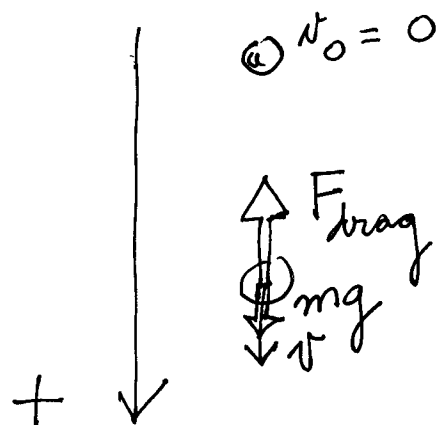


①



$$\text{EOM: } m \frac{dv}{dt} = -c_1 v + mg$$

It reaches terminal velocity v_t :

$$0 = -c_1 v_t + mg \rightarrow v_t = \frac{mg}{c_1}$$

$$\therefore \boxed{\frac{dv}{dt} = -\frac{v}{v_t} \cdot g + g = g \left(1 - \frac{v}{v_t}\right)}$$

$$\int_{0=v_0}^{v(t)} \frac{dv}{g \left(1 - \frac{v}{v_t}\right)} = \int_0^t dt$$

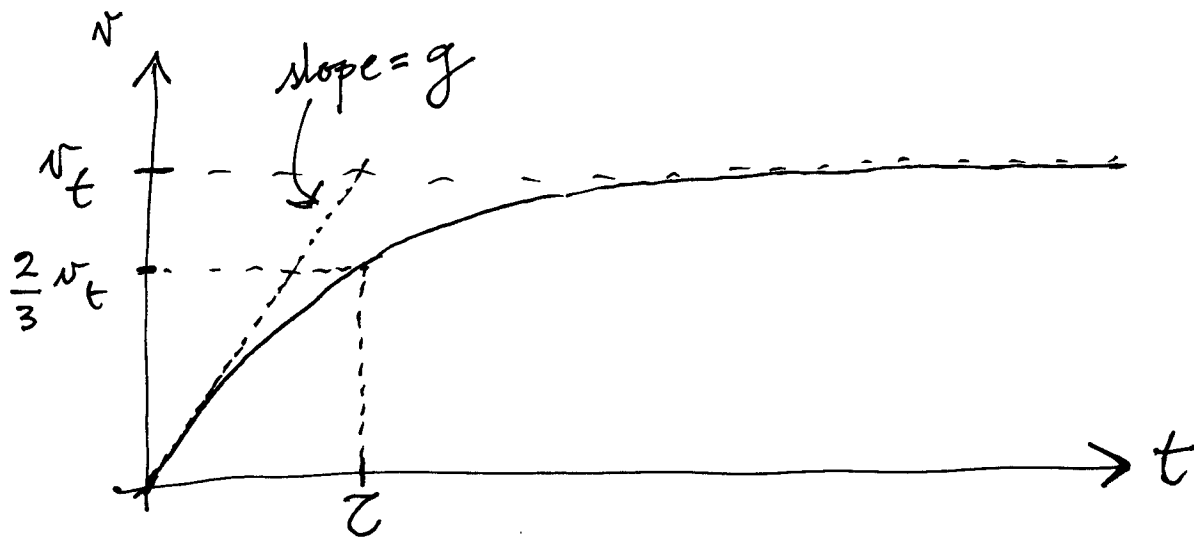
$$\rightarrow \left[-\frac{v_t}{g} \ln \left(1 - \frac{v}{v_t}\right) \right]_0^{v(t)} = t$$

(2)

$$\ln\left(1 - \frac{v}{v_t}\right) = -\frac{g}{v_t} \cdot t$$

$$1 - \frac{v}{v_t} = e^{-\frac{g}{v_t} \cdot t}$$

$$v = v_t \left(1 - e^{-\frac{g}{v_t} t}\right)$$



$$\text{If } 1/\tau = \frac{g}{v_t}, \quad v = v_t \left(1 - e^{-t/\tau}\right)$$

(3)

Linear or quadratic drag?

we found $v_{\text{critical}} = \frac{7.05 \times 10^{-4}}{D}$

In general, it reaches v_t when

↑⁺

$$0 = -mg + c_1/v_t + c_2/v_t^2$$

$$\rightarrow |v_t| = -\frac{v_c}{2} + \sqrt{\left(\frac{v_c}{2}\right)^2 + \frac{mg}{c_2}}$$