

## Lecture 11: Lighting and Shading

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### 1 Shading - Real world

Different types of light-material interactions cause that the object appears to have different colors or shading. Components that play role in these interactions:

- light sources
- material properties
- viewer location
- surface orientation

In real world the light is scattered back and forth between objects, partially absorbed here and there, all in an infinite and quite complex manner expressed by **Rendering equation**.

#### 1.1 Rendering Equation

- describes infinite scattering and absorption
- cannot be solved in general
- global effect

#### 1.2 Ray Tracing

- approach to compute perfectly reflecting surfaces
- not suitable for pipelining

#### 1.3 Global effects

- like translucent surfaces, shadows, multiple light scattering

#### 1.4 Local effects

- good for pipeline architecture, usually can provide sufficient approximation

## 2 Light Sources

### 2.1 Actual light source

- contains infinite number of points
- create soft shadows

### 2.2 Simple light sources

- **Point:** defined by position, color
- **Distant:** special case of Point source, placed in infinity, casts parallel arrays of light, defined by vector
- **Spotlight:** point source restricted in direction
- **Ambient:** same intensity everywhere, can model contribution of many sources and reflective surfaces

## 3 Surface types

### 3.1 Smooth

Ideal smooth surface is a perfect mirror, reflects all light concentrated in one direction.

### 3.2 Rough

Scatters light in all directions.

## 4 Phong Model

Simple, enables rapid computation. But cannot create mirrors. Three main light components are **diffuse**, **specular** and **ambient**. Works with four vectors: direction to light source **l**, direction to viewer **v**, surface normal **n** and perfect reflector **r**.

### 4.1 Ideal Reflector

Ideal reflector has the same angle from **n** as **l** (**angle of incidence** or **angle of reflection**), we assume all three vectors are coplanar. Reflector can be computed  $\mathbf{r} = 2(\mathbf{l} \cdot \mathbf{n})\mathbf{n} - \mathbf{l}$

## 4.2 Lambertian Surface

Lambertian surface is a perfect diffuse reflector. Amount of reflected light is proportional to the vertical component of light. In other words

$$reflectedLight \propto \cos \theta_i$$

where  $\theta_i$  is the angle of incidence. A way to think about it is, the larger the angle, the wider the “beam” of light and the less dense the intensity.

$$\cos \theta_i = \mathbf{l} \cdot \mathbf{n}$$

as long as  $\mathbf{n}$  and  $\mathbf{l}$  are normalized.

## 4.3 Diffuse Term

If we allow only some portion of incoming light to be diffused (no more Lambertian surface), the **diffuse term** can be computed as

$$I_d = L_d k_d (\mathbf{l} \cdot \mathbf{n})$$

where  $L_d$  is incoming light intensity. For material, amounts of light diffused can be expressed separately for each color:  $k_{dr}$ ,  $k_{dg}$ ,  $k_{db}$ .

## 4.4 Specular Term

For shiny surfaces, the Phong Model constructs simplistic model: the amount of light the user sees depends on the angle  $\phi$  between  $\mathbf{r}$  and  $\mathbf{v}$ . The shininess is specified by shininess coefficient  $\alpha$ .  $\alpha$  in range 100 and 200 approximates well metals, 5 to 10 plastic materials.

$$I_s = k_s L_s \cos^\alpha \phi = k_s L_s (\mathbf{r} \cdot \mathbf{v})^\alpha$$

assuming that  $\mathbf{r}$  and  $\mathbf{v}$  are normalized. Again for material, amounts of light reflected can be expressed separately for each color:  $k_{sr}$ ,  $k_{sg}$ ,  $k_{sb}$ .

## 4.5 Ambient Term

$$I_a = k_a L_a$$

Where  $L_a$  is the incoming light intensity. Again for material, amounts of light used for ambient lighting can be expressed separately for each color:  $k_{ar}$ ,  $k_{ag}$ ,  $k_{ab}$ .

## 4.6 Distance term

For positional light sources, we may also want to account for the attenuation of light received due to its distance from the source.  $(a + bd + cd^2)^{-1}$  where  $d$  is distance between  $\mathbf{p}$  and  $\mathbf{p}_0$ . Constants  $a, b, c$  can be chosen to soften lighting. This term is added to diffuse and specular lighting equations. It's not correct in terms of physics but it makes it look nicer.

