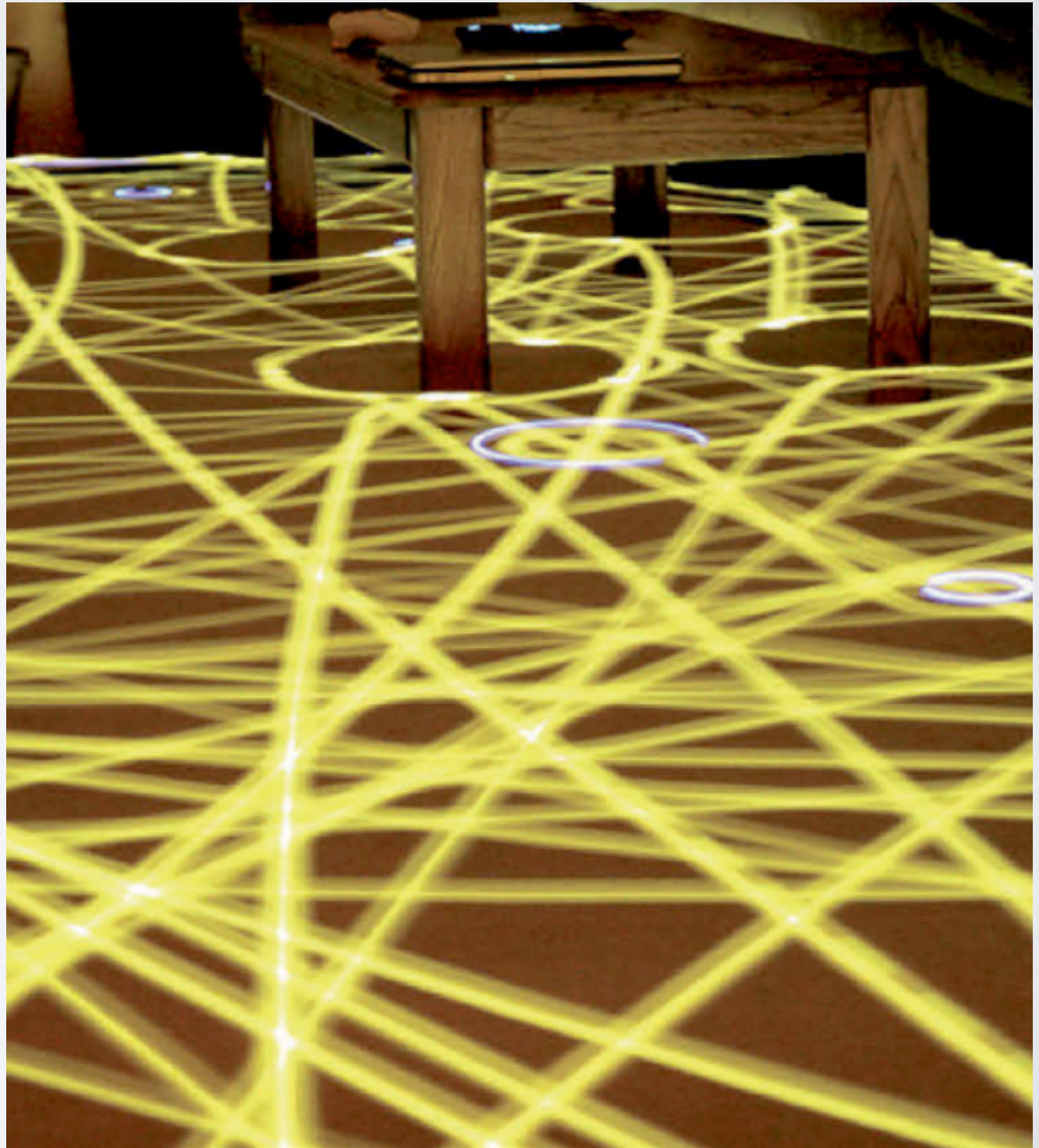


NAVIGATION

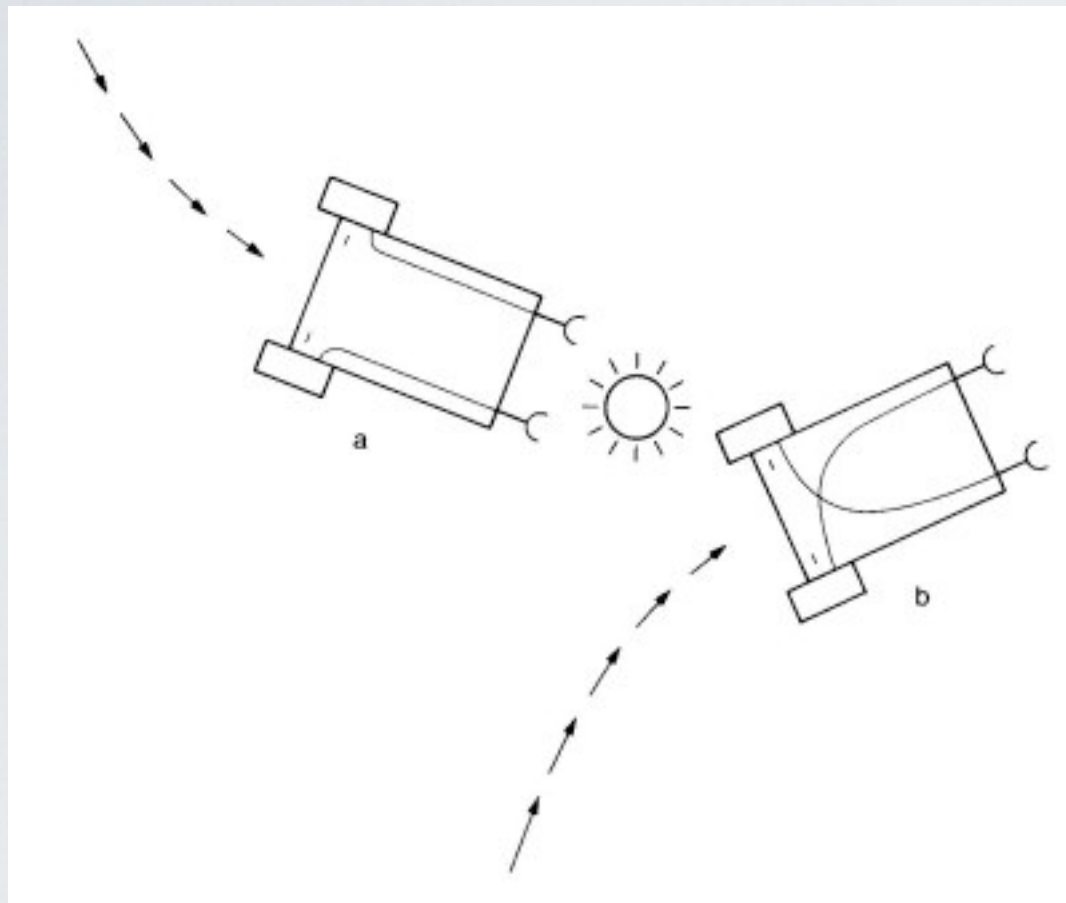
CS 3630 Introduction to Robotics and Perception
Frank Dellaert

INTRODUCTION

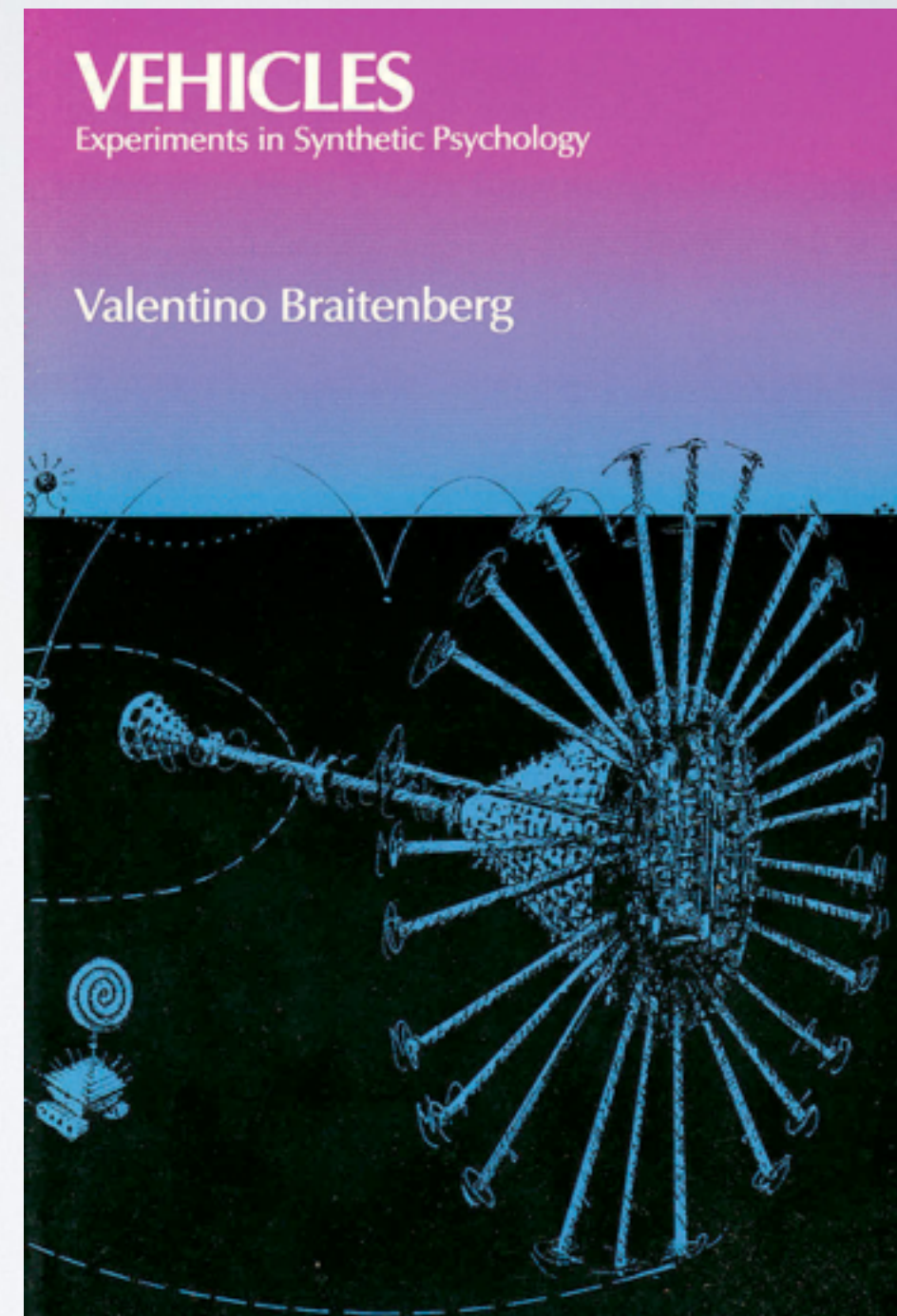
- Map-based Navigation
 - human-like
 - requires a map
- **Reactive Navigation**
 - Elsie
 - Roomba



