions, HW #8 due
Oct 30	Collisions, center of mass, rockets
Nov 1	Circular motion, gravitation, HW #9 due
Nov 6	Gravitation, Kepler's laws, intro to rigid body rotation
Nov 8	Rotation, torque, angular momentum
Nov 13	Conservation of angular momentum HW #10 due
Nov 15	Exam 3
Nov 20	Fall Recess — No class
Nov 22	Fall Recess — No class
Nov 27	Temperature, gas laws
Nov 29	Phase changes, heat transfer, HW #11 due
Dec 4	Laws of thermodynamics, entropy
Dec 6	Harmonic motion, HW #12 due
Dec 11	Harmonic motion & waves
Dec 13	Gravitational waves, harmonic motion, black holes, HW #13 due
Dec 20	Final exam 9:30AM-11:20AM

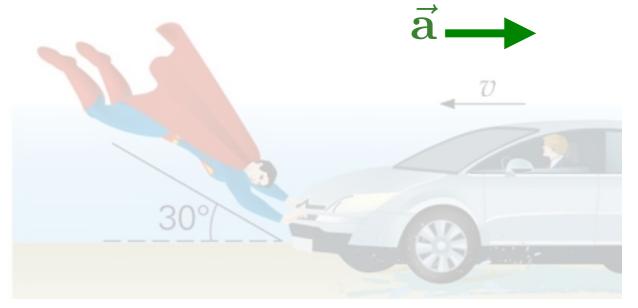
Lecture 12 outline

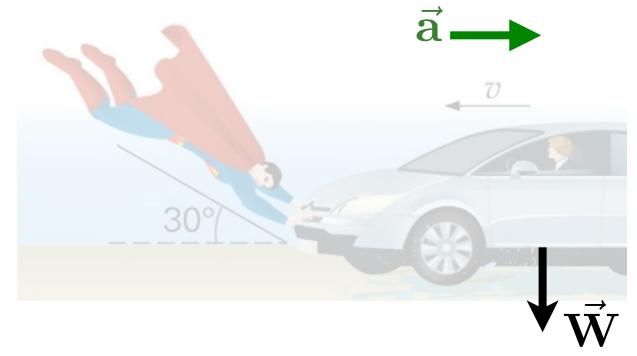
- Announcements
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- Class participation tutorial: second law

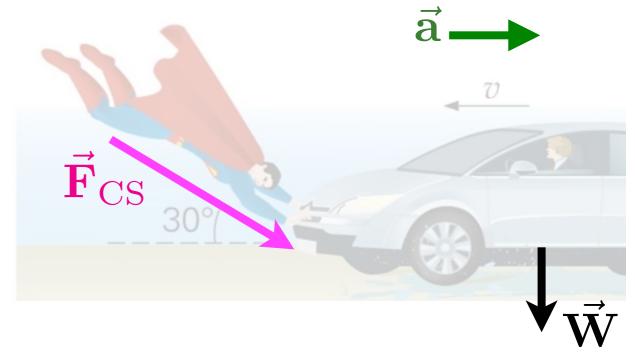
- 0. Name
- 1. Draw a free-body diagram for example from the textbook:
 - A car is sliding through a puddle. Superman arrives at the last moment and tries to stop the car. (Neglect friction.)
 - Hint: list all of the forces acting on the car. Then draw the diagram.

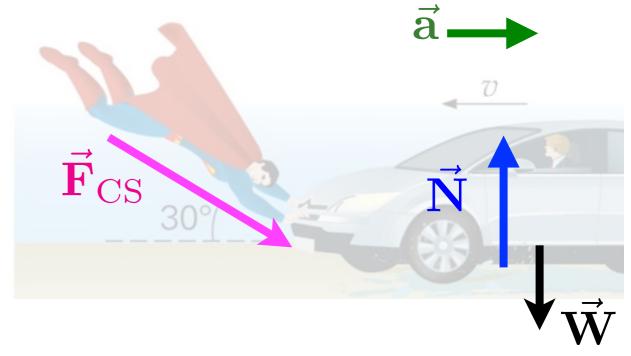


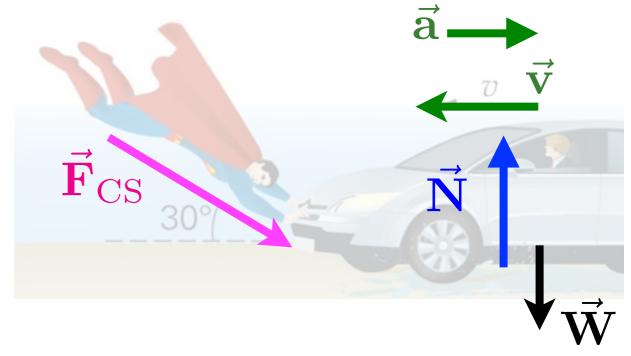




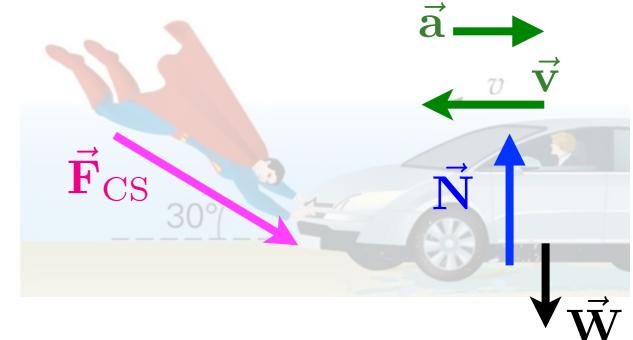




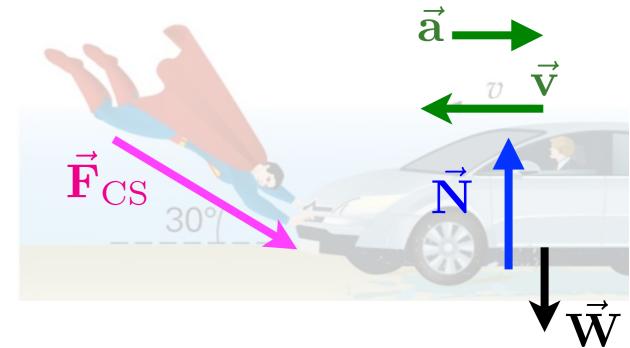




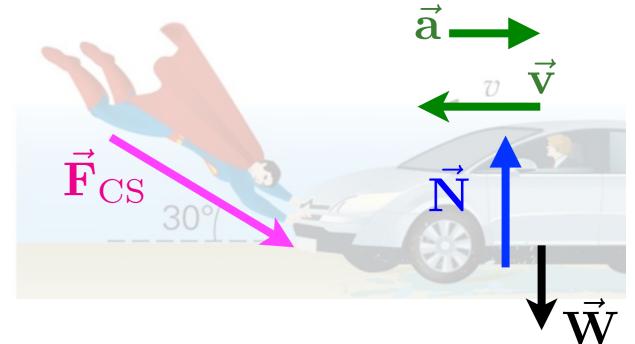
- 1. Draw axes
 - Origin where force applied
 - Direction: choose 1 axis to point in direction of motion



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 - Origin where force applied
 - Direction: choose 1 axis to point in direction of motion

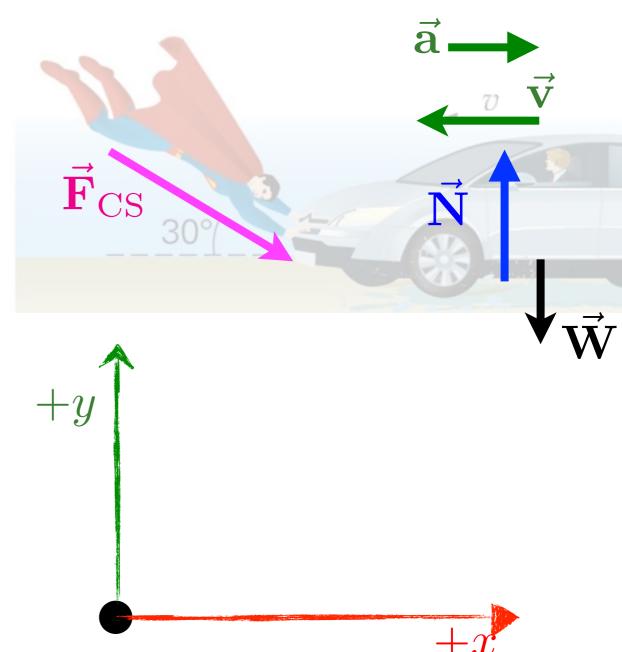


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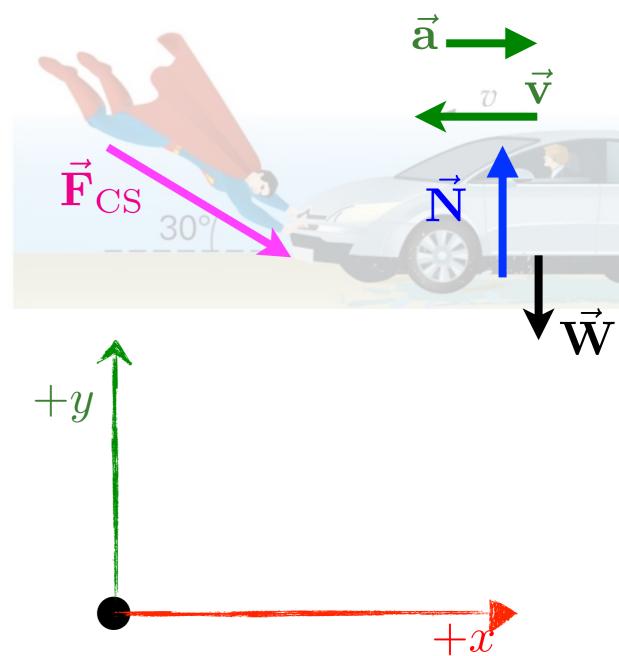




