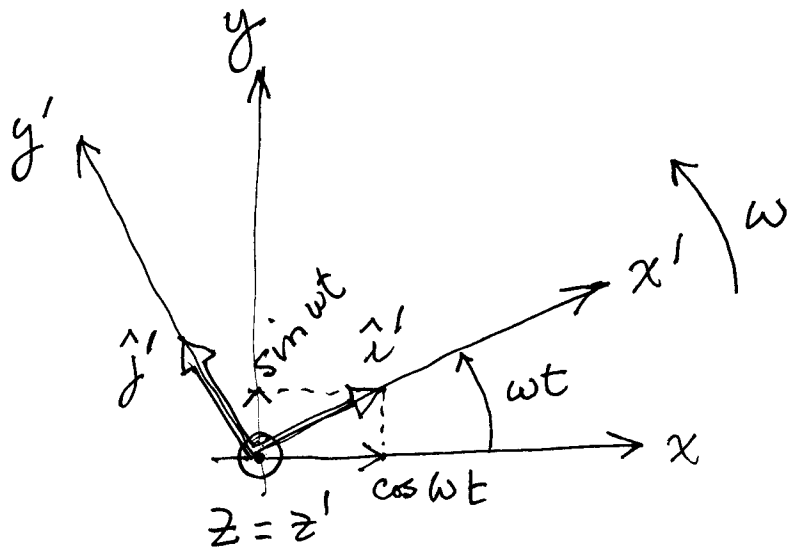




Define $\vec{\omega} = \omega \hat{k}$

$$\hat{i}' = \hat{i} \cos \omega t + \hat{j} \sin \omega t$$

$$\dot{\hat{i}}' = -\hat{i} \omega \sin \omega t + \hat{j} \omega \cos \omega t$$

Compare with

$$\vec{\omega} \times \hat{i}' = \omega \hat{k} \times \hat{i}' = \omega \hat{j}'$$

$$\therefore \dot{\hat{i}}' = \vec{\omega} \times \hat{i}'$$

$$\dot{\hat{j}}' = \vec{\omega} \times \hat{j}'$$

$$\downarrow$$

$$-\hat{i} \sin \omega t + \hat{j} \cos \omega t$$

Consider a generic vector $\vec{u}$. In the rotating frame

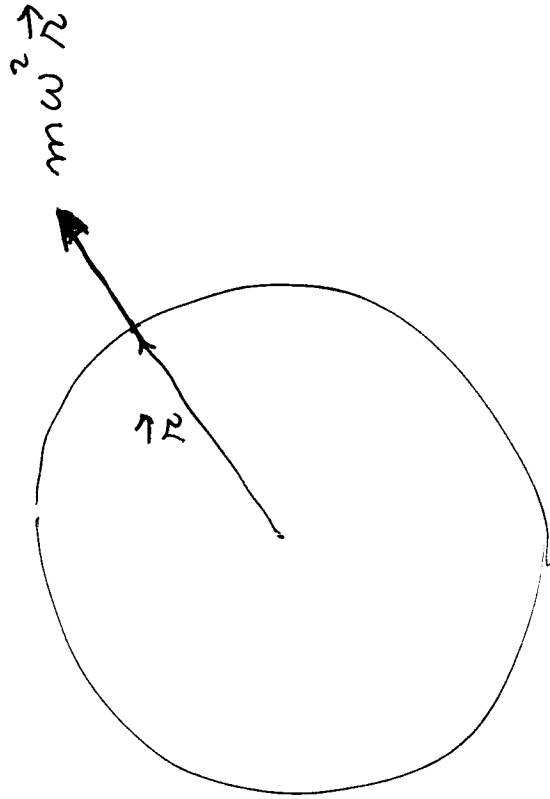
$$\vec{u} = u'_x \hat{i}' + u'_y \hat{j}'$$

$$\begin{aligned} \dot{\vec{u}} &= \underbrace{\dot{u}'_x \hat{i}' + \dot{u}'_y \hat{j}'}_{\left(\frac{d\vec{u}}{dt}\right)_{\text{rot}}} + \underbrace{u'_x \dot{\hat{i}}' + u'_y \dot{\hat{j}}'}_{\vec{\omega} \times \underbrace{(u'_x \hat{i}' + u'_y \hat{j}')}_{\vec{u}}} \\ &\uparrow \\ u_x \hat{i} + u_y \hat{j} &= \left(\frac{d\vec{u}}{dt}\right)_{\text{in}} \end{aligned}$$

$$\boxed{\left(\frac{d\vec{u}}{dt}\right)_{\text{in}} = \left(\frac{d\vec{u}}{dt}\right)_{\text{rot}} + \vec{\omega} \times \vec{u}}$$

$$\begin{aligned}
 m \vec{a}_{rot} = & \vec{F} - \underbrace{2m\vec{\omega} \times \vec{v}_{rot}}_{\text{Coriolis force}} - \underbrace{m\vec{\omega} \times (\vec{\omega} \times \vec{r})}_{\text{Centrifugal force}}
 \end{aligned}$$

If $\vec{v}_{rot} = 0$,



F. ex. set $\vec{u} = \vec{r}$

$$\vec{v}_{in} = \vec{v}_{rot} + \vec{\omega} \times \vec{r}$$

Now set $\vec{u} = \vec{v}_{in}$

$$\left(\frac{d\vec{v}_{in}}{dt} \right)_{in} = \left(\frac{d\vec{v}_{in}}{dt} \right)_{rot} + \vec{\omega} \times \vec{v}_{in}$$

$$\left(\frac{d\vec{v}_{in}}{dt} \right)_{in} = \left(\frac{d\vec{v}_{rot}}{dt} \right)_{rot} + \vec{\omega} \times \left(\frac{d\vec{r}}{dt} \right)_{rot} + \vec{\omega} \times \vec{v}_{rot} + \vec{\omega} \times (\vec{\omega} \times \vec{r})$$

$$\vec{a}_{in} = \vec{a}_{rot} + 2\vec{\omega} \times \vec{v}_{rot} + \underbrace{\vec{\omega} \times (\vec{\omega} \times \vec{r})}_{-\omega^2 \vec{r}}$$

$$\underbrace{m\vec{a}_{in}}_{\vec{F}} = m\vec{a}_{rot} + \dots$$

(gravity, Coulomb, etc.)

ROTATING PLATFORM

