## ENGR 105: Feedback Control Design Winter 2013

## Lecture 8 - Closed-Loop Systems

Friday, January 25, 2013

## Today's Objectives

- 1. develop closed-loop system transfer functions
- 2. examine the behavior of closed-loop poles

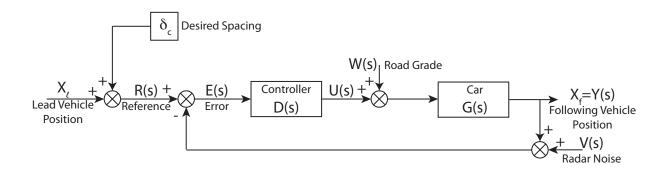
Reading: FPE Section 4.1

## 1 Closed-loop system transfer functions

The payoff for studying Laplace transforms and transfer functions is the ability to design controllers that can achieve desired performance characteristics. We will study this over the next few lectures for a system in the form:



To make the concepts more concrete, we will use the example of vehicle following. Here, a following vehicle tries to maintain a constant distance behind a lead vehicle. This is one suggested scenario for autonomous cars.

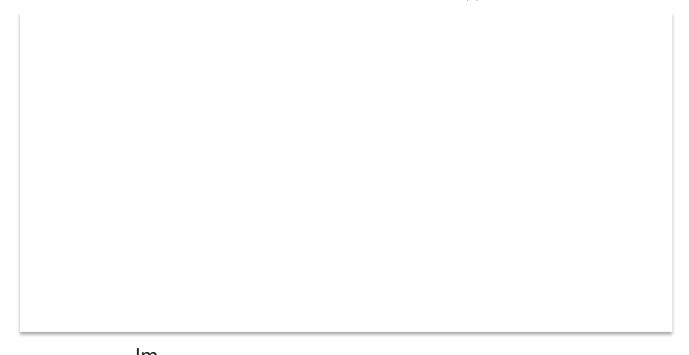


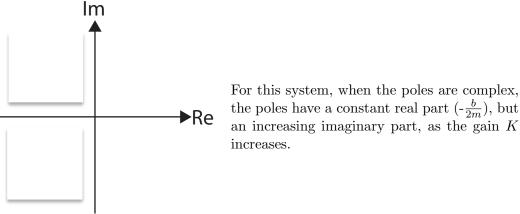
We will model the following vehicle as follows (where we use $x$ instead of $x_f$ for clarity):	
This can be re-written as:	
	h
The open loop system poles are at $s = 0$ and $s = -$	$\frac{\sigma}{m}$ . What does the pole at $s = 0$ imply?
We can look at the response of $Y$ , $E$ or $U$ to $R$ , $W$	or $V$ :
	<b>V2</b>
The first thing to notice is that all nine transfer fu	unctions contained in these equations have the
same denominator. This means that all of the response	
2 Closed-loop poles	
	oquation:
The poles are just the solution to the characteristic	equation:
Stability of the system is determined by the poles.	· ·
the book defines stability as having all poles in the l	ett half plane. Under this definition, the initial

conditions will decay to zero for a stable system. Systems with poles on the imaginary axis are unstable under this definition but can also be referred to as  $marginally\ stable$ . Note that marginally stable does not actually mean stable. Remember that the impulse response of a stable system always goes to zero as  $t \to \infty$ . This might not be true with a marginally stable system.

In terms of stability, there is no difference between the response of the output to a reference, the response of the error to a disturbance, or any other combination. If the system is stable, all of these transfer functions are stable.

For our example, we will begin with a proportional gain controller, D(s) = K:





What is a good location for the closed-loop poles? To answer this, we need to decide what we want the system to do. One approach is to place some specifications on the step response of the system, and we will examine this in the next lecture.