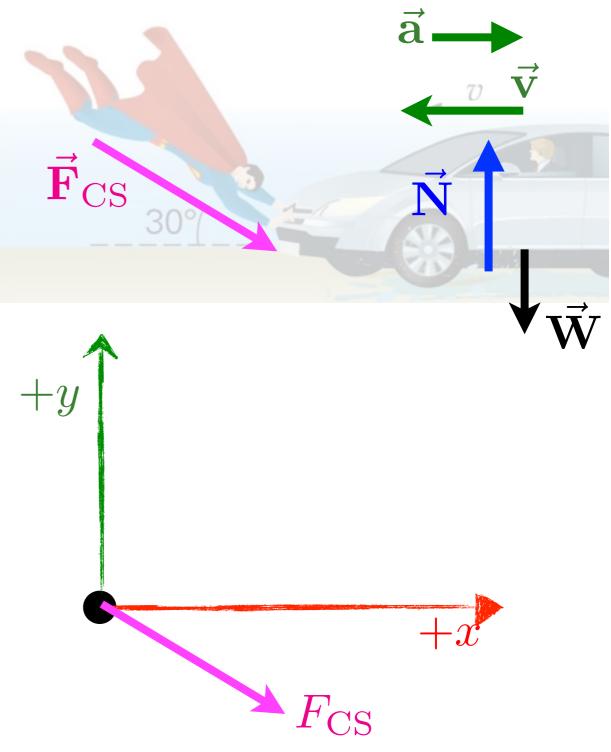
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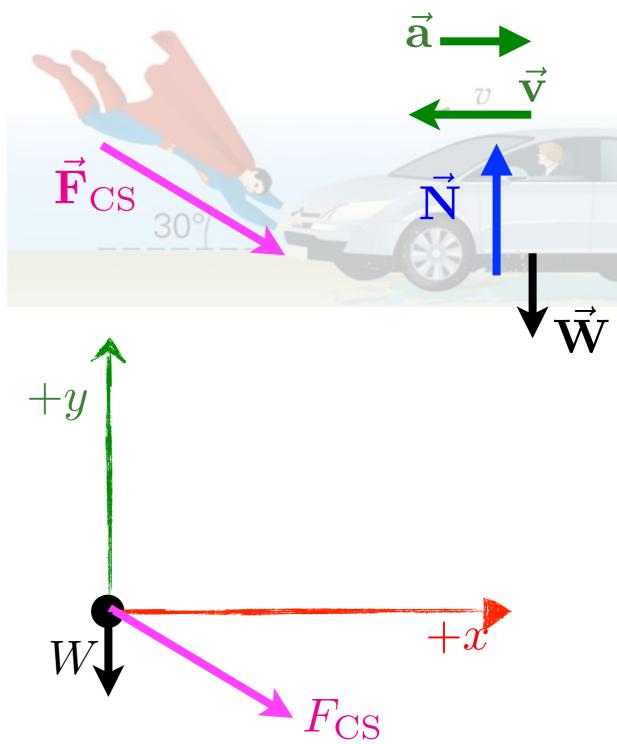
- 1. Draw axes
 - Origin where force applied
 - Direction: choose 1 axis to point in direction of motion
- 2. Draw all forces on object
 - Place tail of all forces at origin



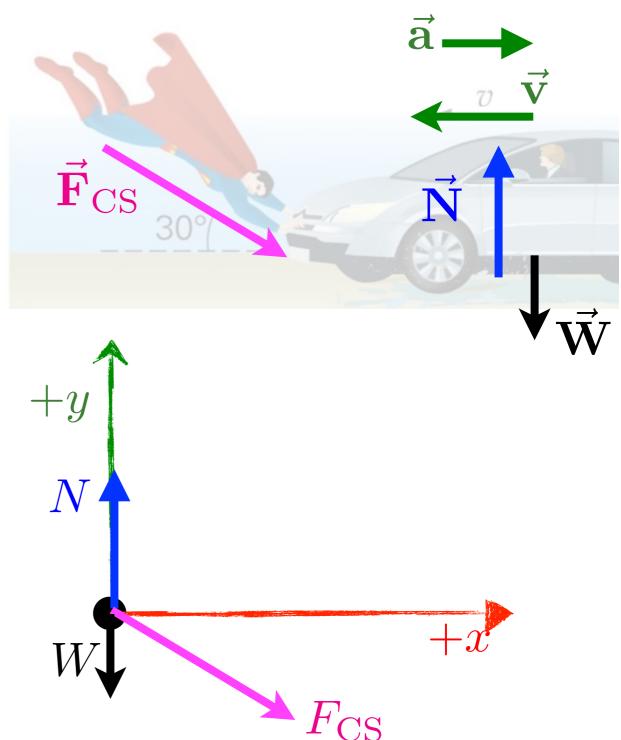
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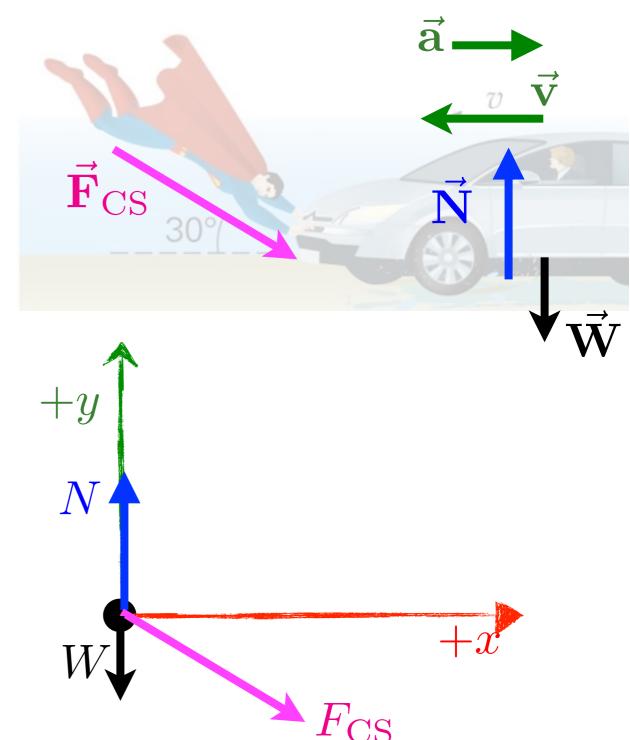
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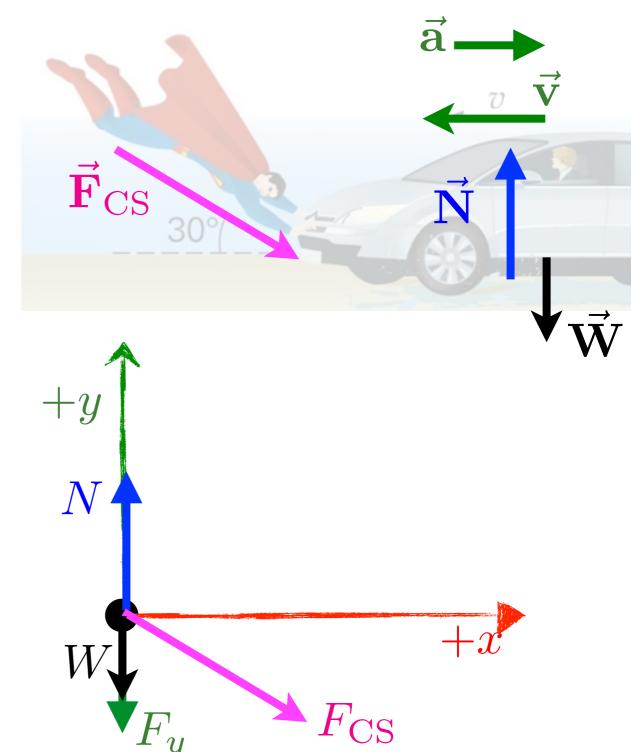
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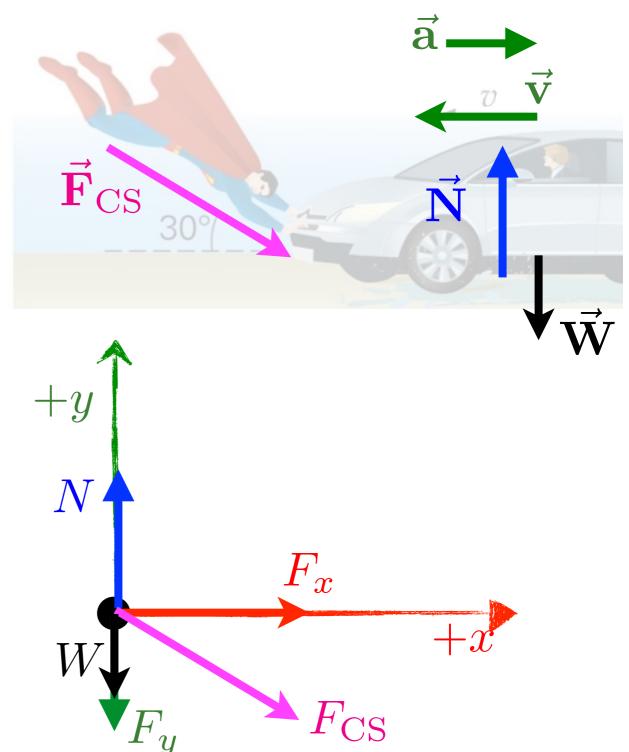
- 1. Draw axes
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- 2. Draw all forces on object
 - Place tail of all forces at origin
- 3. Resolve components
 - Use colors or draw



