
Note: Homework is due **5pm** on the due date. Please submit your homework through the dropbox in the Siebel Center basement. Make sure to include your name and **netid** in your homework.

Problem 1 [5pt] Let \mathbf{A} and \mathbf{B} be two $n \times n$ matrices.

- (a) Is it necessarily true that $\mathbf{AB} = \mathbf{BA}$? Explain why or give an example where this does not hold.
- (b) Is it necessarily true that $\mathbf{A} + \mathbf{B} = \mathbf{B} + \mathbf{A}$? Explain why or give an example where this does not hold.

Problem 2 [5pt] True/False questions

- (a) (**True/False**) The forward elimination phase of naive Gaussian elimination produces an upper diagonal matrix.
- (b) (**True/False**) Every diagonal matrix is symmetric.
- (c) (**True/False**) Every $n \times n$ matrix has an inverse.
- (d) (**True/False**) The dot product of two vectors is a vector.
- (e) (**True/False**) A system of linear equations always has either one unique solution or no solutions.

Problem 3 [10pt] Consider the following system of equations:

$$\begin{cases} .209x_1 + .113x_2 = .647 \\ .458x_1 + .237x_2 = .981 \end{cases}$$

- (a) Rewrite the system in the form $\mathbf{Ax} = \mathbf{b}$ (matrix-vector form).
- (b) Solve the system by hand using Gaussian elimination. At every step in the calculation, retain 3 significant figures. Provide your answer, $\hat{\mathbf{x}}$, in vector form.
- (c) What is the exact solution? Use Python to compute the exact solution. Hint (Use the `numpy.linalg.solve()` command to compute the exact solution).
- (d) What is the residual vector with the approximation, $\hat{\mathbf{x}}$, from above?
- (e) What is the error vector with the approximation, $\hat{\mathbf{x}}$, from above?