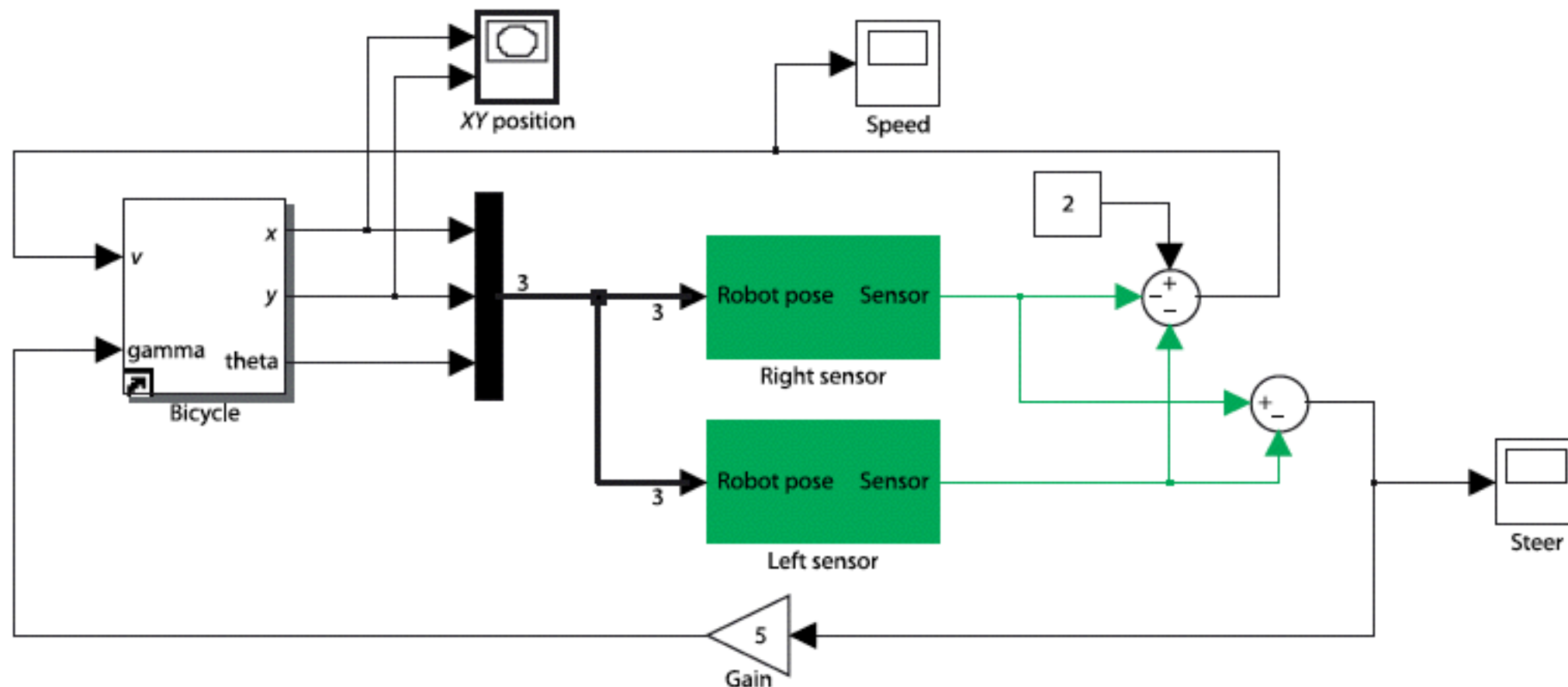
BRAITENBERG VEHICLES



- Love-Hate
- Simple Connections
- No (explicit) plan



RVC BRAITNAV



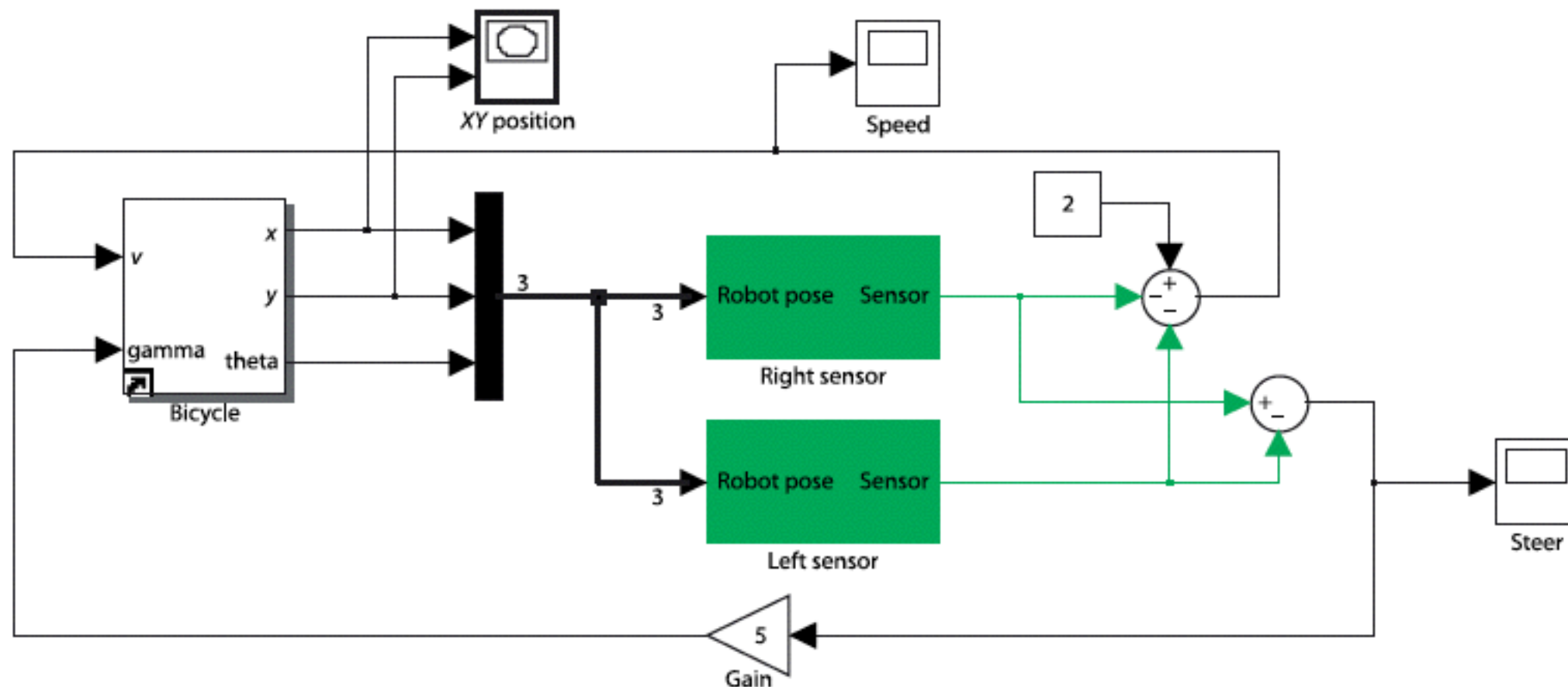
```

1 function sensor = sensorfield(x, y)
2     xc = 60; yc = 90;
3     sensor = 200./((x-xc).^2 + (y-yc).^2 + 200);

```

- $v = 2 - (s_r + s_l)$
- $g = k(s_r - s_l)$
- How to do this with Scribbler?
- Elsie had 4 behaviors (touch)

RVC BRAITNAV

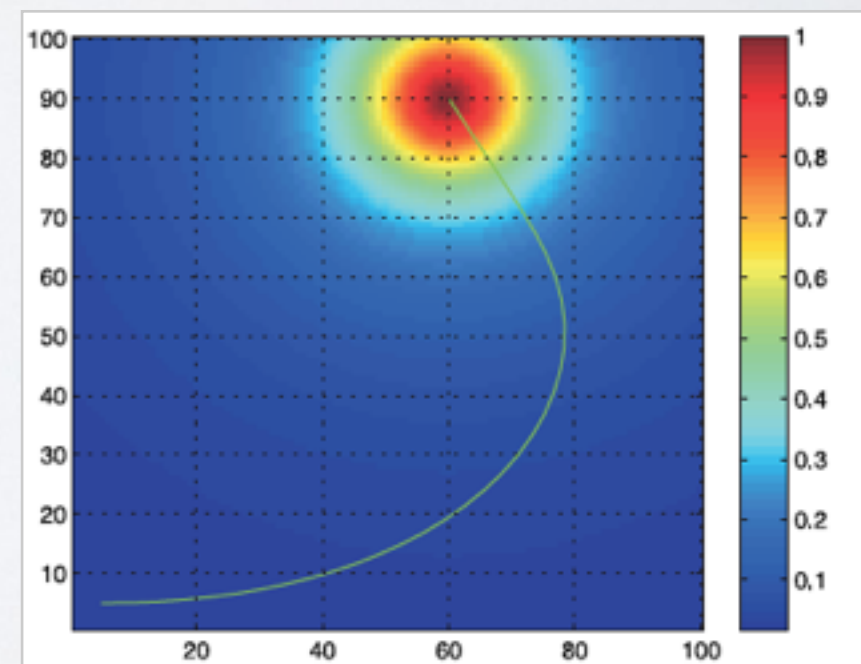


```

1 function sensor = sensorfield(x, y)
2     xc = 60; yc = 90;
3     sensor = 200./((x-xc).^2 + (y-yc).^2 + 200);

```

- $v = 2 - (s_r + s_l)$
- $g = k(s_r - s_l)$
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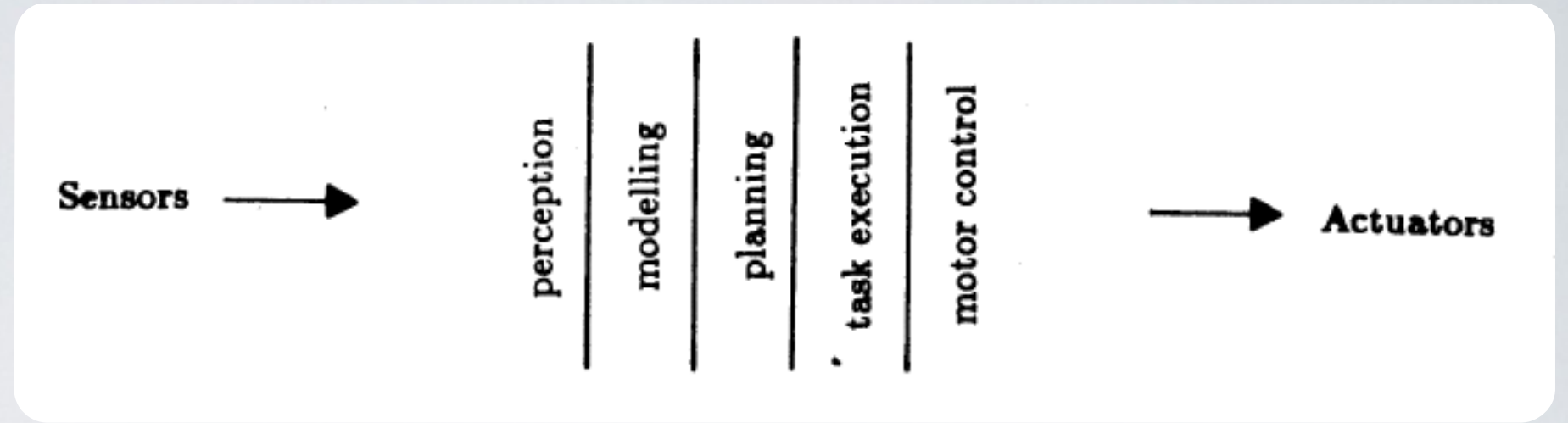
Rodney Brooks



SUBSUMPTION ARCHITECTURE



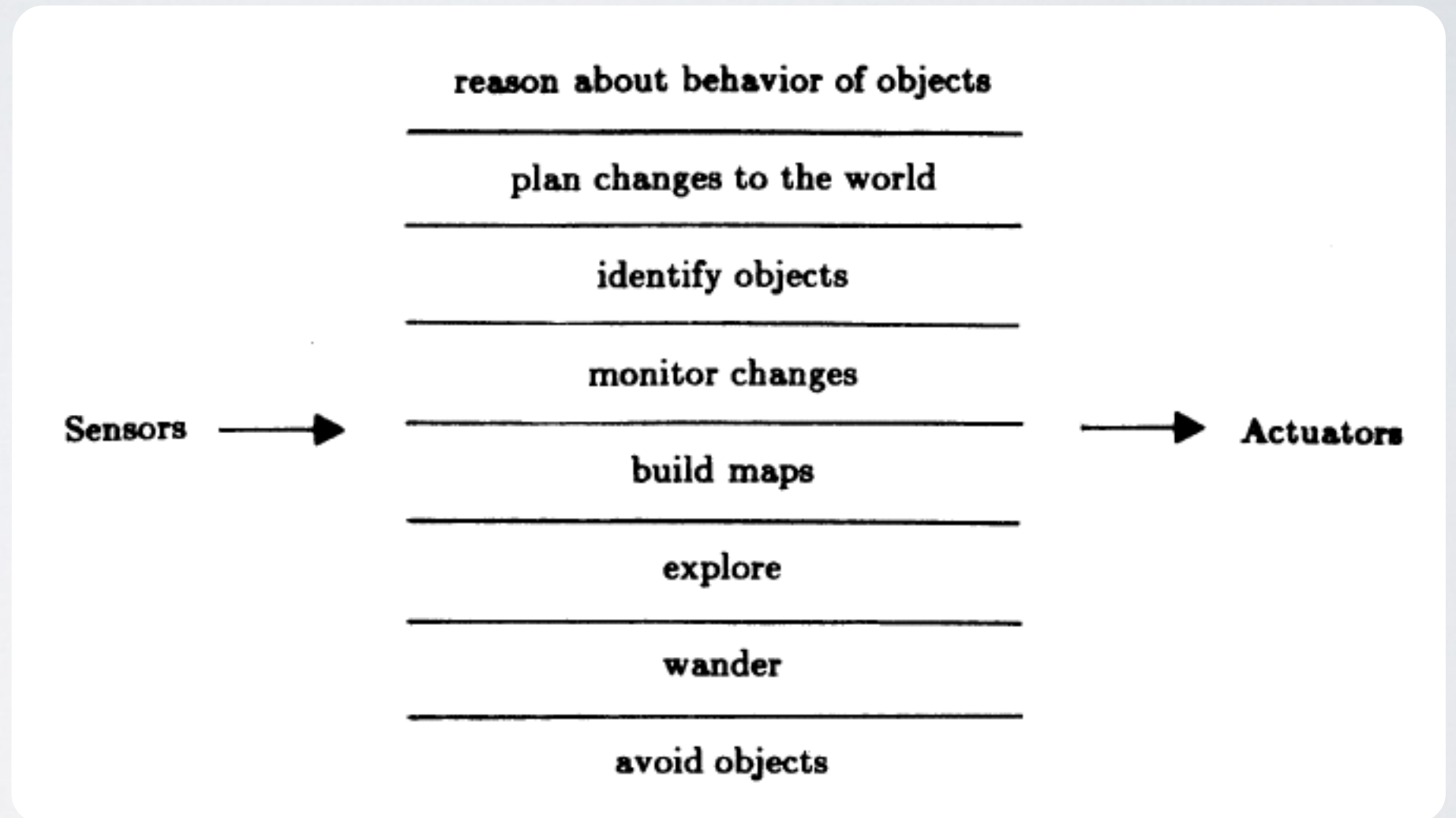
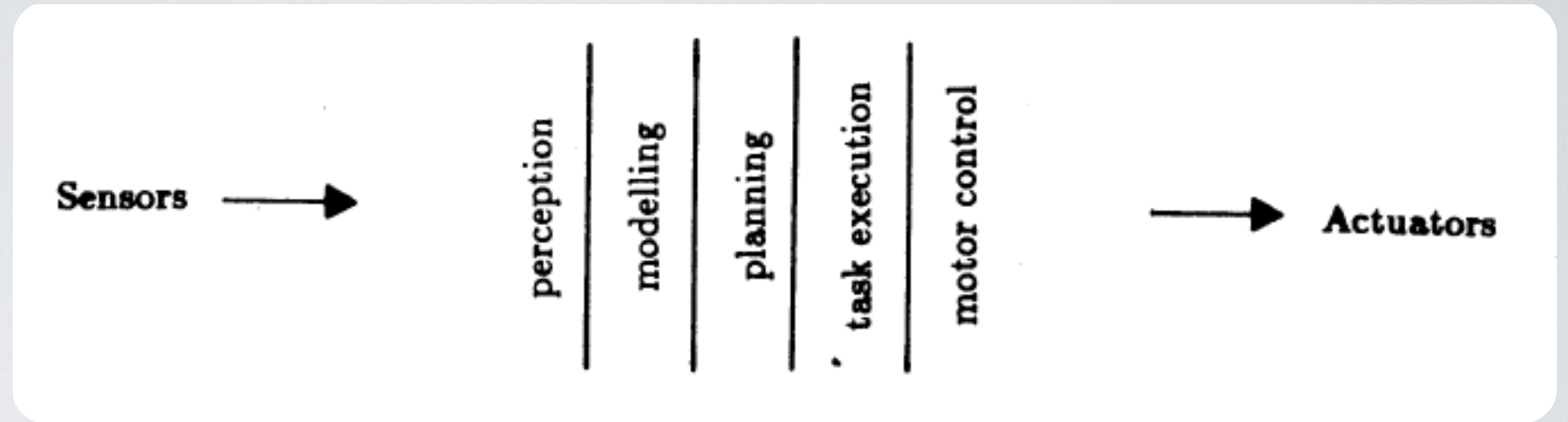
Rodney Brooks