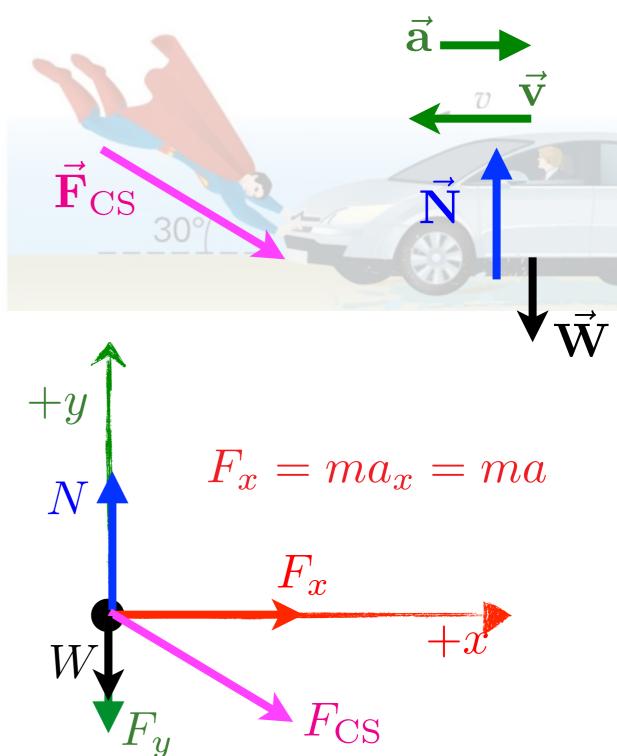
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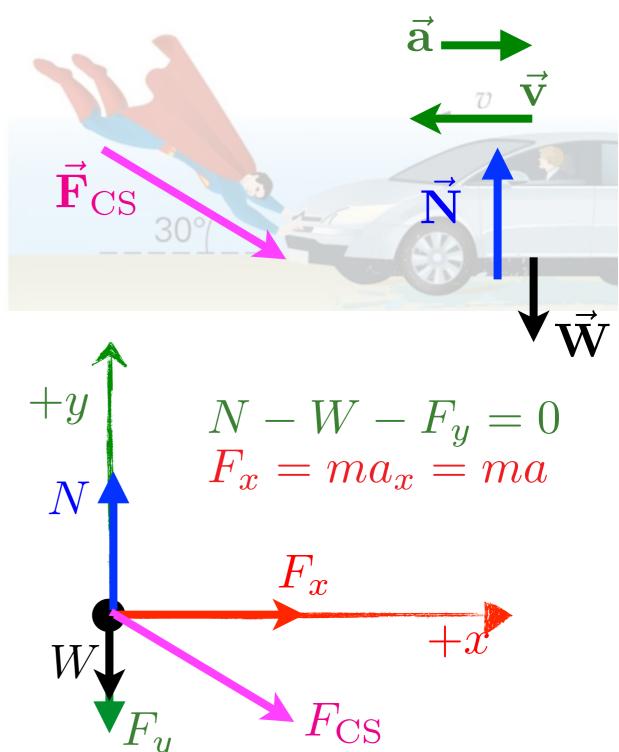
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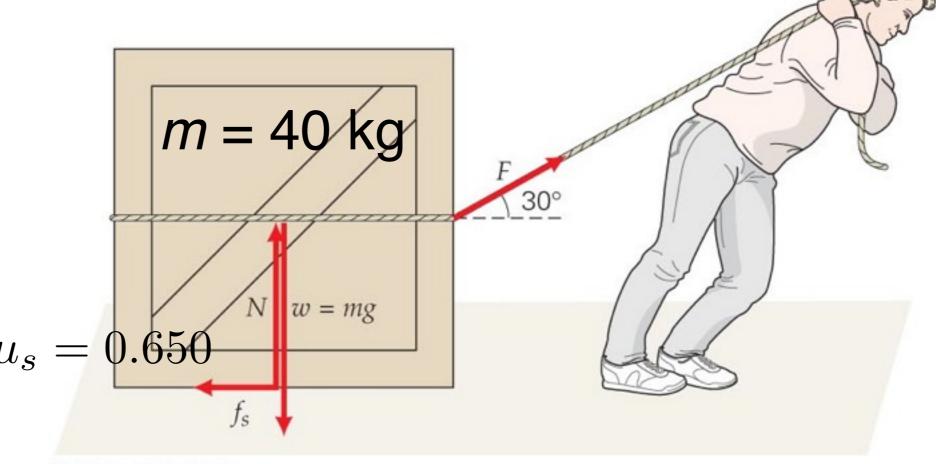
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Tutorial

Formula sheet:

$$\vec{\mathbf{a}} = \vec{\mathbf{F}}_{\mathrm{net}}/m$$
 $f_s^{\mathrm{max}} = \mu_s N$



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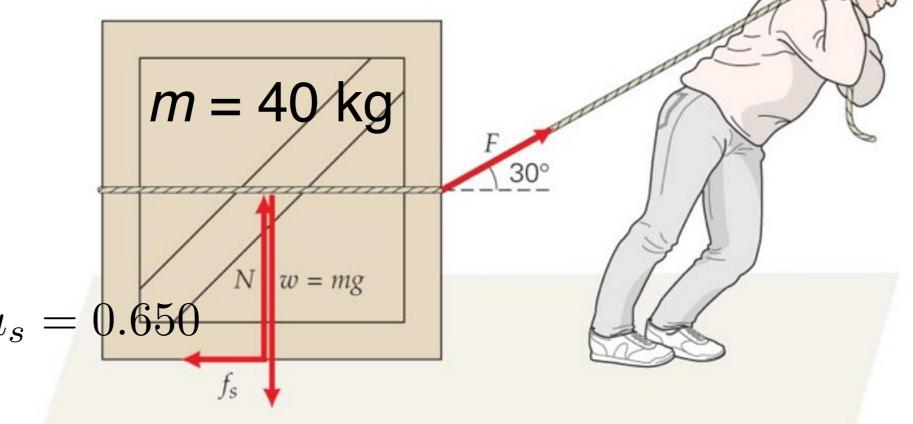
Minimum force so crate moves?

Tutorial

• (After class, see also Ex. 4.11 in textbook)

Formula sheet:

$$\vec{\mathbf{a}} = \vec{\mathbf{F}}_{\text{net}}/m$$
$$f_s^{\text{max}} = \mu_s N$$



Minimum force so crate moves?

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- Announcements
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- Class participation tutorial: second law
- Work & energy
 - Constant force
 - Variable force example: spring

Homework #5 followup

- A. Multiple Choice Question 4.12
 - Kinematic equations = constant acceleration
 - Newton's second law $\vec{\mathbf{a}} = \vec{\mathbf{F}}_{\mathrm{net}}/m$
- So...

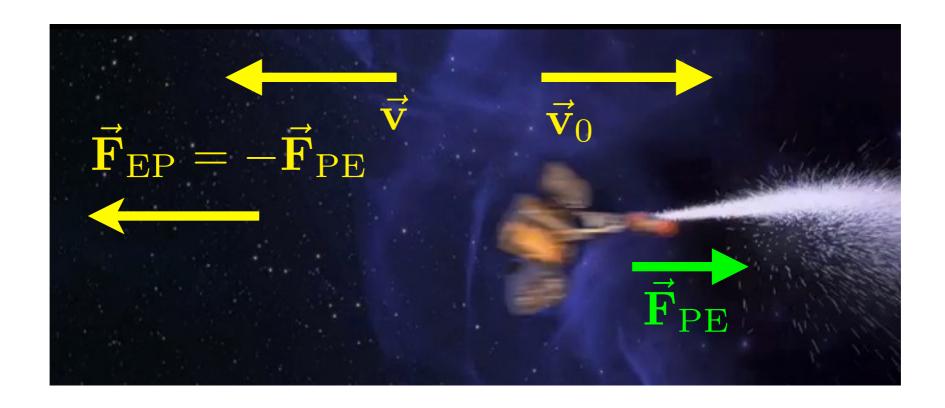
Clicker question #45

• The kinematic equation $x = x_0 + v_0 t + \frac{1}{2}at^2$ can be used...

- A Only with constant forces
- B With variable accelerations
- C Only with constant velocities
- A, B, and C

Homework #5 followup

- ullet If force $ec{\mathbf{F}}_{\mathrm{AB}}$ on A by B, then...
 - Force on B by A is $ec{\mathbf{F}}_{\mathrm{BA}} = -ec{\mathbf{F}}_{\mathrm{AB}}$
 - Relates forces acting on different objects
- So...



Clicker question #46

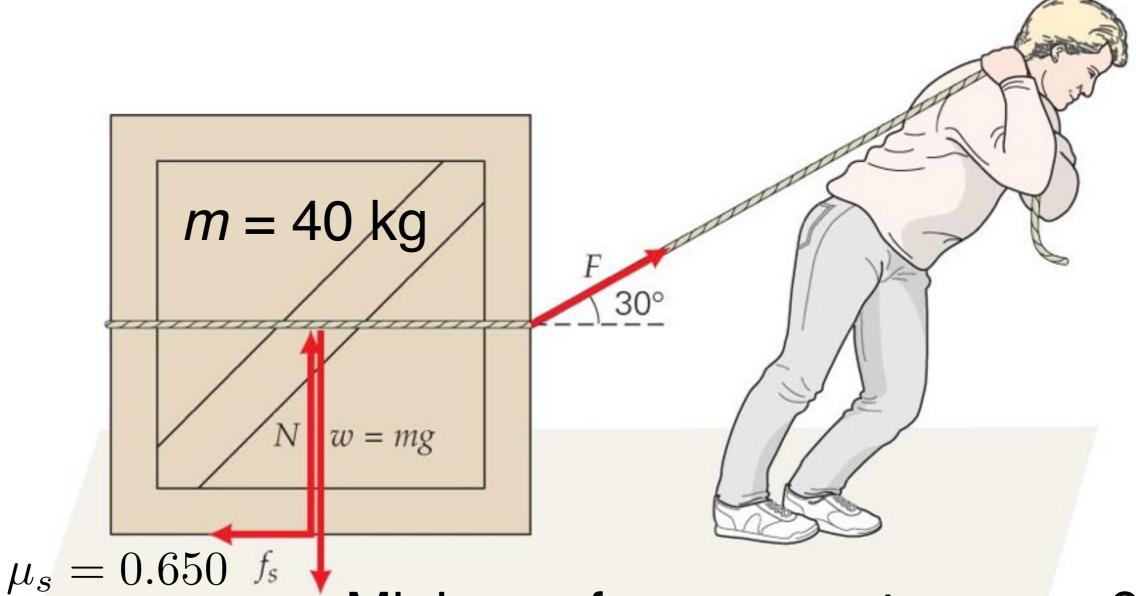
 \bullet Given force on Earth by Moon \vec{F}_{EM} , Newton's third law says the force on Moon by Earth \vec{F}_{ME}



- Greater in magnitude than, opposite in direction from
- B Greater in magnitude than, in the same direction as
- Equal in magnitude to, opposite in direction from
- Smaller in magnitude than, opposite in direction from
- Smaller in magnitude than, in the same direction as

Ex. 4.11

Given: $\theta = 30^{\circ}$, μ_s , m, gGoal: Min. F so crate moves



Minimum force so crate moves?

