

## Priority Line Mechanism: An Example

Suppose there are four people: 1, 2, 3, 4 and four houses A, B, C, D. Preferences are:

- 1:  $A > B > C > D$
- 2:  $B > C > A > D$       Owns A
- 3:  $C > A > D > B$       Owns D
- 4:  $A > C > B > D$

To begin, house B and C are vacant. The priority order is 1, 2, 3, 4.

### Priority Line Algorithm

Under the priority line algorithm, individuals pick in order of their priority and point to a house. If vacant, they take it. If occupied, the owner goes to the front of the line and picks a house. If a cycle forms, we clear it and continue.

- 1 chooses first and wants A, owned by 2. So 2 gets to jump ahead in line.
- 2 chooses B, which is vacant. (2,B) is cleared. Now A is vacant.
- 1 chooses A, now vacant. (1, A) is cleared.
- 3 chooses C, which is vacant. (3, C) is cleared.
- 4 takes D, the only house left. (4, D) is cleared.

Final match is (1,A), (2,B), (3,C), (4,D).

### Equivalent Top Trading Cycles Approach

This runs like regular TTC, except that at every round, vacant houses all point to the remaining person with highest priority.

Round 1: Vacant houses B, C. Here is the pointing...

- 1 -> A      A -> 2 (2 owns A)
- 2 -> B      B -> 1 (1 is highest priority)
- 3 -> C      C -> 1 (1 is highest priority)
- 4 -> A      D -> 3 (3 owns D)

The cycle is 1->A ->2 ->B ->1. So we clear (1,A) and (2,B).

Round 2: Vacant house C.

- 3 -> C      C -> 3 (3 is highest remaining priority with 1,2 gone)
- 4 -> C      D -> 3 (3 owns D)

The cycle is 3 -> C -> 3. So we clear (3, C).

Round 3: only (4,D) are left, clear them. Same outcome as Priority Line!