SUBSUMPTION ARCHITECTURE



Rodney Brooks



SUBSUMPTION ARCHITECTURE

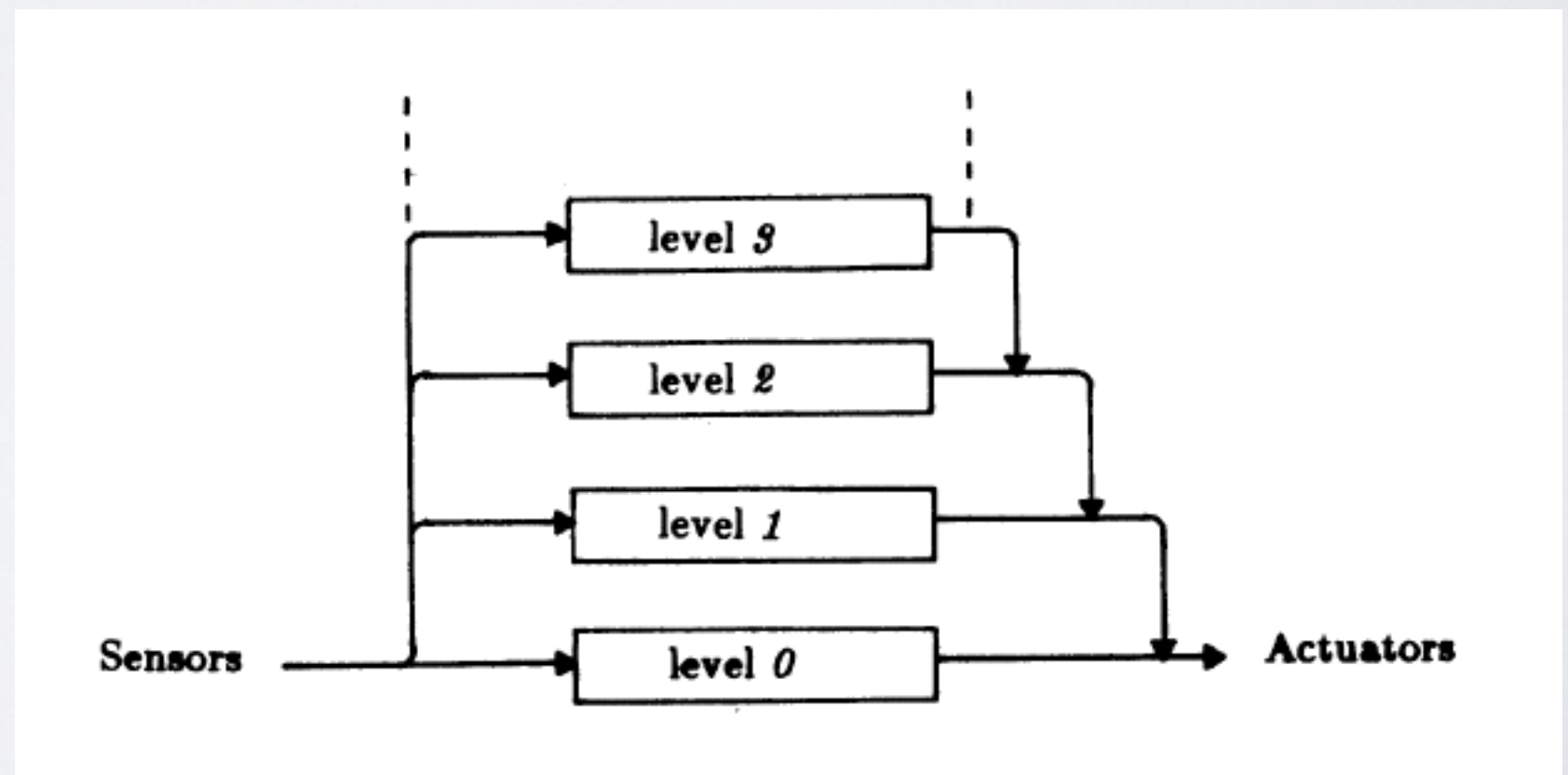
LEVELS OF COMPETENCE

- Assumptions:
 - Simple control, complex behavior
 - Relative, not absolute
 - Real world
 - Robust

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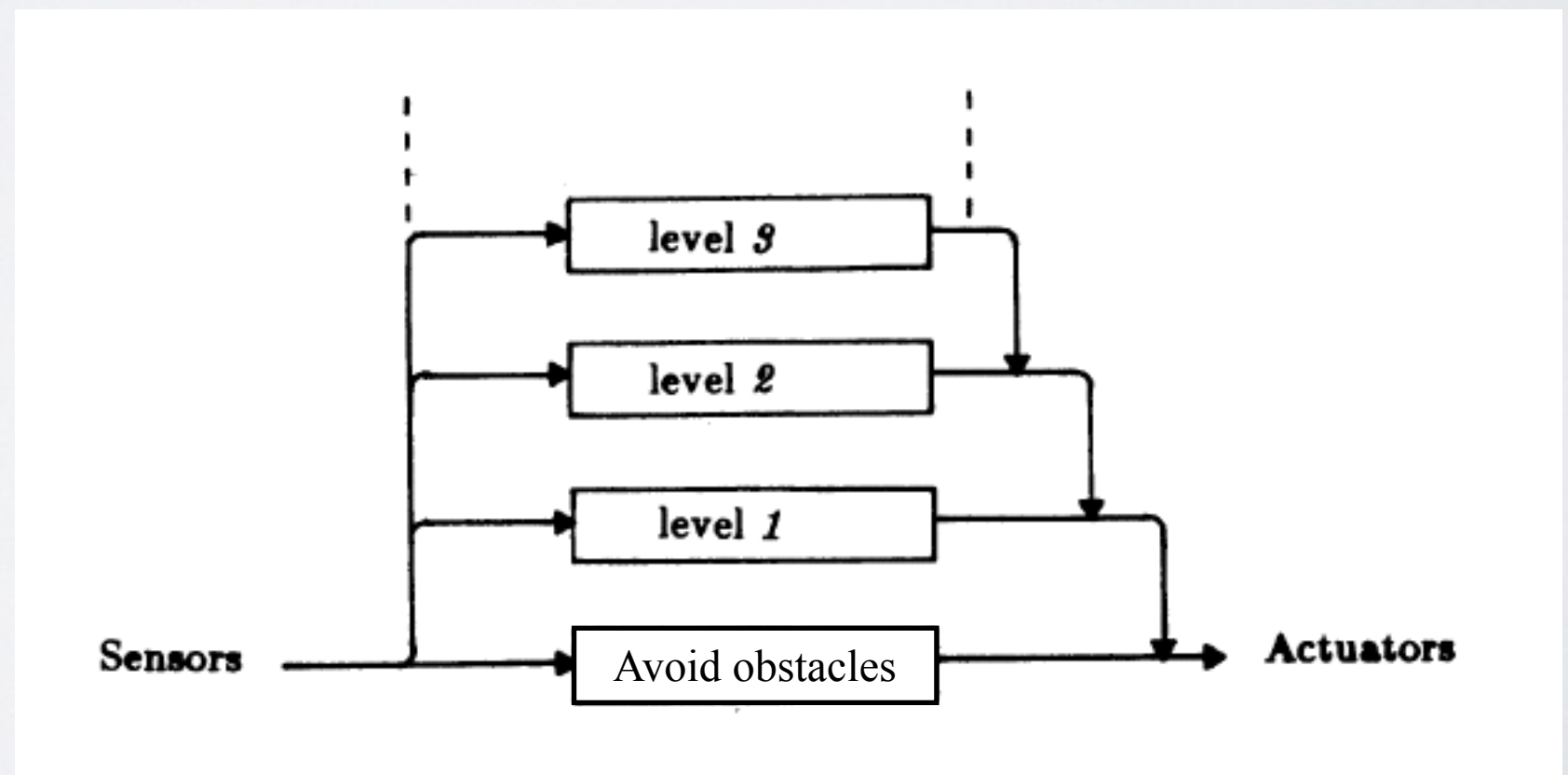
Subsumption:



LEVELS OF COMPETENCE

- Assumptions:
 - Simple control, complex behavior
 - Relative, not absolute
 - Real world
 - Robust

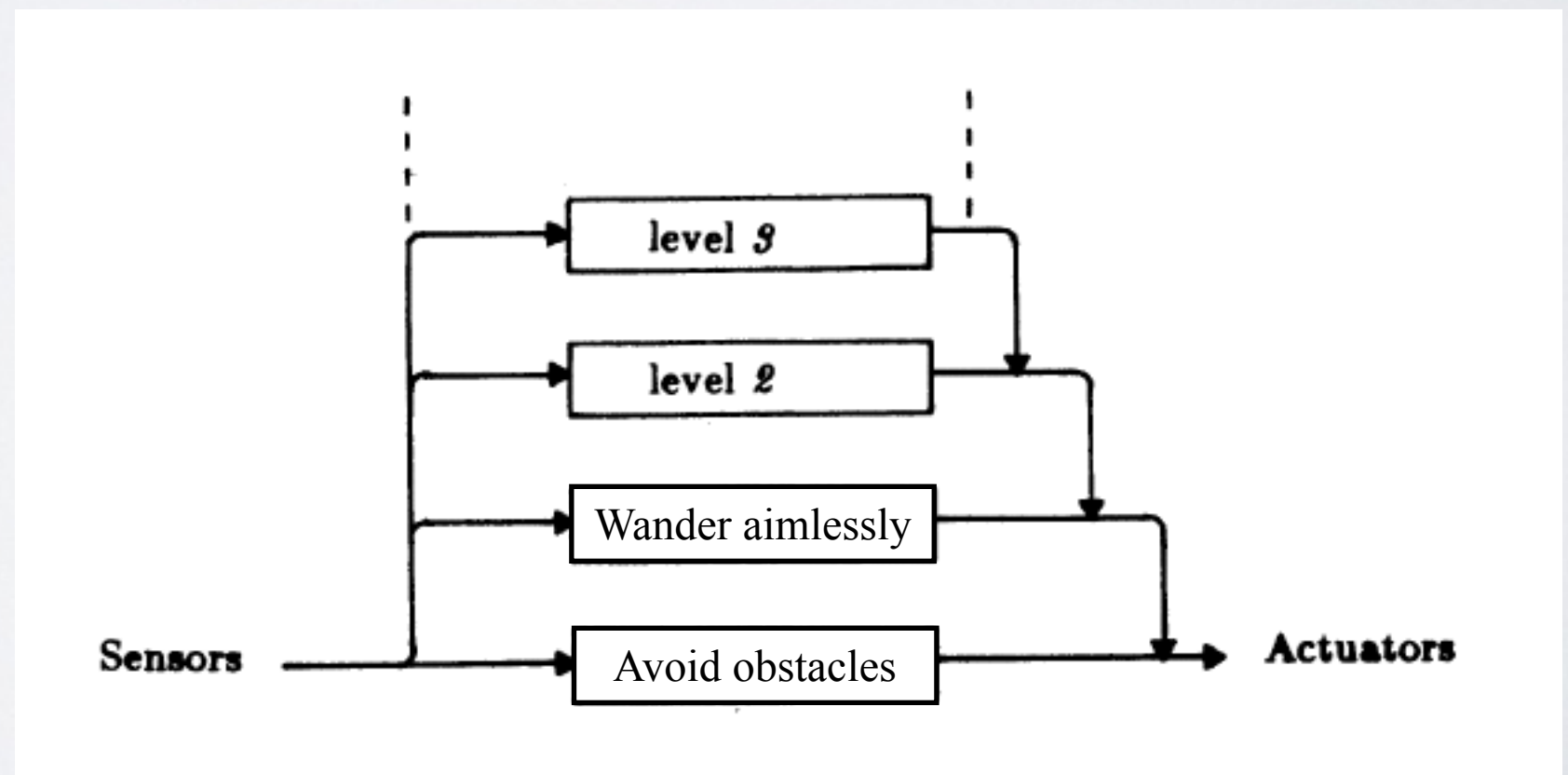
Subsumption:



LEVELS OF COMPETENCE

- Assumptions:
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Subsumption:

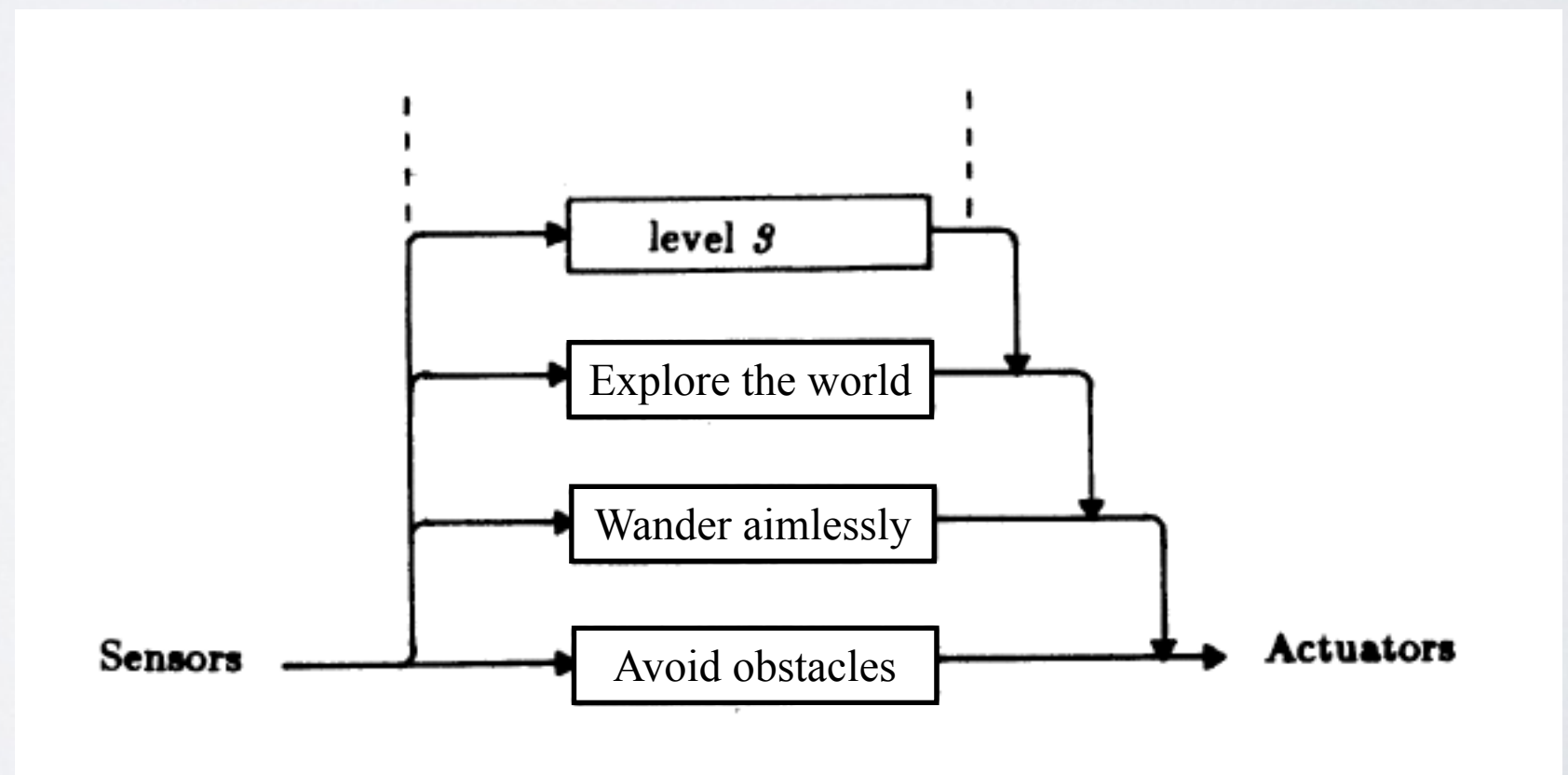


LEVELS OF COMPETENCE

- Assumptions:

- Simple control, complex behavior
- Relative, not absolute
- Real world
- Robust

Subsumption:

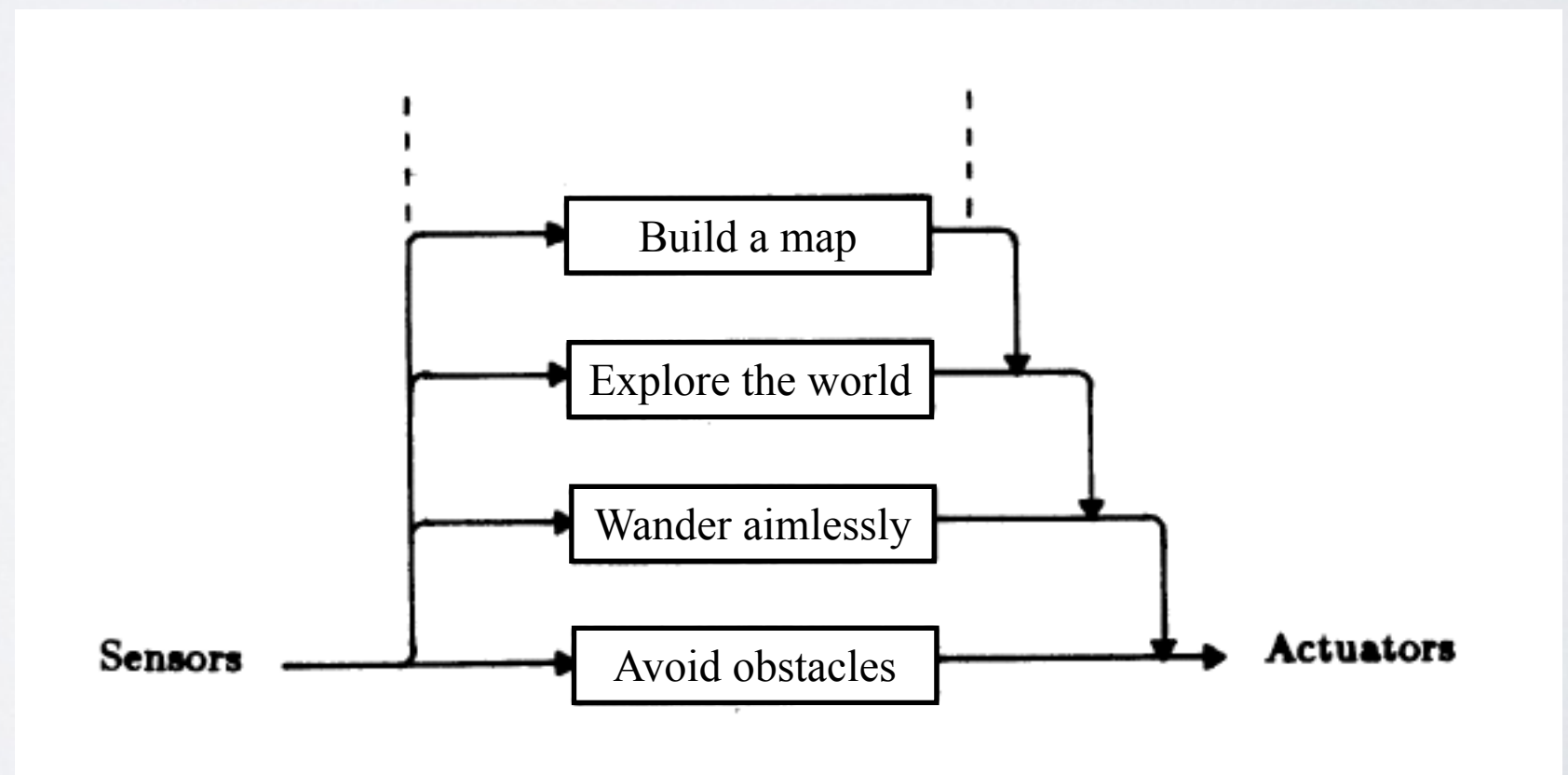


LEVELS OF COMPETENCE

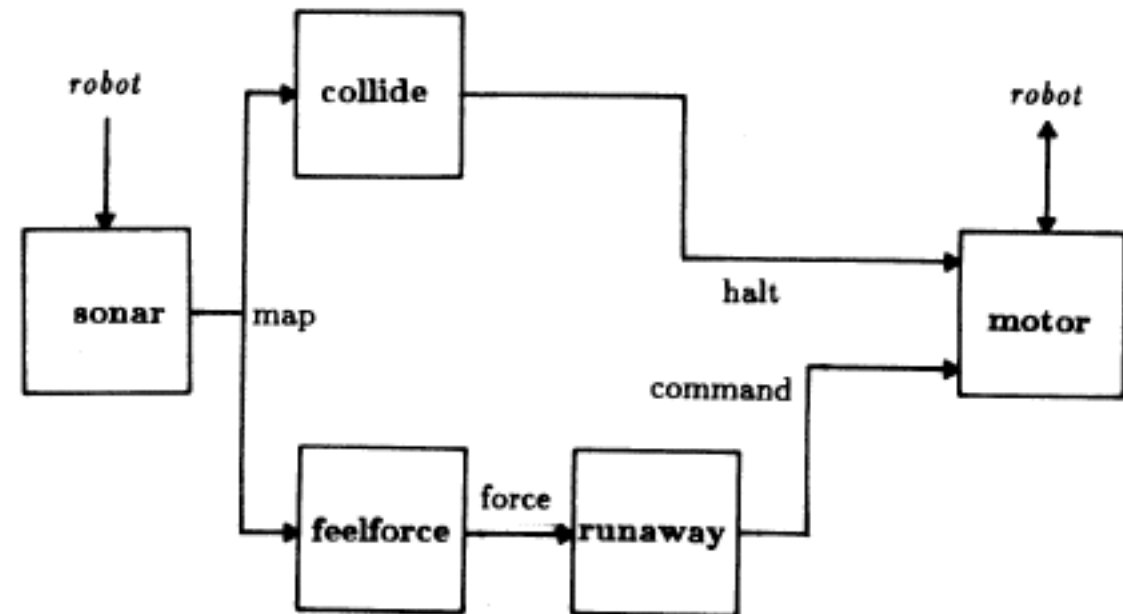
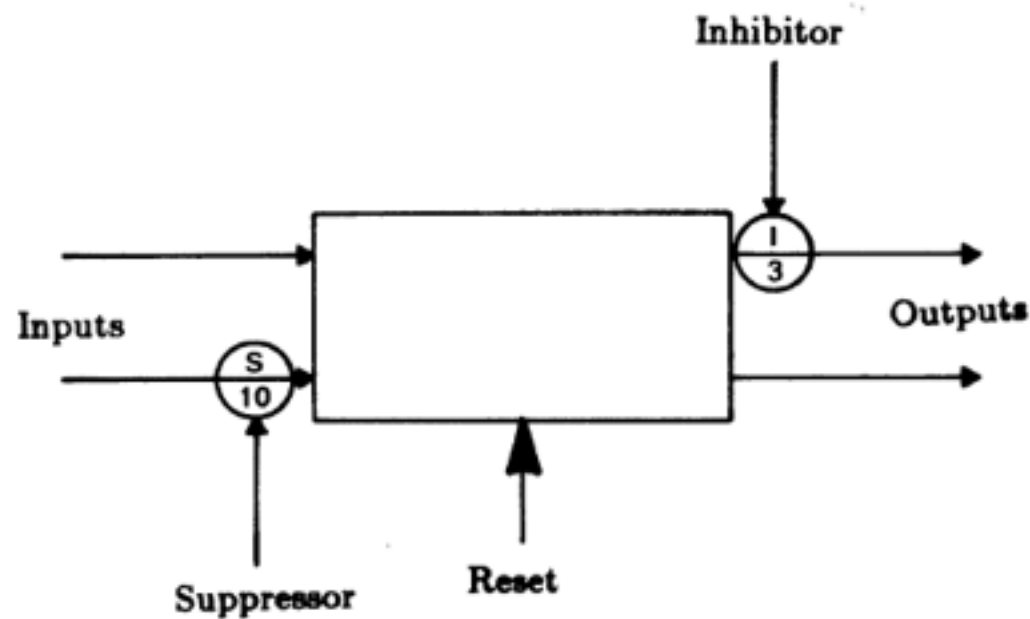
- Assumptions:

- Simple control, complex behavior
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- Real world
- Robust

Subsumption:

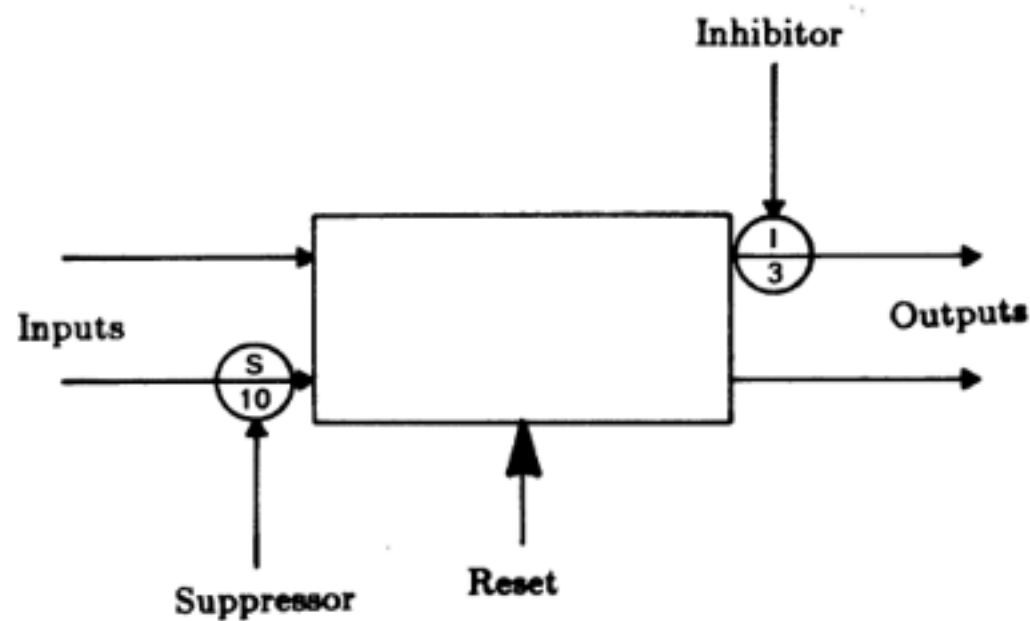


SUBSUMPTION

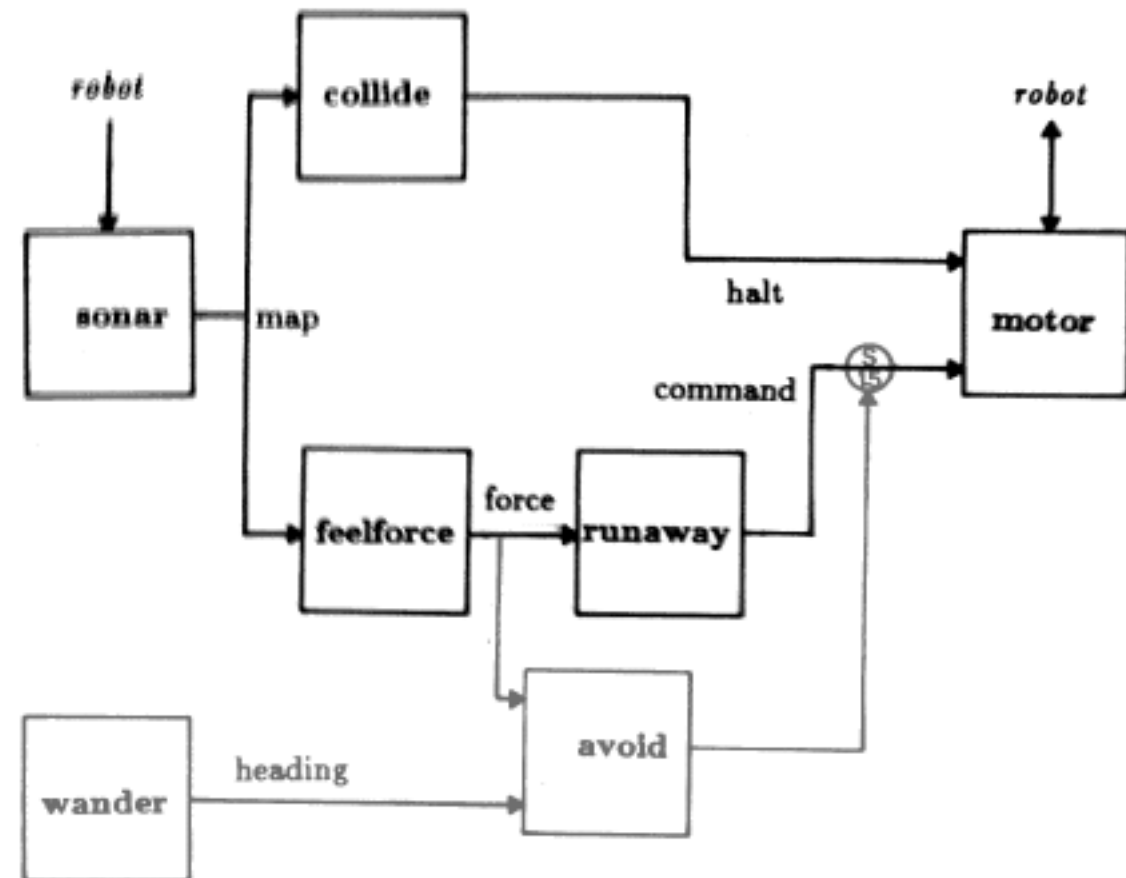


- Inputs can be suppressed
- Outputs can be inhibited

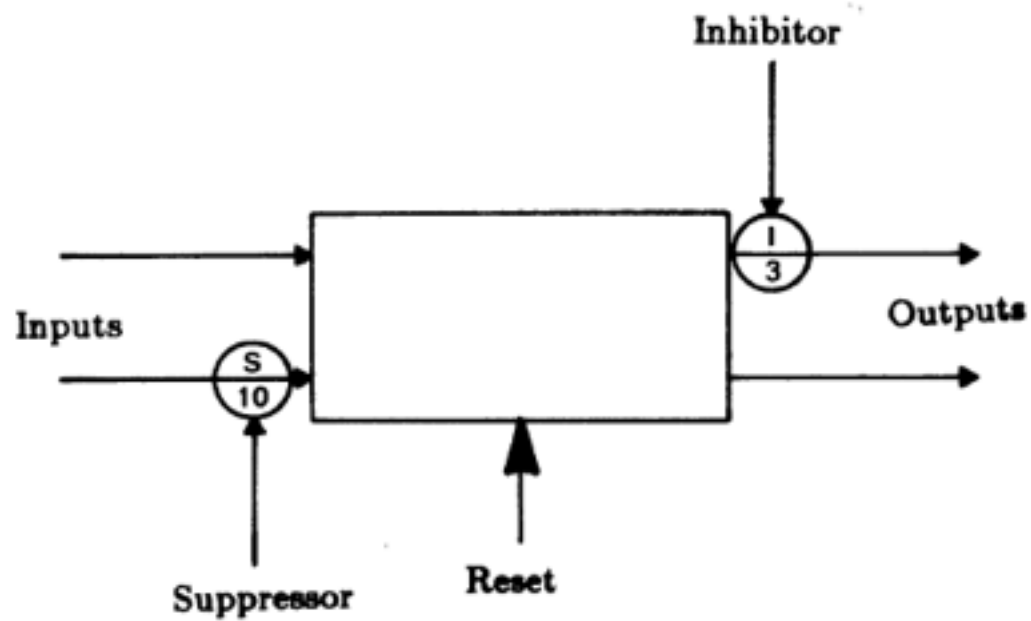
SUBSUMPTION



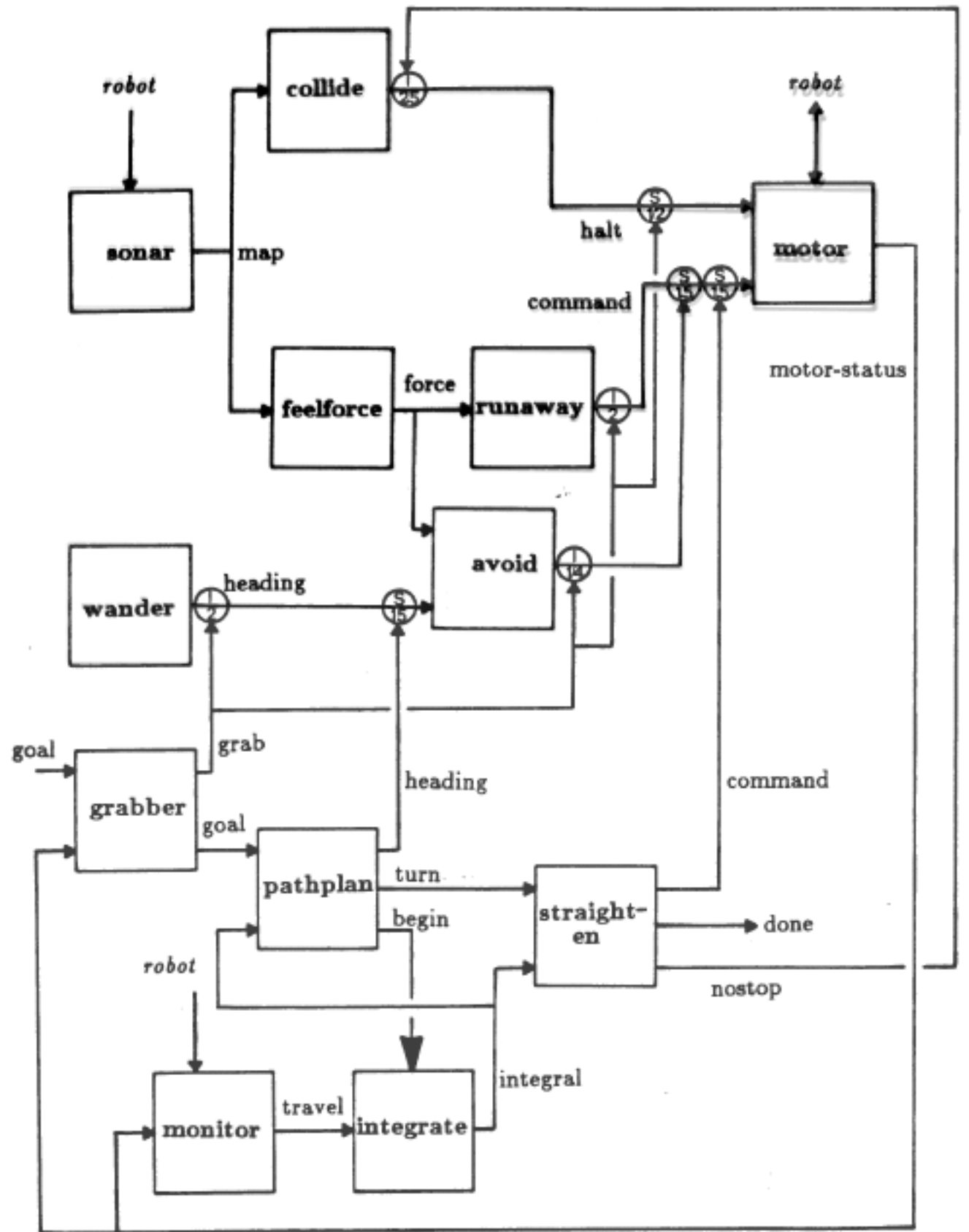
- Inputs can be suppressed
- Outputs can be inhibited



SUBSUMPTION

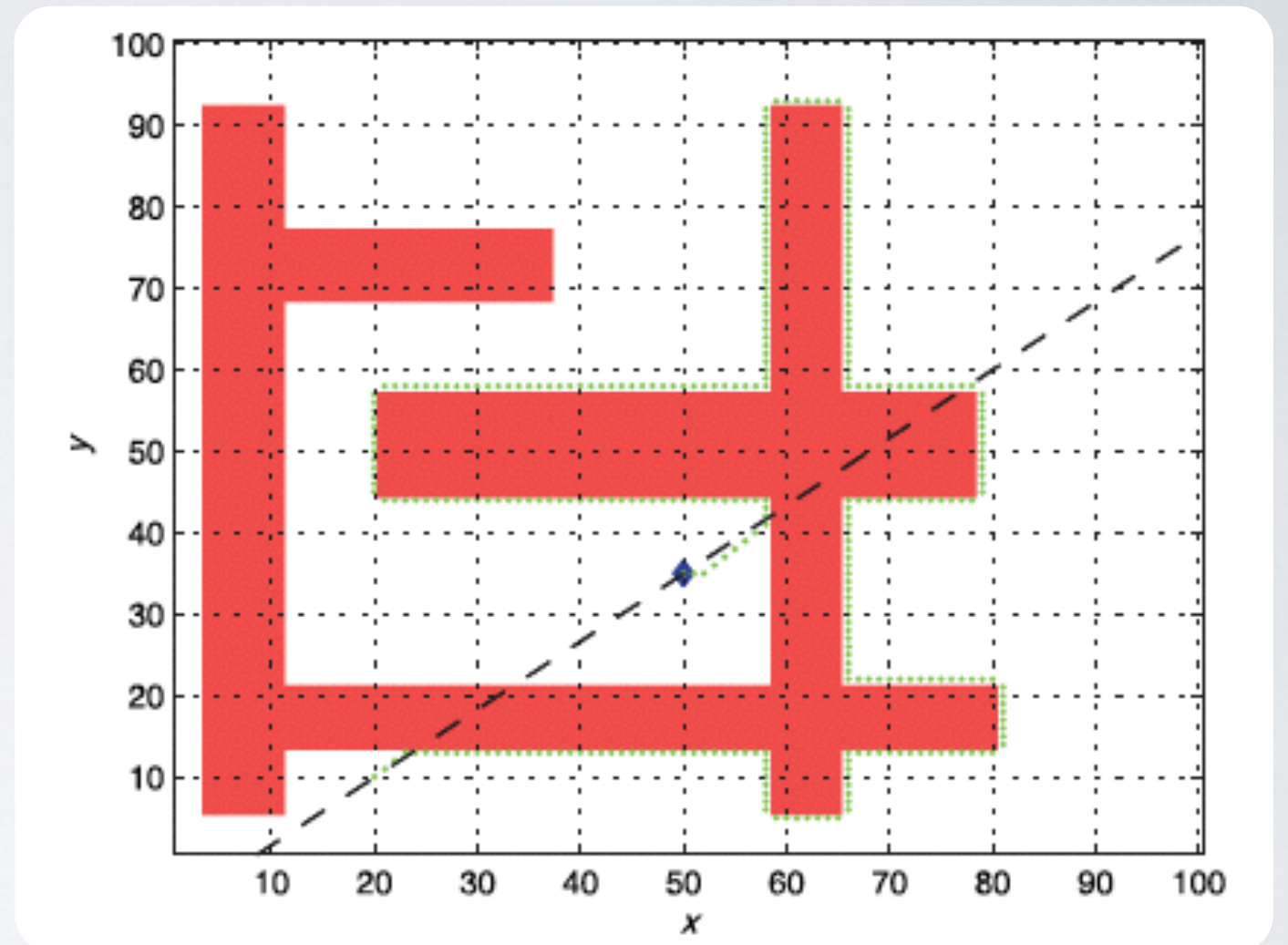


- Inputs can be suppressed
- Outputs can be inhibited



SIMPLE AUTOMATA

- Bug Algorithms
- Bug2 Demo:
 - straight line
 - go around obstacles CCW
- Suboptimal !