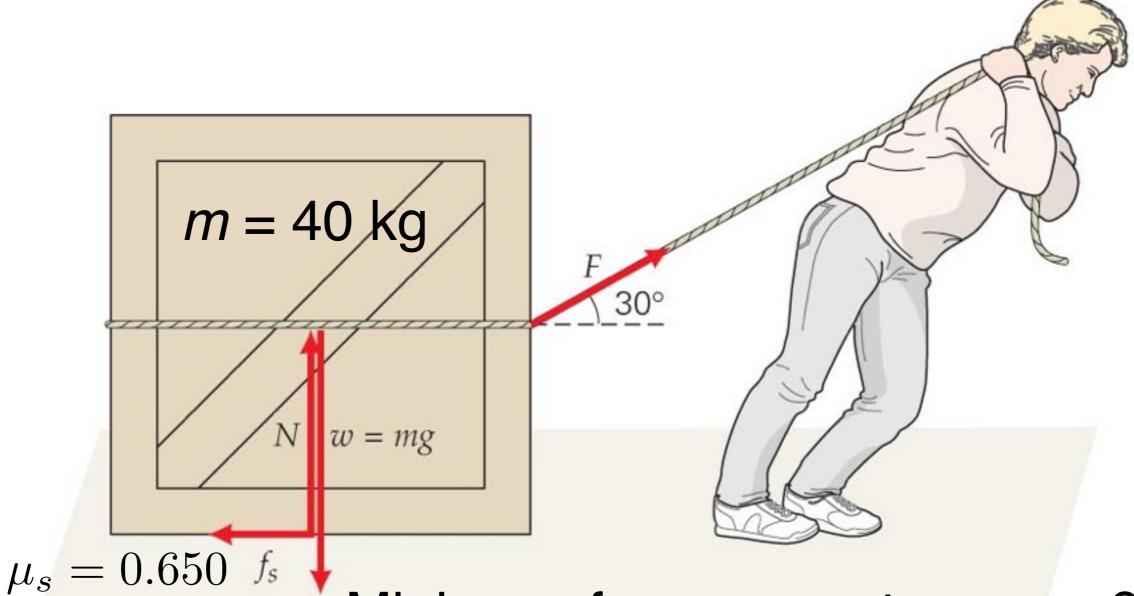
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Ex. 4.11

Given: $\theta = 30^{\circ}, \, \mu_s, \, m, \, g$

Goal: Min. F so crate moves

1.Read carefully



Minimum force so crate moves?

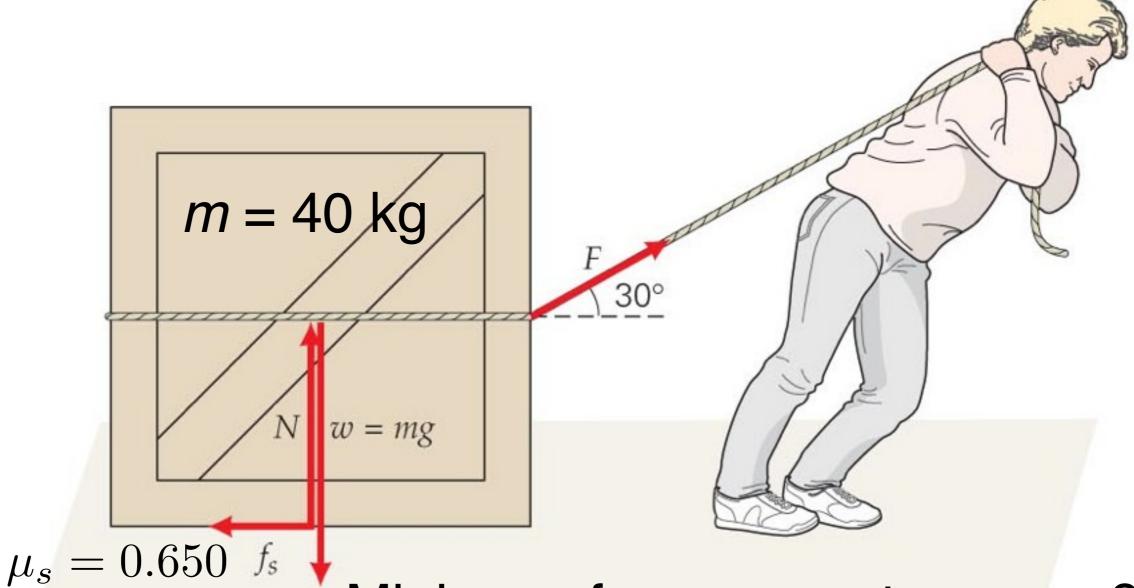
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Ex. 4.11

Given: $\theta = 30^{\circ}, \, \mu_s, \, m, \, g$

Goal: Min. F so crate moves

- 1.Read carefully
- 2.Draw a sketch = space diagram



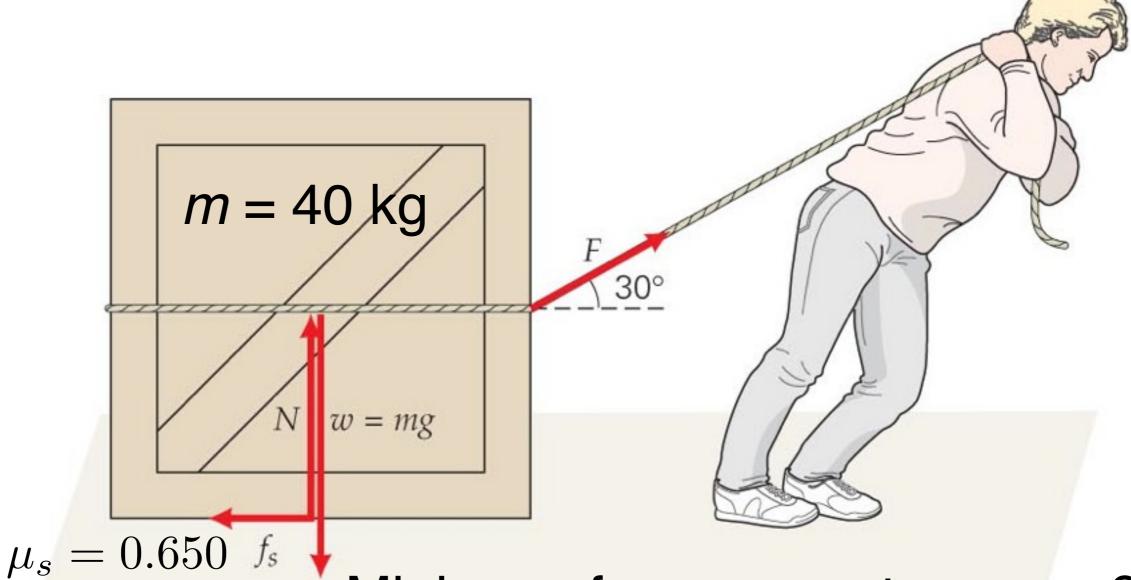
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Minimum force so crate moves?

Given: $\theta = 30^{\circ}, \, \mu_s, \, m, \, g$

Goal: Min. F so crate moves

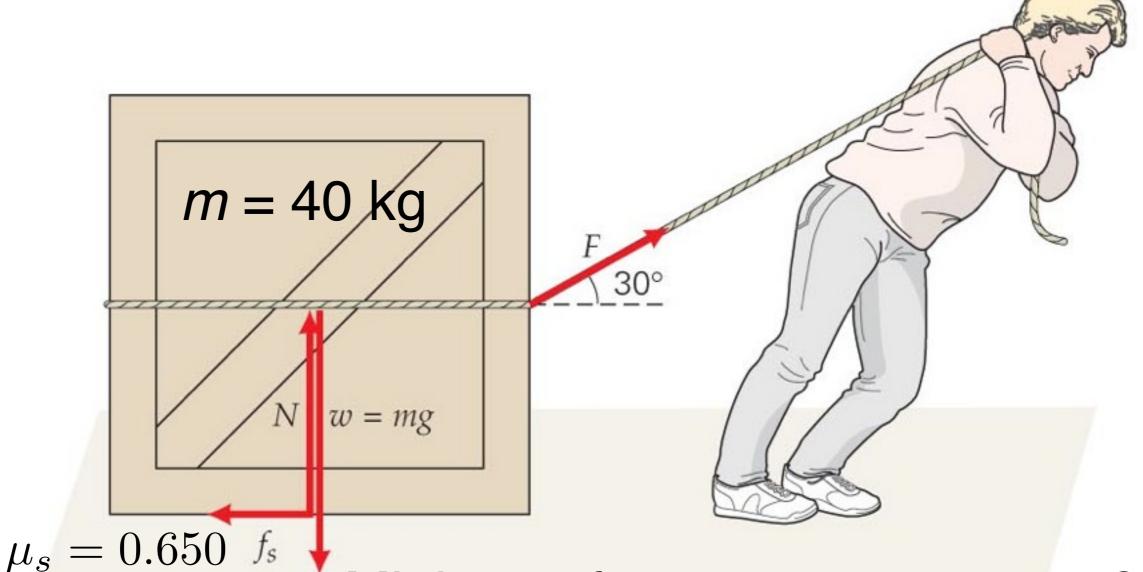
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Given: $\theta = 30^{\circ}, \, \mu_s, \, m, \, g$

