

Lecture 25: Fatigue Failure Theories II

BAEN 375
Design Fundamentals of Agricultural
Machines and Structures

Fatigue Failure Models

- There are 3 Fatigue Failure Models
 - Stress-Life (S-N)
 - Strain-Life (ϵ -N)
 - Linear-Elastic Fracture-Mechanics (LEFM)
- There are 2 Fatigue Regimes
 - Low-Cycle Fatigue (LCF)
 - High-Cycle Fatigue (HCF)
 - For this text/course, the assumption is 10^3 cycles divides LCF from HCF

Fatigue Failure Models

- Stress-Life (S-N) Approach
 - Most often used for HCF applications
 - Works best when load amplitudes are
 - Predictable
 - Consistent
 - Stress-based model that determines
 - Fatigue strength
 - Endurance limit
 - Attempts to keep stress in notches in elastic range to prevent crack initiation

Fatigue Failure Models

- Stress-Life (S-N) Approach
 - Pluses
 - Easy
 - Lots of relevant data available
 - Minuses
 - Most empirical
 - Least accurate
 - Not good for LCF design

Fatigue Failure Models

- Strain-Life (ϵ -N) Approach
 - Gives fairly accurate picture of crack initiation stage
 - Accounts for cumulative damage from variation in cyclic load over life of part
 - Handles fatigue loading combined with temperature because creep can be included
 - Plus
 - Works well with LCF design
 - Minuses
 - Most complicated
 - Requires computer solution

Fatigue Failure Models

- LEFM Approach
 - Provides best model of crack propagation stage
 - Applied to LCF design
 - Useful in predicting remaining life of cracked parts
 - Used with NDT in periodic service inspections
 - Requires accurate
 - Stress intensity geometry factor (β)
 - Estimate of initial crack size

Fatigue Failure Models

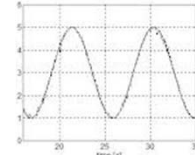
- Fatigue Loads

- Rotating Machinery Loading

- Stress-time (strain-time) functions can be represented as sinusoids characterized by

- Minimum stress (or strain) amplitude

- Maximum stress (or strain) amplitude



$$\Delta\sigma = \sigma_{max} - \sigma_{min} \quad \text{where } \Delta\sigma = \text{stress range}$$

$$\sigma_a = \frac{\sigma_{max} - \sigma_{min}}{2} \quad \text{where } \sigma_a = \text{alternating component}$$

$$\sigma_m = \frac{\sigma_{max} + \sigma_{min}}{2} \quad \text{where } \sigma_m = \text{mean component}$$

$$R = \frac{\sigma_{min}}{\sigma_{max}} \quad \text{where } R = \text{stress ratio}$$

$$A = \frac{\sigma_a}{\sigma_m} \quad \text{where } A = \text{amplitude ratio}$$

Fatigue Failure Models

- Service Equipment Loading

- Semi-random
- Non-cyclical, so the load-time function is difficult to define
- Good data come from measurements on machines in operation or simulated conditions