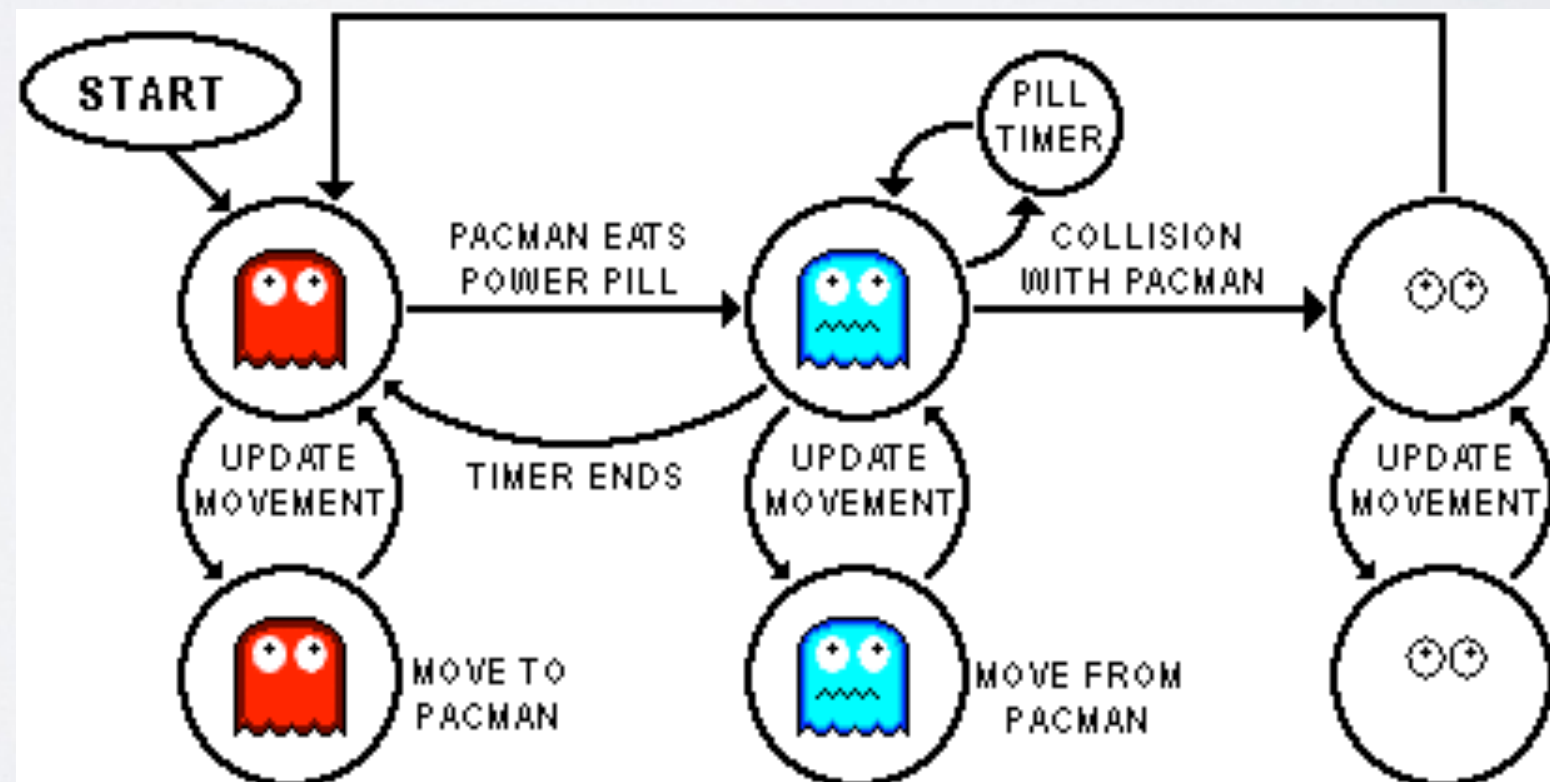


```
load map1
bug = Bug2(map);
bug.goal = [50; 35];
bug.path([20; 10]);
```