Goal: Min. F so crate moves

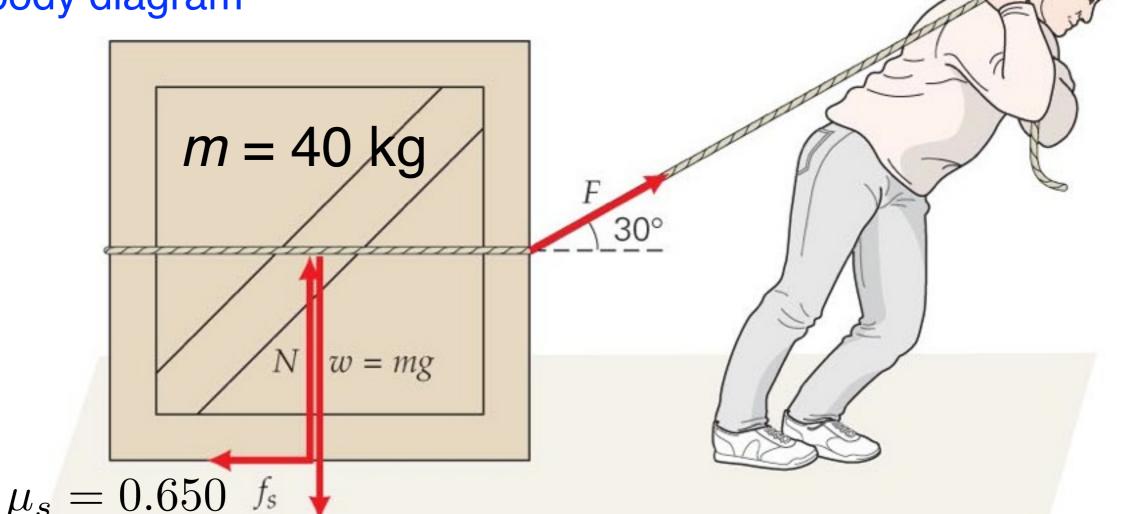
- 1.Read carefully
- 2.Draw a sketch = space diagram
- 3. Given? Goal?
- 4. Brainstorm: 2nd law + friction



Given: $\theta = 30^{\circ}, \, \mu_s, \, m, \, g$

Goal: Min. F so crate moves

- 1.Read carefully
- 2.Draw a sketch = space diagram
- 3. Given? Goal?
- 4. Brainstorm: 2nd law + friction 4a. For each body, draw a free-body diagram



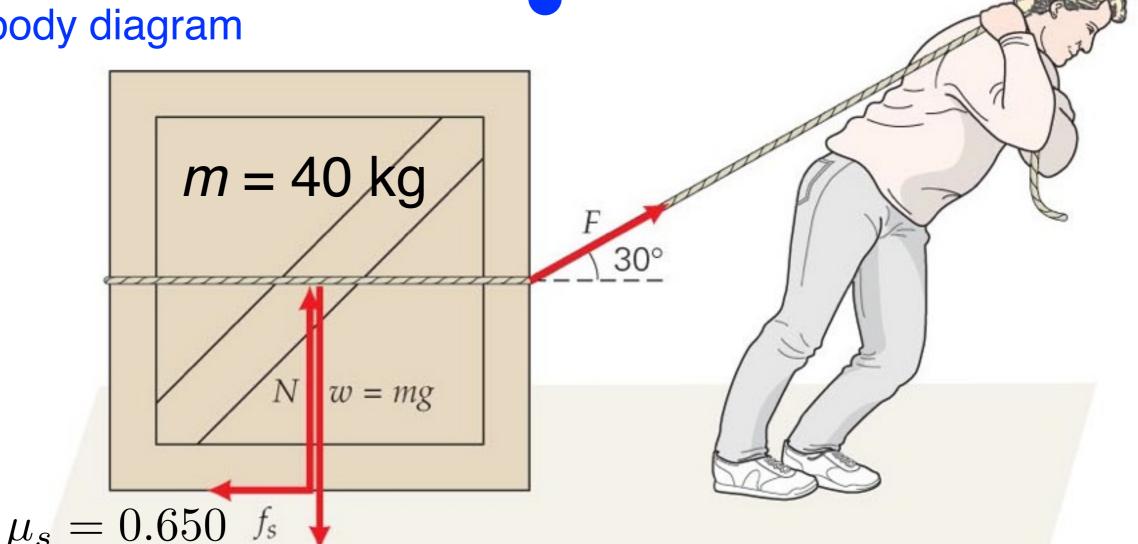
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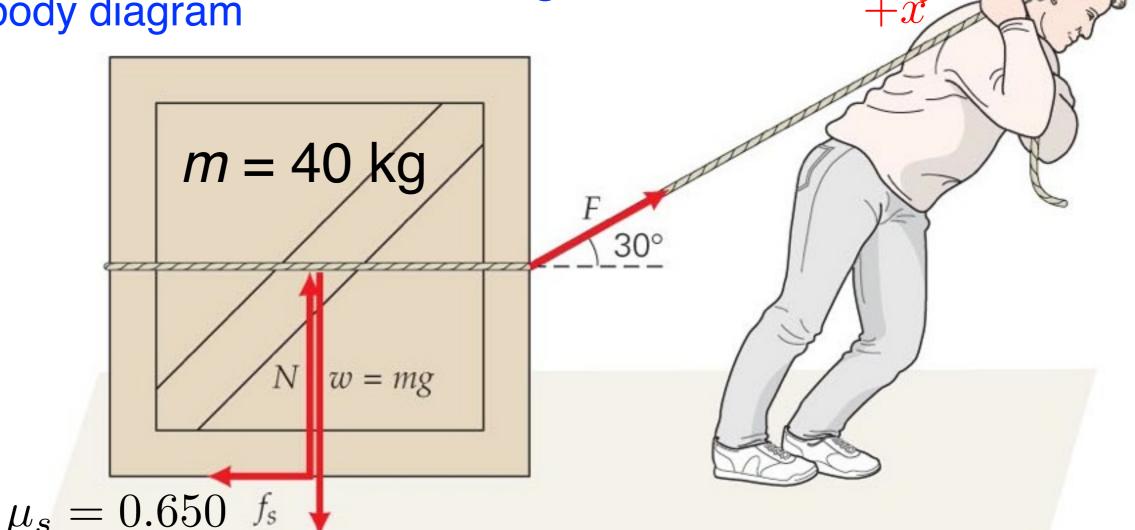
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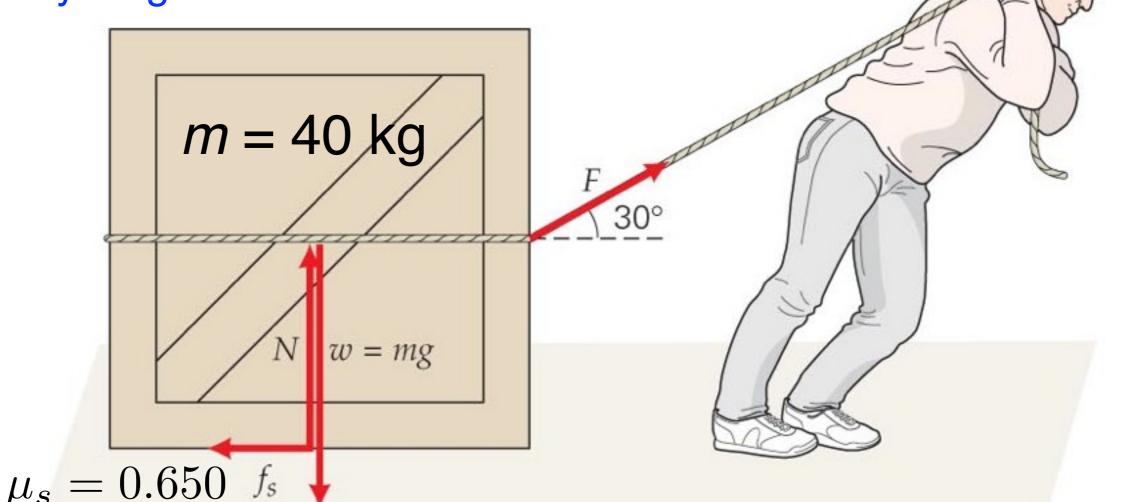
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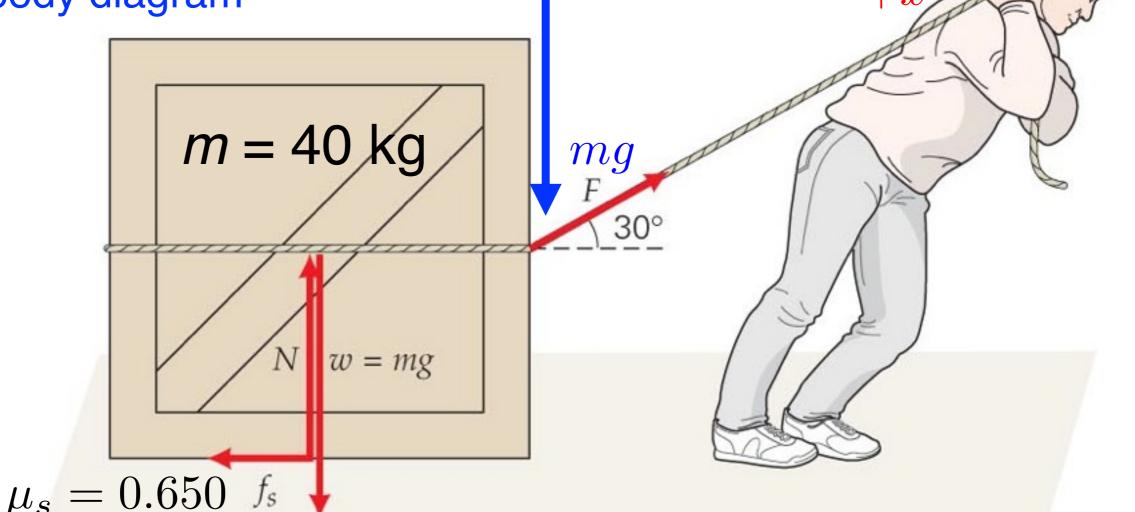


