

Homework Math 140, Lectures 20-21.

Will be quizzed Monday December 2

Problem 1 (page 273) Find all antiderivatives of the functions.

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| 1. $f(x) = x - 3.$ | 7. $f(x) = 7x^{2/5} + 8x^{-4/5}.$ | 13. $g(t) = \frac{1+t+t^2}{\sqrt{t}}.$ |
| 2. $f(x) = \frac{1}{2}x^2 - 2x + 6.$ | 8. $f(x) = x^{3.4} - 2x^{\sqrt{2}-1}.$ | 14. $f(x) = 3 \cos t - 4 \sin t.$ |
| 3. $f(x) = \frac{1}{2} + \frac{3}{4}x^2 - \frac{4}{5}x^3.$ | 9. $f(x) = \sqrt{2}.$ | 15. $f(\theta) = 2 \sin \theta - \sec^2 \theta.$ |
| 4. $f(x) = 8x^9 - 3x^6 + 12x^3.$ | 10. $f(x) = \pi^2.$ | 16. $f(\theta) = 6\theta^2 - 7 \sec^2 \theta.$ |
| 5. $f(x) = (x+1)(2x-1).$ | 11. $f(x) = \frac{10}{x^9}.$ | 17. $f(t) = 2 \sec t \tan t + \frac{1}{2}t^{-1/2}.$ |
| 6. $f(x) = x(2-x)^2.$ | 12. $f(x) = \frac{5-4x^3+2x^6}{x^6}.$ | 18. $f(x) = 2\sqrt{x} + 6 \cos x.$ |

Problem 2 Verify by differentiation that the formula is correct.

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| 1. $\int \frac{1}{x^2\sqrt{1+x^2}}dx = -\frac{\sqrt{1+x^2}}{x} + C.$ | 3. $\int \cos^3 x \, dx = \sin x - \frac{1}{3} \sin^3(x) + C.$ |
| 2. $\int \cos^2 x \, dx = \frac{1}{2}x + \frac{1}{4} \sin(2x) + C.$ | 4. $\int \frac{x}{\sqrt{a+bx}}dx = \frac{2}{3b^2}(bx-2a)\sqrt{a+bx} + C$ |

Problem 3 Evaluate the definite integral.

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| 1. $\int_{-2}^3 (x^2 - 3)dx.$ | 8. $\int_1^2 \left(\frac{1}{x^2} - \frac{4}{x^3} \right) dx.$ | 15. $\int_0^{\frac{\pi}{4}} \frac{1 + \cos^2 \theta}{\cos^2 \theta} d\theta.$ |
| 2. $\int_1^2 (4x^3 - 3x^2 + 2x)dx.$ | 9. $\int_1^4 \left(\frac{4+6u}{\sqrt{u}} \right) du.$ | 16. $\int_0^{\frac{\pi}{3}} \frac{\sin \theta + \sin \theta \tan^2 \theta}{\sec^2 \theta} d\theta.$ |
| 3. $\int_{-2}^0 \left(\frac{1}{2}t^4 + \frac{1}{4}t^3 - t \right) dt.$ | 10. $\int_1^2 \left(x + \frac{1}{x} \right)^2 dx.$ | 17. $\int_0^1 \frac{1 + \sqrt[3]{x}}{\sqrt{x}} dx.$ |
| 4. $\int_0^3 (1 + 6w^2 - 10w^4)dw.$ | 11. $\int_1^4 \sqrt{\frac{5}{x}} dx.$ | 18. $\int_1^8 \frac{x-1}{\sqrt[3]{x^2}} dx.$ |
| 5. $\int_0^2 (2x-3)(4x^2+1)dx.$ | 12. $\int_1^9 \frac{3x-2}{\sqrt{x}} dx.$ | 19. $\int_0^1 (\sqrt[4]{x^5} + \sqrt[5]{x^4}) dx.$ |
| 6. $\int_{-1}^1 t(1-t)^2 dt.$ | 13. $\int_1^4 \sqrt{t}(1+t)dt.$ | 20. $\int_0^1 (1+x^2)^3 dx.$ |
| 7. $\int_0^{\pi} (4 \sin \theta - 3 \cos \theta) d\theta.$ | 14. $\int_{\frac{\pi}{4}}^{\frac{\pi}{2}} \csc^2 \theta \, d\theta.$ | 21. $\int_2^5 x-3 dx.$ |

$$22. \int_0^2 |2x - 1| dx.$$

$$23. \int_{-1}^2 (x - 2|x|) dx.$$

$$24. \int_0^{\frac{3\pi}{2}} |\sin x| dx.$$