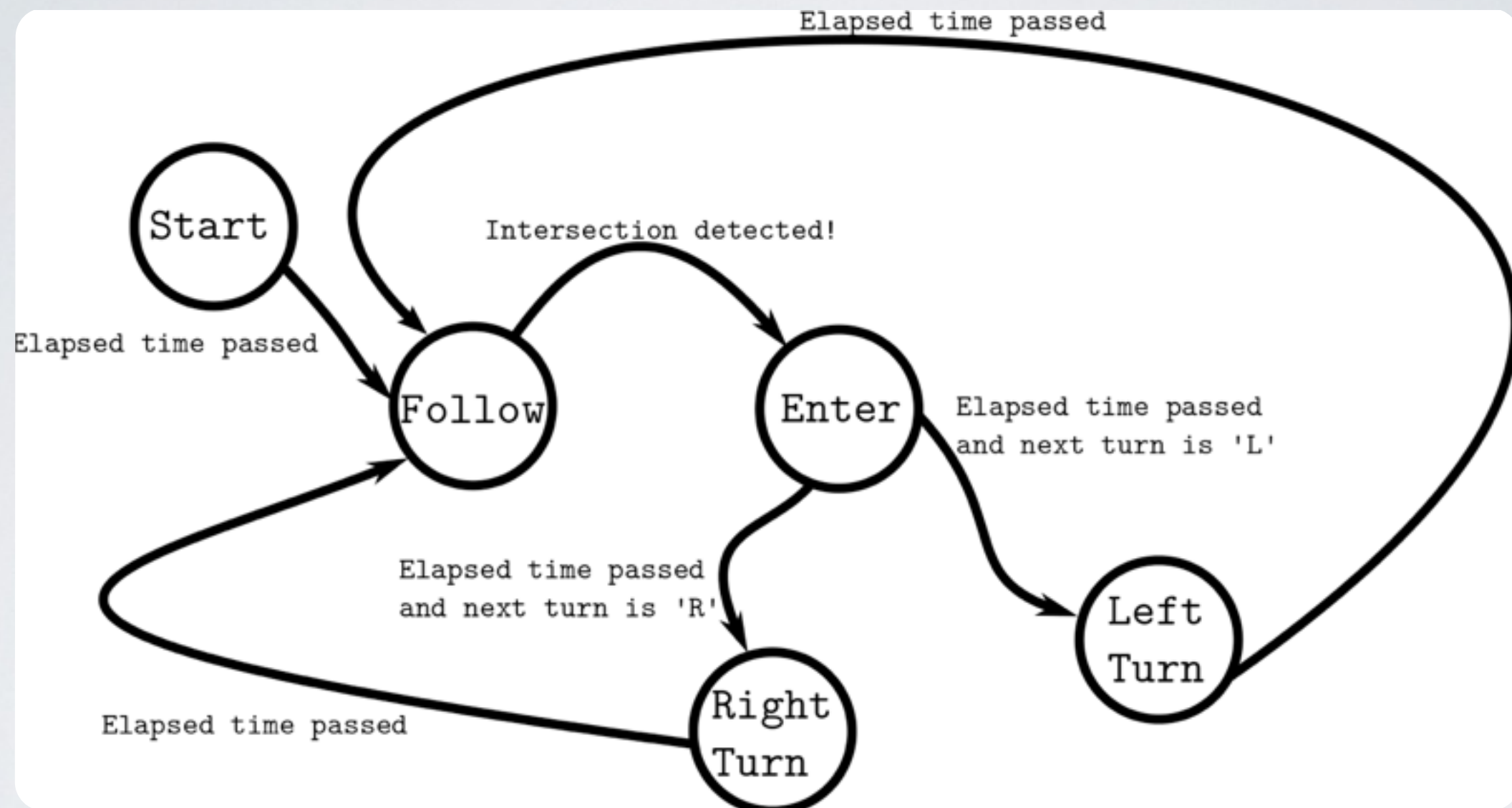
FINITE STATE MACHINES



- States
- Transitions
- Events



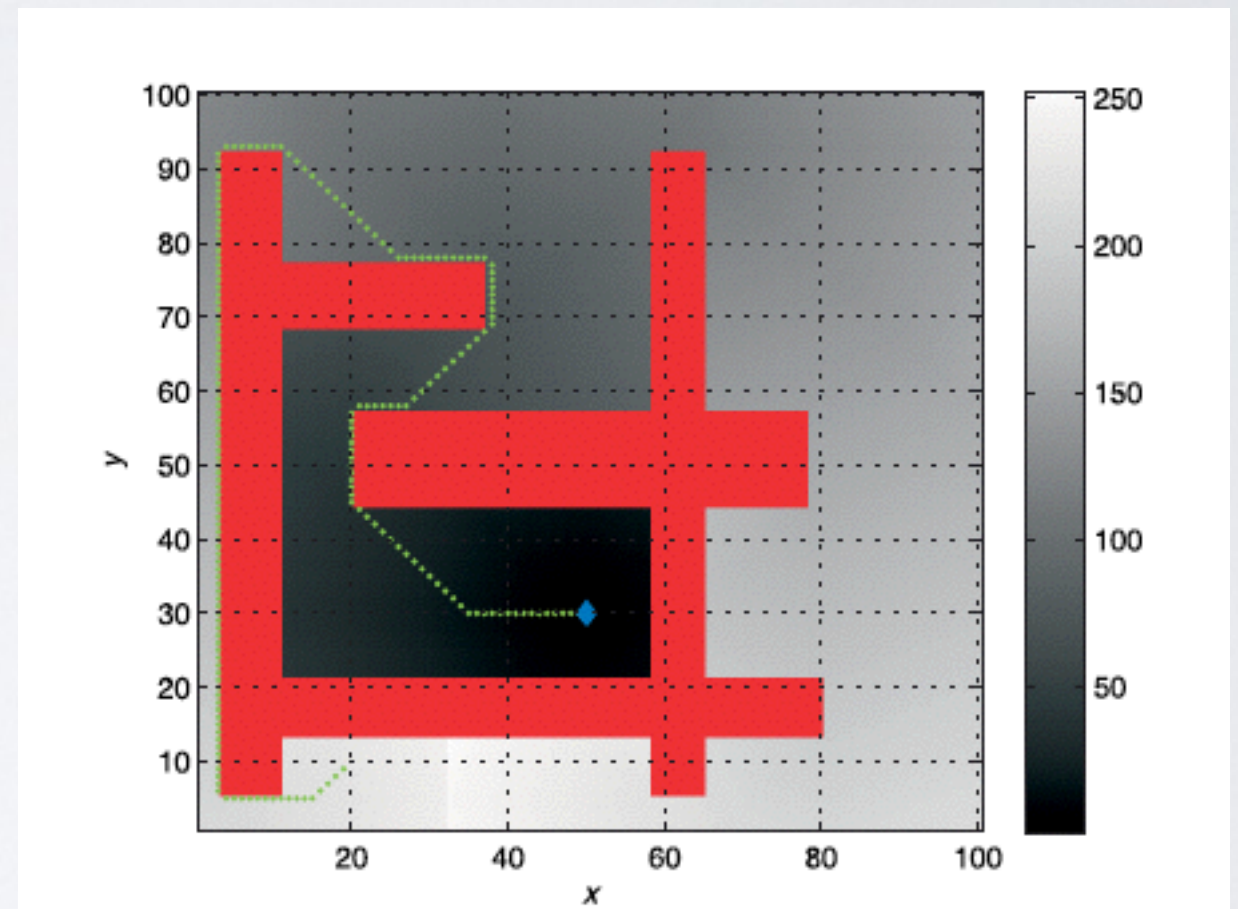
MAZE RUNNER



- Andrew Explains

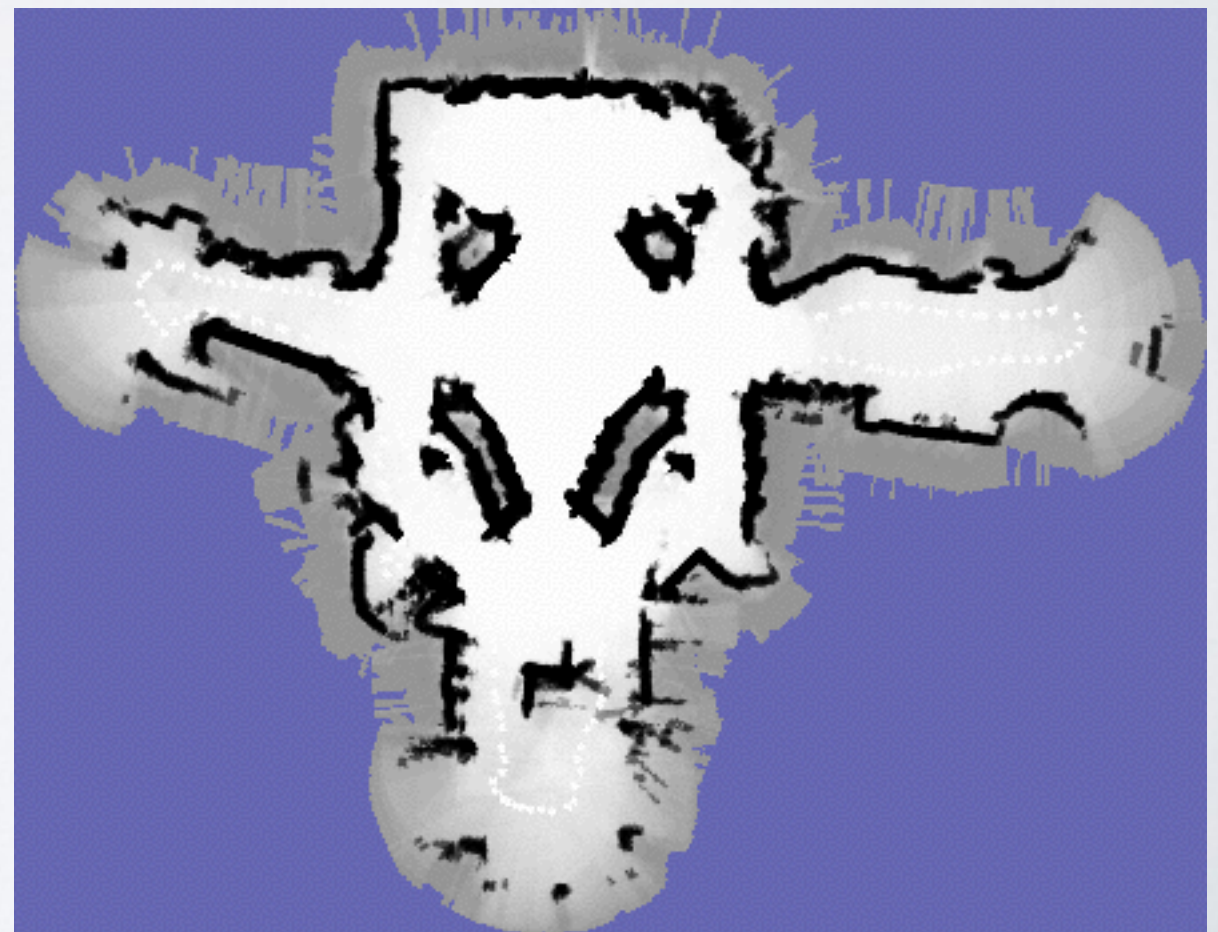
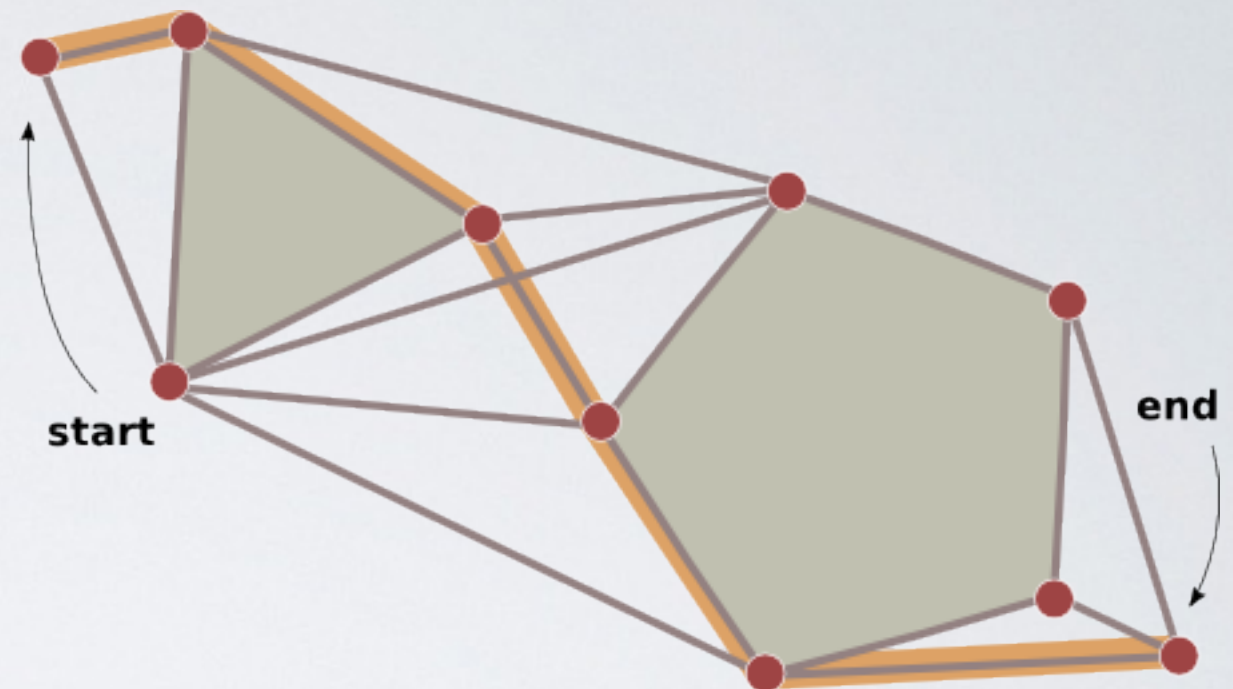
MAP-BASED PLANNING

- Maps:
 - Polygons
 - Occupancy Grid
- Shortest Path
 - Dijkstra
 - Distance Transform



MAP REPRESENTATIONS

- Polygons
 - vertices edges
 - Very compact
- Occupancy Grid
 - Memory $\sim$ area
 - Quite doable nowadays



Navigation superclass. The examples in this chapter are all based on classes derived from the `Navigation` class which is designed for 2D grid-based navigation. Each example consists of essentially the following pattern. Firstly we create an instance of an object derived from the `Navigation` class by calling the class constructor.

```
>> nav = MyNavClass(world)
```

which is passed the occupancy grid. Then a plan to reach the goal is computed

```
>> nav.plan(goal)
```

The plan can be visualized by

```
>> nav.plot()
```

and a path from an initial position to the goal is computed by

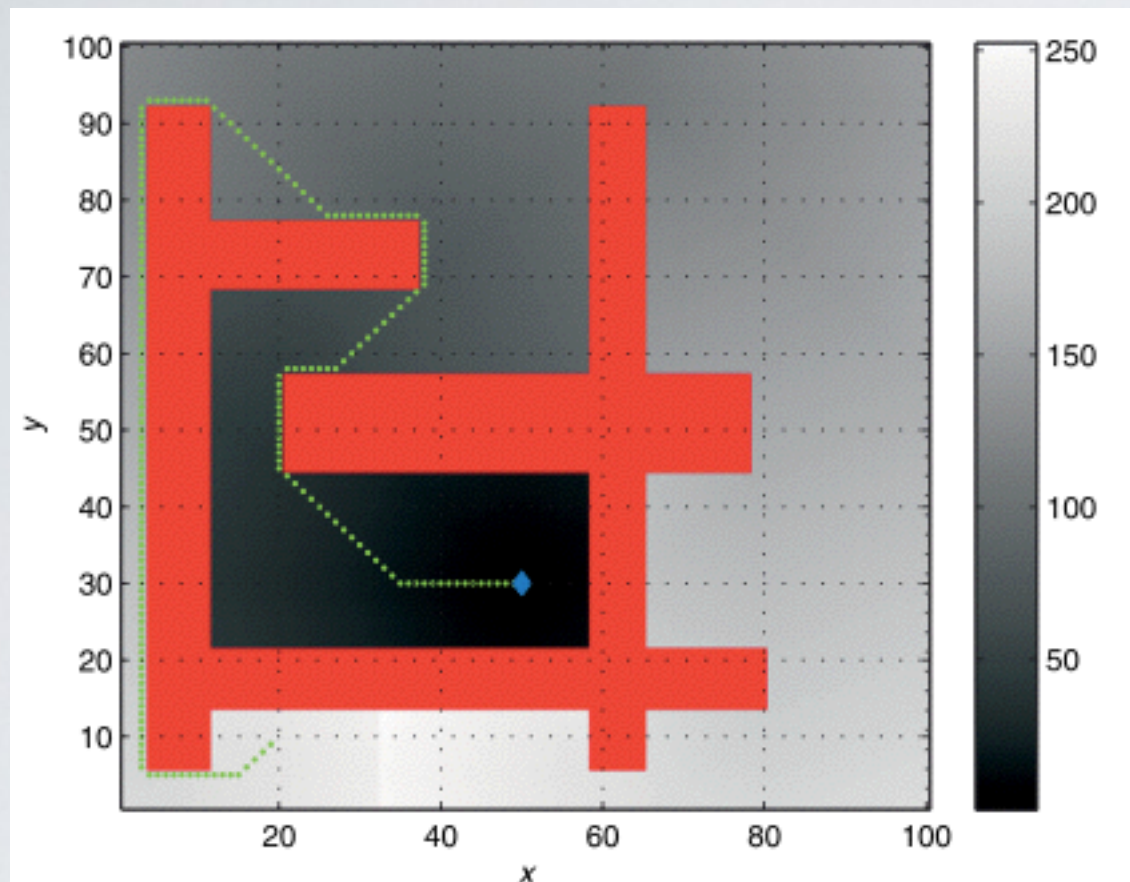
```
>> p = nav.path(start)
```

```
>> p = nav.path()
```

where `p` is the path, a sequence of points from `start` to `goal`, one row per point, and each row comprises the x- and y-coordinate. If `start` is not specified, as in the second example, the user is prompted to interactively click the start point. If no output argument is provided an animation of the robot's motion is displayed.