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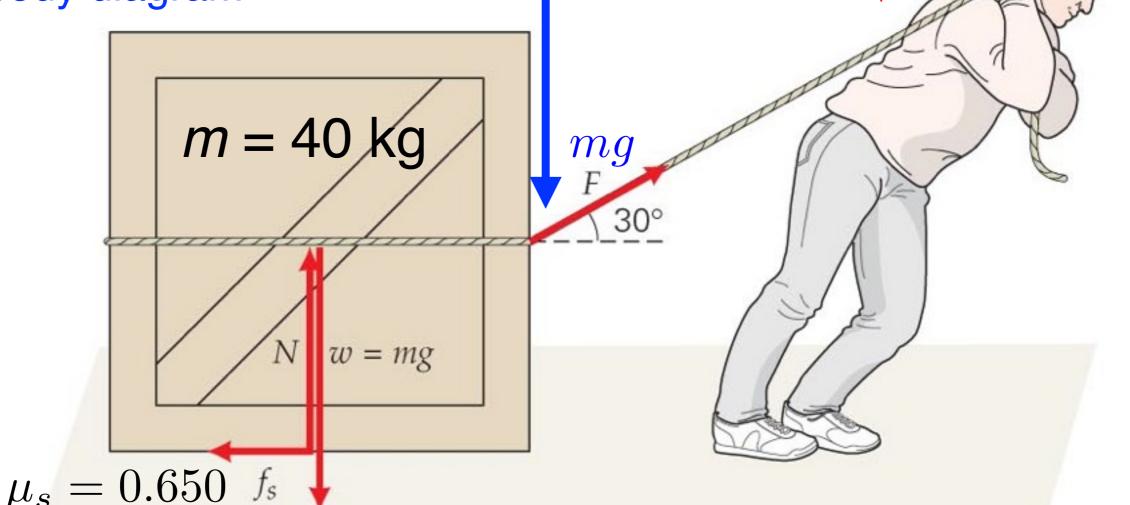
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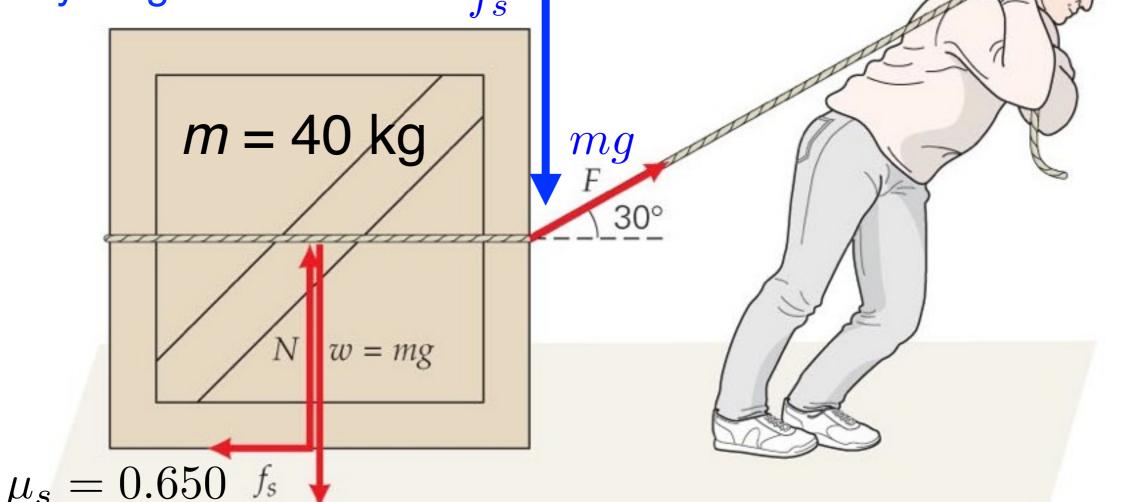
+y

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Given: $\theta = 30^{\circ}, \, \mu_s, \, m, \, g$

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+y

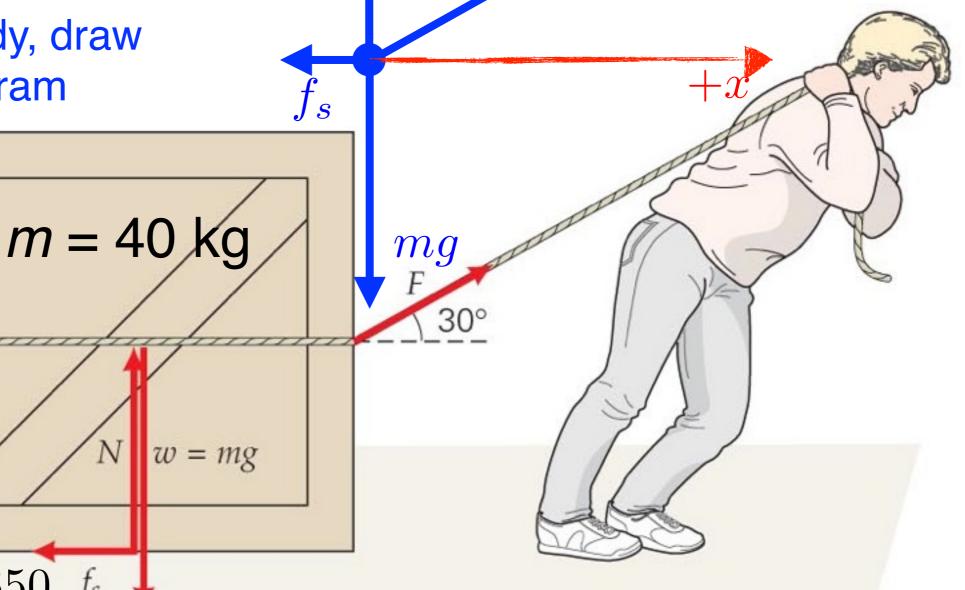
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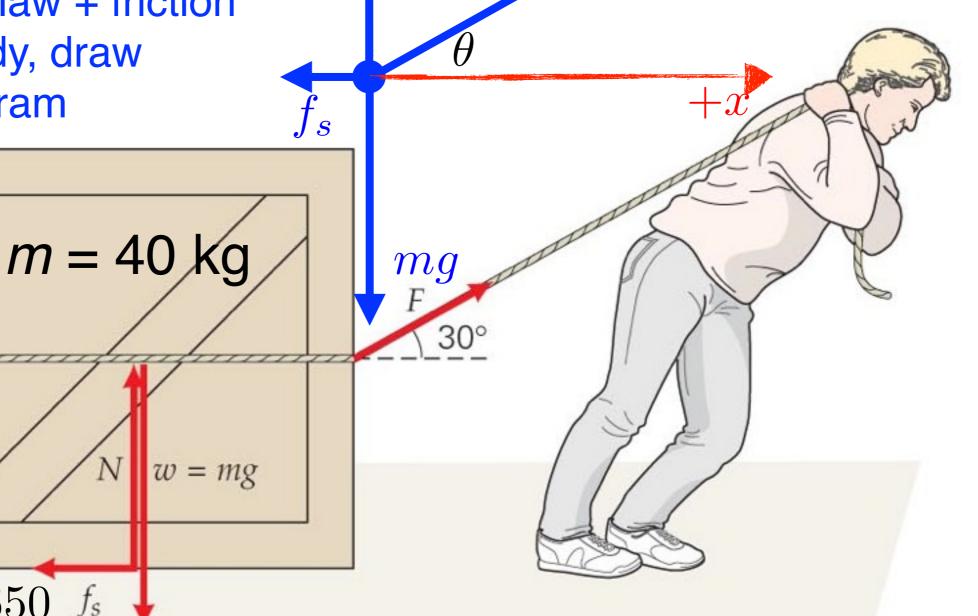
Minimum force so crate moves?