#### 4.7 Light source

For diffuse, specular and ambient component and each for each color, we can express the source intensities with 9 variables:  $L_{dr}, L_{dg}, L_{db}, L_{sr}, L_{sg}, L_{sb}, L_{ar}, L_{ag}, L_{ab}$ .

#### 4.8 Adding sources

We can then compute the contribution for each color by all sources source by adding the ambient, diffuse, and specular components computed in previous sections together:  $I_{dr}, I_{dg}, I_{db}, I_{sr}, I_{sg}, I_{sb}, I_{ar}, I_{ag}, I_{ab}$ .

For example, for red term, it would be:

$$I_r = \sum_i (I_{iar} + I_{idr} + I_{isr}) + I_{ar}$$

$I_{ar}$  is the red component of the global ambient light.

Note, that we might be using a slightly different notation than in textbook. All  $L$ 's represent light components of different light sources. All  $I$ 's represent light intensities transformed by materials. Thus in the above equation, the  $L$ 's of each light source we previously “transformed” into  $I$ 's by material (by equation in next section) and now are being added together since we have multiple sources.

#### 4.9 Material properties

We are specifying ambient, diffuse, and specular reflectivity coefficients ( $k_a, k_d, k_s$ ) for each primary color.

Phong model allows us to compute the intensity of the reflected light that the viewer sees. It can be expressed as

$$I = k_d L_d \mathbf{l} \cdot \mathbf{n} + k_s L_s (\mathbf{v} \cdot \mathbf{r})^\alpha + k_a L_a$$

Or in a more developed fashion including the attenuation by the distance term:

$$I = \frac{1}{a + bd + cd^2} (k_d L_d \max(\mathbf{l} \cdot \mathbf{n}, 0) + k_s L_s \max((\mathbf{r} \cdot \mathbf{v})^\alpha, 0)) + k_a L_a$$

#### 4.10 Modified Phong model (Blinn-Phong Model)

With the Phong model, we have to recalculate  $\mathbf{r} \cdot \mathbf{v}$  at every point on the surface. If we take vector  $\mathbf{h}$  halfway between  $\mathbf{v}$  and  $\mathbf{r}$

$$\mathbf{h} = \frac{\mathbf{l} + \mathbf{v}}{|\mathbf{l} + \mathbf{v}|}$$

and  $\mathbf{v}$  lies in the same plane as  $\mathbf{l}$ ,  $\mathbf{n}$  and  $\mathbf{r}$  (which usually does not, but it still works pretty well), then we can replace  $\mathbf{r} \cdot \mathbf{v}$  with  $\mathbf{n} \cdot \mathbf{h}$  and avoid calculation of  $\mathbf{r}$ . However, the new angle is half the size of the previous and we have to appropriately fix the shininess coefficient.

## 5 Implementation in OpenGL

- Normally, we have to specify normal for each vertex.
- If we have normalized vectors, we can use dot product to compute cosines.
- GLSL vector normalization using  $n = \text{normalize}(v)$

### 5.1 Finding normal to the plane

Given noncollinear points  $p_0, p_1, p_2$ , we need to find the normal of the plane defined by these points. We can find the normal like this:

$$\mathbf{n} = (\mathbf{p}_2 - \mathbf{p}_0) \times (\mathbf{p}_1 - \mathbf{p}_0)$$

### 5.2 Light sources

- Diffuse, ambient, specular.
- Specified in homogeneous coordinates, 0 in  $w$  coordinate for parallel light source (distant), 1 for point light source.
- Attenuation at the edges for spotlight is proportional to  $\cos^\alpha \phi$ .
- We can use global ambient term instead of ambient term for each light source. Easier calculation, same result.

### 5.3 Polygon shading

- If we use normals of the polygons that approximate the shape (e.g. sphere), it'll be very ugly.
- In simple cases we can solve analytically (like sphere), we can get precise normals. For more complex shapes, we can't get normals everywhere.
- Gouraud shading solves this by defining the normal at a vertex to be the normalized average of the normals of the polygons that share the vertex.