Given: $\theta = 30^{\circ}, \, \mu_s, \, m, \, g$

Goal: Min. F so crate moves

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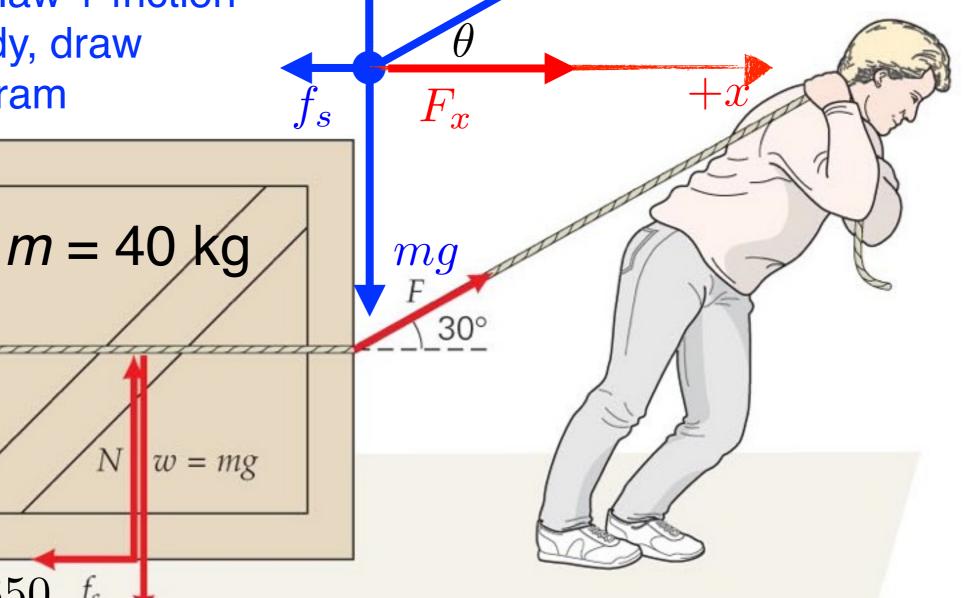
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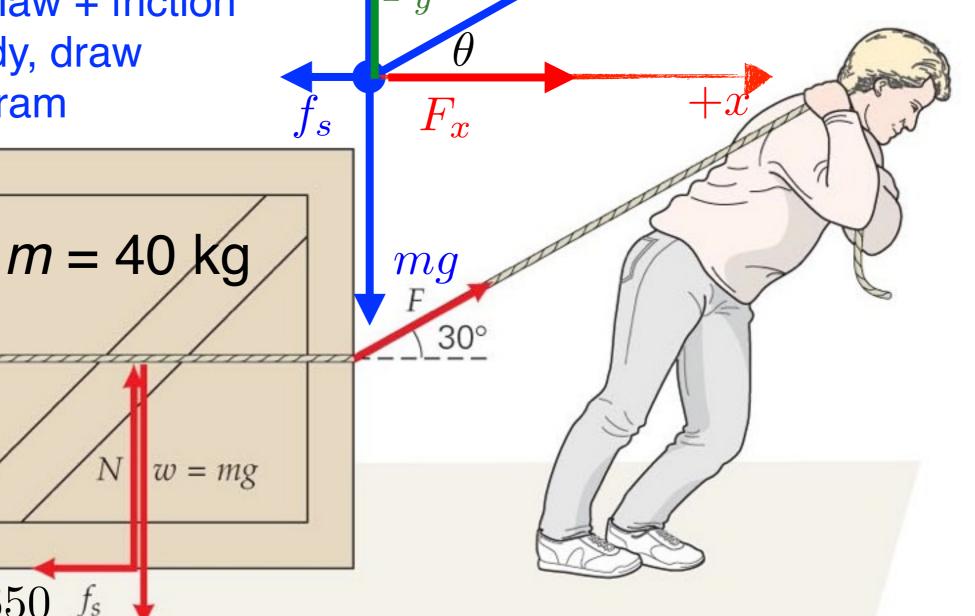
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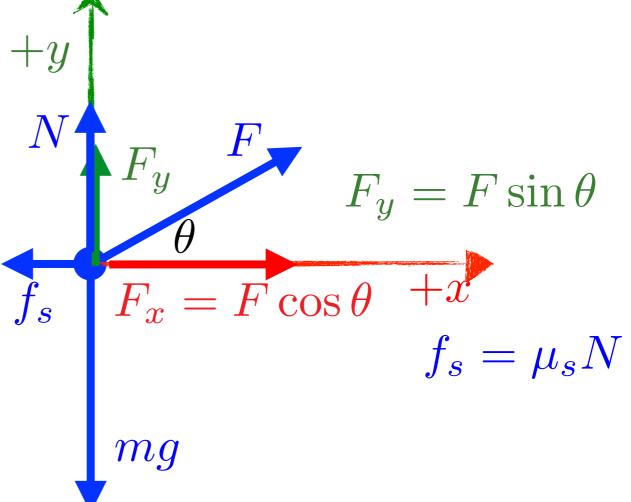
+y

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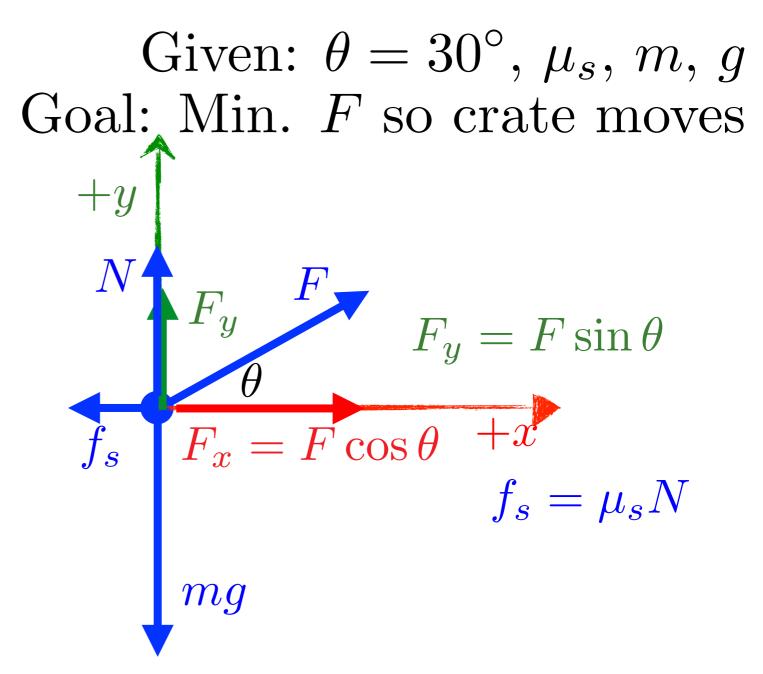


Minimum force so crate moves?

Given: $\theta = 30^{\circ}$, μ_s , m, g Goal: Min. F so crate moves +y



5. Calculate



5. Calculate

$$N + F\sin\theta - mg = 0$$

Given: $\theta = 30^{\circ}, \, \mu_s, \, m, \, g$ Goal: Min. F so crate moves

mg

5. Calculate

$$N + F\sin\theta - mg = 0$$
$$N = mg - F\sin\theta$$

Given: $\theta = 30^{\circ}, \, \mu_s, \, m, \, g$ Goal: Min. F so crate moves $= F \cos \theta + x$ $f_s = \mu_s N$

mg

5. Calculate

$$N + F \sin \theta - mg = 0$$
$$N = mg - F \sin \theta$$

$$F\cos\theta - f_s = ma \to 0 \text{ as } a \to 0$$

Given: $\theta = 30^{\circ}, \, \mu_s, \, m, \, g$ Goal: Min. F so crate moves $= F \cos \theta + x$ $f_s = \mu_s N$

$$f_s = \mu_s \Lambda$$

5. Calculate

$$N + F \sin \theta - mg = 0$$
$$N = mg - F \sin \theta$$

$$F\cos\theta - f_s = ma \to 0 \text{ as } a \to 0$$
$$F\cos\theta - \mu_s N = 0$$

Given: $\theta = 30^{\circ}$, μ_s , m, gGoal: Min. F so crate moves

$$F_{y} = F \sin \theta$$

$$F_{x} = F \cos \theta + x$$

$$f_{s} = \mu_{s} N$$

$$f_{s} = \mu_{s} N$$

5. Calculate

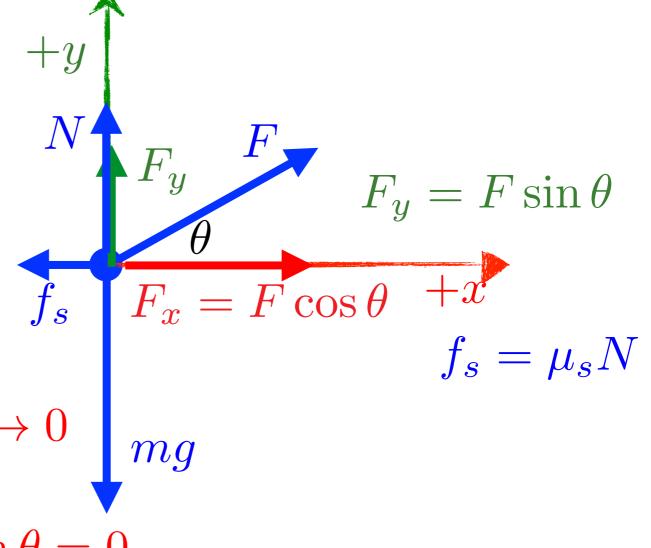
$$N + F \sin \theta - mg = 0$$
$$N = mg - F \sin \theta$$

$$F\cos\theta - f_s = ma \to 0 \text{ as } a \to 0$$

$$F\cos\theta - \mu_s N = 0$$

$$F\cos\theta - \mu_s Mg + \mu_s F\sin\theta = 0$$

Given: $\theta = 30^{\circ}$, μ_s , m, g Goal: Min. F so crate moves



5. Calculate

$$N + F \sin \theta - mg = 0$$
$$N = mg - F \sin \theta$$

$$F\cos\theta - f_s = ma \to 0 \text{ as } a \to 0$$

$$F\cos\theta - \mu_s N = 0$$

$$F\cos\theta - \mu_s mg + \mu_s F\sin\theta = 0$$

$$F(\cos\theta + \mu_s \sin\theta) = \mu_s mg$$

Given: $\theta = 30^{\circ}$, μ_s , m, g Goal: Min. F so crate moves

$$F_{y} = F \sin \theta$$

$$F_{x} = F \cos \theta + x$$

$$f_{s} = \mu_{s} N$$

$$\theta = 0$$

5. Calculate

$$N + F \sin \theta - mg = 0$$
$$N = mg - F \sin \theta$$

$$F\cos\theta - f_s = ma \to 0 \text{ as } a \to 0$$

 $F\cos\theta - \mu_s N = 0$
 $F\cos\theta - \mu_s mg + \mu_s F\sin\theta = 0$
 $F(\cos\theta + \mu_s\sin\theta) = \mu_s mg$

Given:
$$\theta = 30^{\circ}$$
, μ_s , m , g
Goal: Min. F so crate moves
$$+y$$

$$F_{y} = F \sin \theta$$

$$F_{x} = F \cos \theta + x$$

$$f_{s} = \mu_{s} N$$

$$\theta = 0$$

$$F = \frac{\mu_{s} mg}{\cos \theta + \mu_{s} \sin \theta}$$

5. Calculate(6. Plug in numbers)

$$N + F \sin \theta - mg = 0$$
$$N = mg - F \sin \theta$$

$$F\cos\theta - f_s = ma \to 0 \text{ as } a \to 0$$

 $F\cos\theta - \mu_s N = 0$
 $F\cos\theta - \mu_s mg + \mu_s F\sin\theta = 0$
 $F(\cos\theta + \mu_s\sin\theta) = \mu_s mg$

Given:
$$\theta = 30^{\circ}$$
, μ_s , m , g
Goal: Min. F so crate moves
$$F_y = F \sin \theta$$

$$F_x = F \cos \theta + x$$

$$f_s = \mu_s N$$

$$F = \frac{\mu_s mg}{\cos \theta + \mu_s \sin \theta}$$

5. Calculate (6. Plug in numbers)

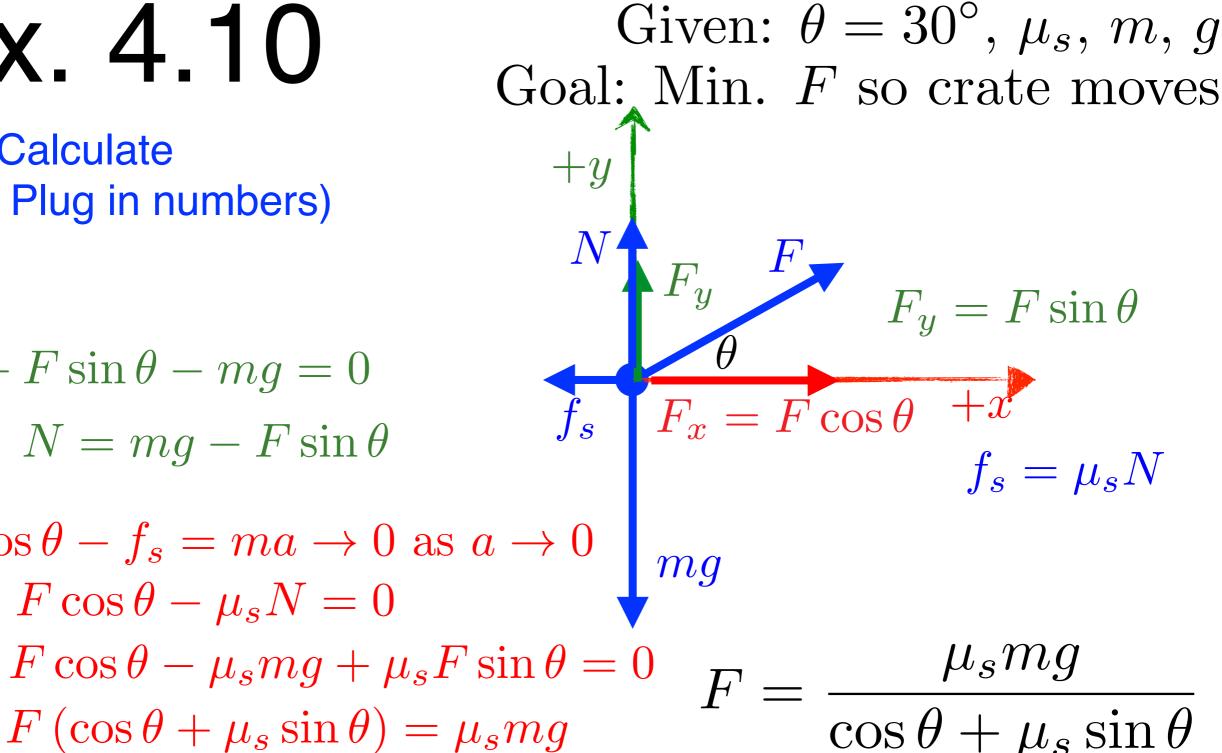
$$N + F \sin \theta - mg = 0$$
$$N = mg - F \sin \theta$$

$$F\cos\theta - f_s = ma \to 0 \text{ as } a \to 0$$

$$F\cos\theta - \mu_s N = 0$$

$$F\cos\theta - \mu_s mg + \mu_s F\sin\theta = 0$$

$$\mu_s = 0.650$$



5. Calculate (6. Plug in numbers)

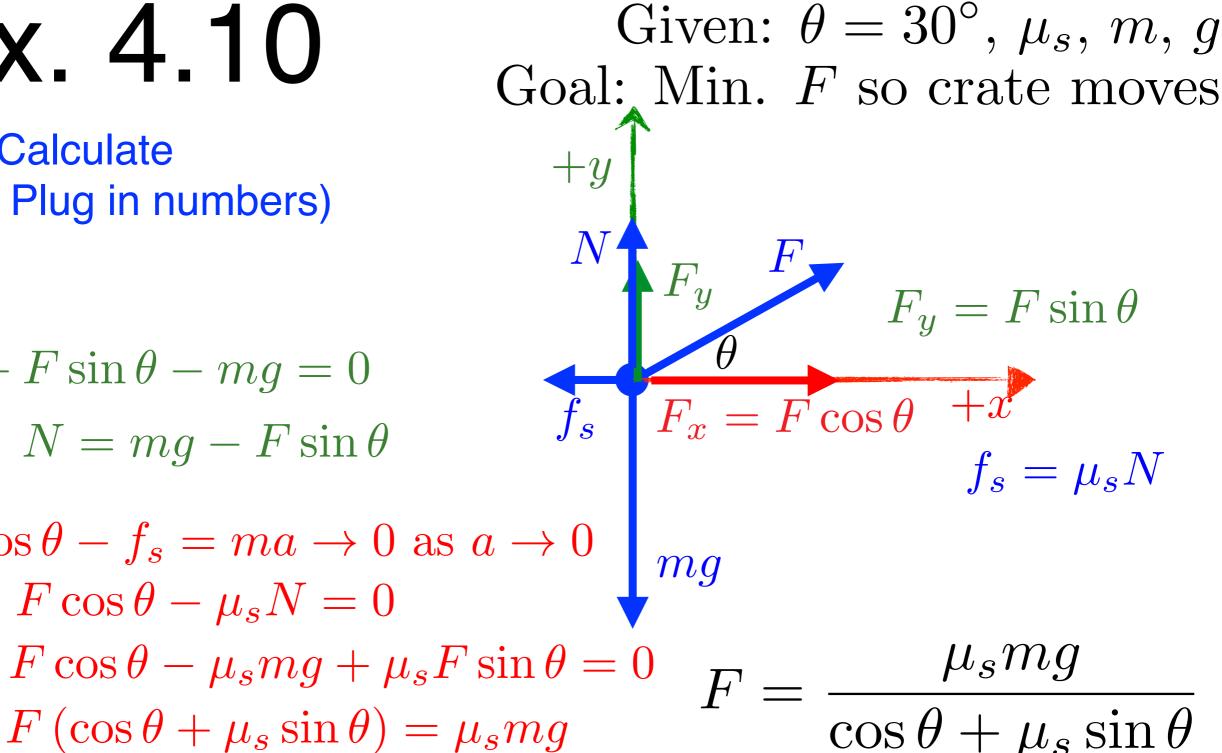
$$N + F \sin \theta - mg = 0$$
$$N = mg - F \sin \theta$$

$$F\cos\theta - f_s = ma \to 0 \text{ as } a \to 0$$

$$F\cos\theta - \mu_s N = 0$$

$$F\cos\theta - \mu_s mg + \mu_s F\sin\theta = 0$$

$$\mu_s = 0.650$$
$$m = 40 \text{ kg}$$



5. Calculate(6. Plug in numbers)

$$N + F \sin \theta - mg = 0$$
$$N = mg - F \sin \theta$$

$$F\cos\theta - f_s = ma \to 0 \text{ as } a \to 0$$

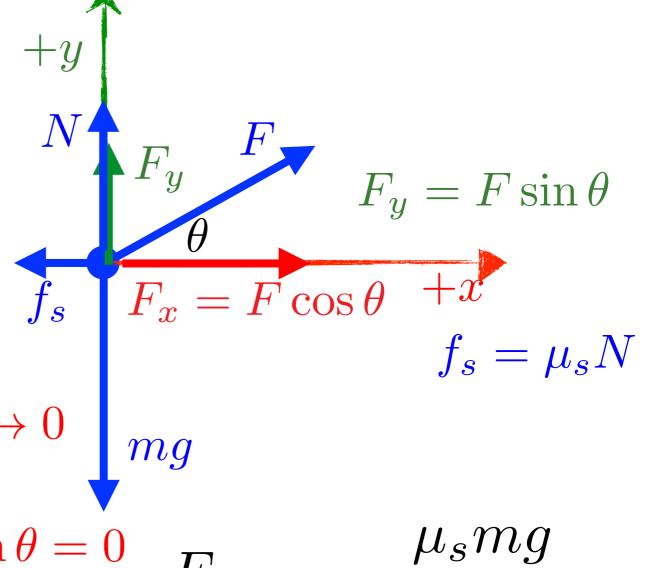
$$F\cos\theta - \mu_s N = 0$$

$$F\cos\theta - \mu_s mg + \mu_s F\sin\theta = 0$$

 $F\left(\cos\theta + \mu_s\sin\theta\right) = \mu_s mg$

$$\mu_s = 0.650$$
$$m = 40 \text{ kg}$$

Given: $\theta = 30^{\circ}$, μ_s , m, g Goal: Min. F so crate moves



$$F = 214 \text{ N (vs. } 255 \text{ N for } \theta = 0)$$

- 5. Calculate
- (6. Plug in numbers)
- 7. Is answer reasonable?

$$N + F \sin \theta - mg = 0$$
$$N = mg - F \sin \theta$$

Given: $\theta = 30^{\circ}$, μ_s , m, g Goal: Min. F so crate moves

$$F_{y} = F \sin \theta$$

$$F_{x} = F \cos \theta + x$$

$$f_{s} = \mu_{s} N$$

$$f_{s} = \mu_{s} N$$

$$F\cos\theta - f_s = ma \to 0 \text{ as } a \to 0$$

$$F\cos\theta - \mu_s N = 0$$

$$F\cos\theta - \mu_s mg + \mu_s F\sin\theta = 0$$

$$F(\cos\theta + \mu_s \sin\theta) = \mu_s mg$$

$$F = \frac{\mu_s mg}{\cos\theta + \mu_s \sin\theta}$$

$$\mu_s = 0.650$$
 $m = 40 \text{ kg}$
 $F = 214 \text{ N (vs. 255 N for } \theta = 0)$