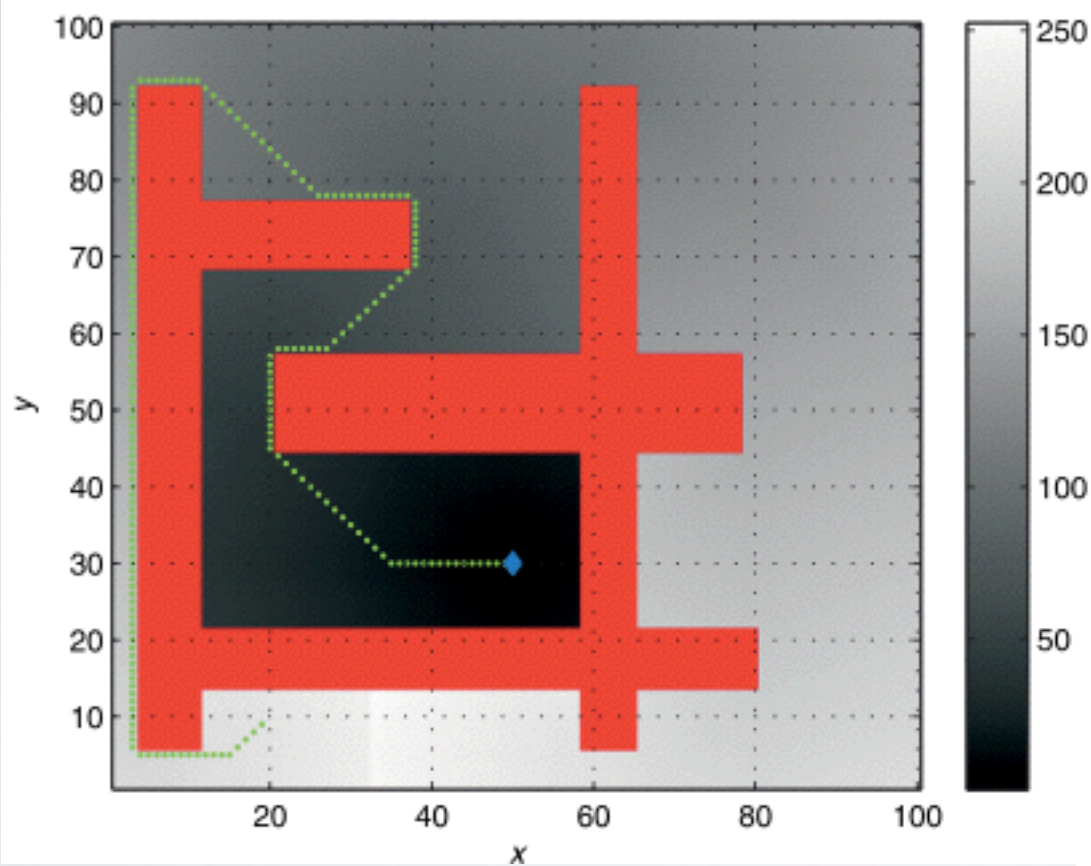
NAVIGATION RVC CLASS

DISTANCE TRANSFORM

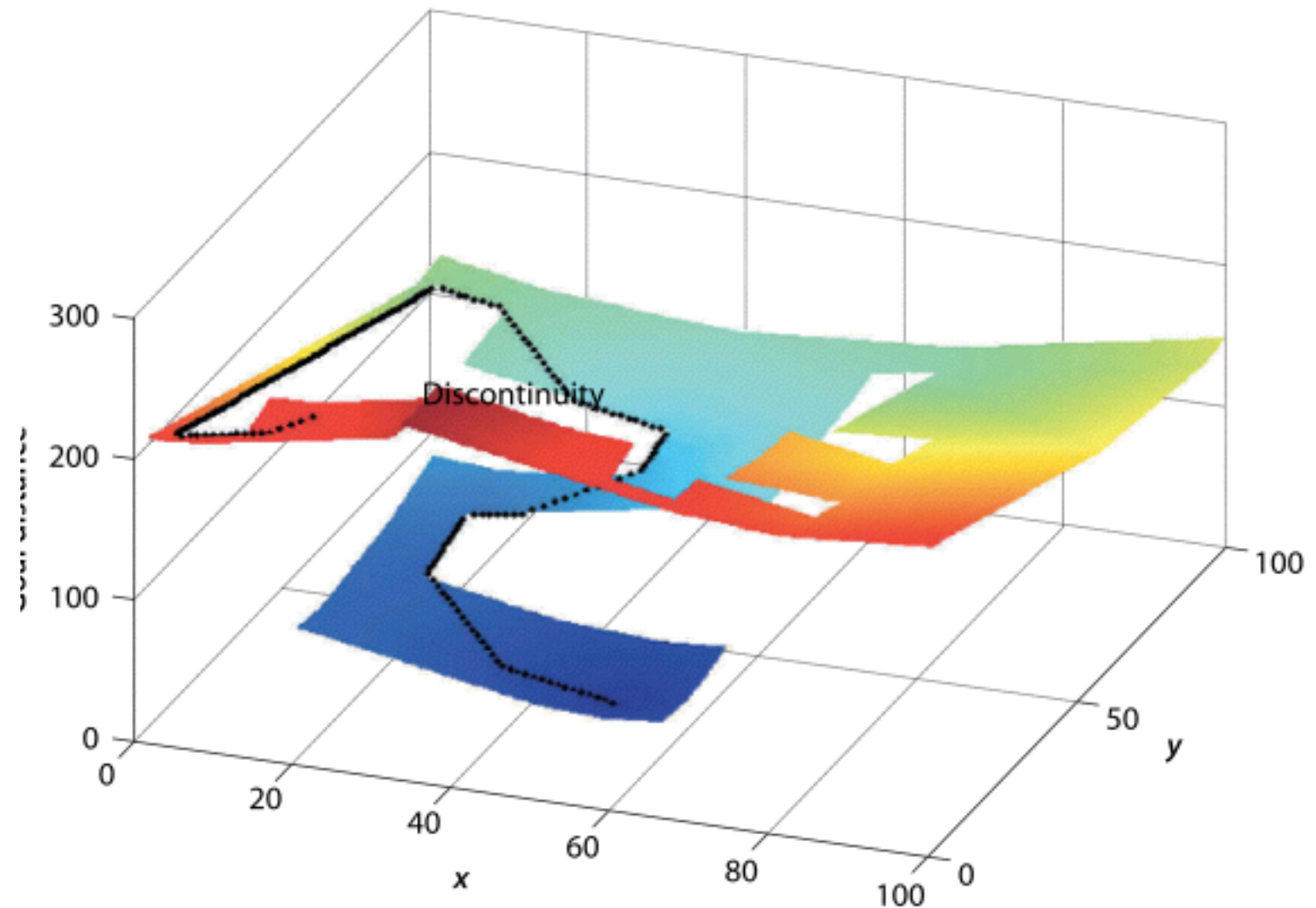


```
dx = DXform(map);  
dx.plan([50;35]);  
dx.plot();  
dx.path([20; 10]);  
dx.plan(goal, 0.1);
```

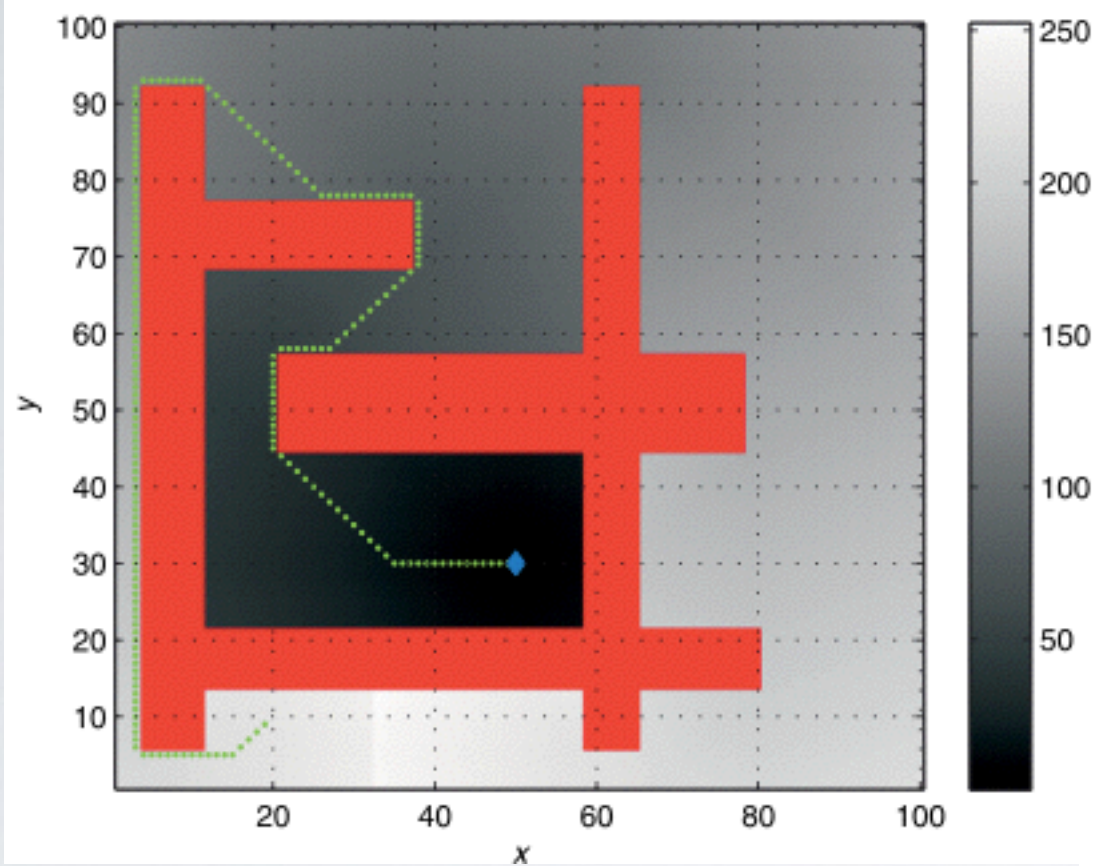
DISTANCE TRANSFORM



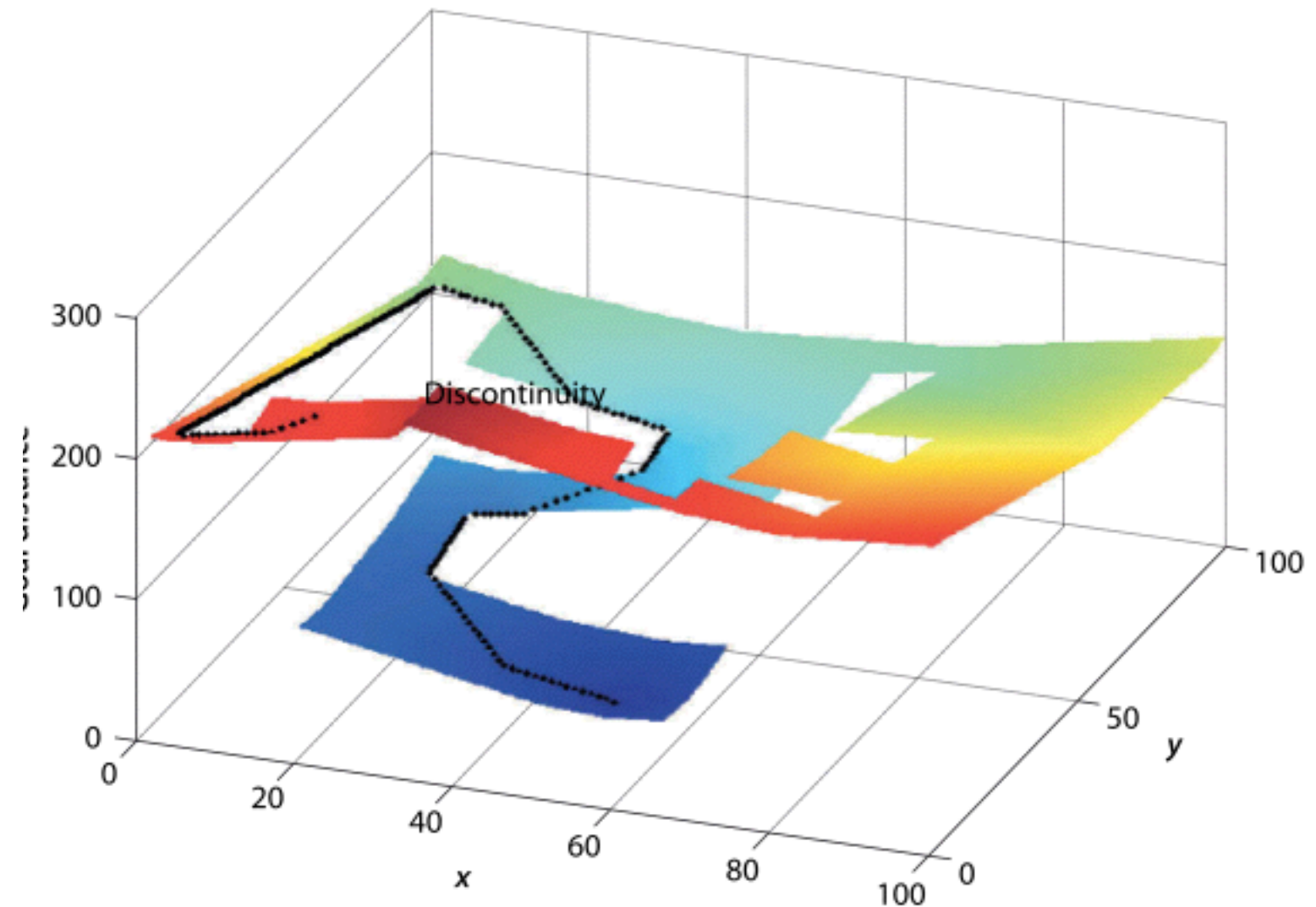
```
dx = DXform(map);  
dx.plan([50;35]);  
dx.plot();  
dx.path([20; 10]);  
dx.plan(goal, 0.1);
```



DISTANCE TRANSFORM



```
dx = DXform(map);  
dx.plan([50;35]);  
dx.plot();  
dx.path([20; 10]);  
dx.plan(goal, 0.1);
```



- Rolling downhill!

Next: excerpts from...

Real-Time Planning in Dynamic and Partially Known Domains



Maxim Likhachev
University of Pennsylvania
maximl@seas.upenn.edu



Sven Koenig
University of Southern California
skoenig@usc.edu

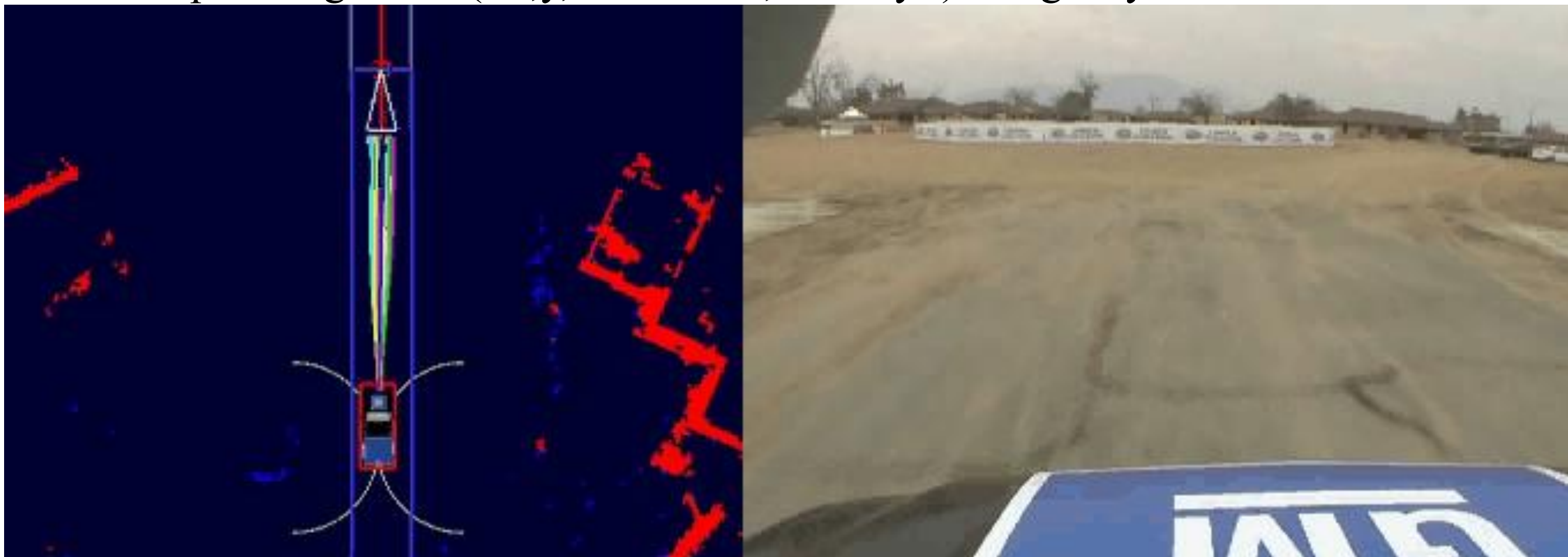
Real-time Planning in Dynamic and Partially-known Domains

Maxim

■ Challenges

- complexity/size (high-dim., expensive to compute costs, etc.)
- severe time constraints (e.g., tens of msecs to few seconds)
- robustness to uncertainties in execution, sensing, environment

planning in 4D ($\langle x, y, \text{orientation}, \text{velocity} \rangle$) using Anytime D*



part of efforts by Tartanracing team from CMU for the Urban Challenge 2007 race

$$A^* \quad f(x) = g(x) + h(x)$$

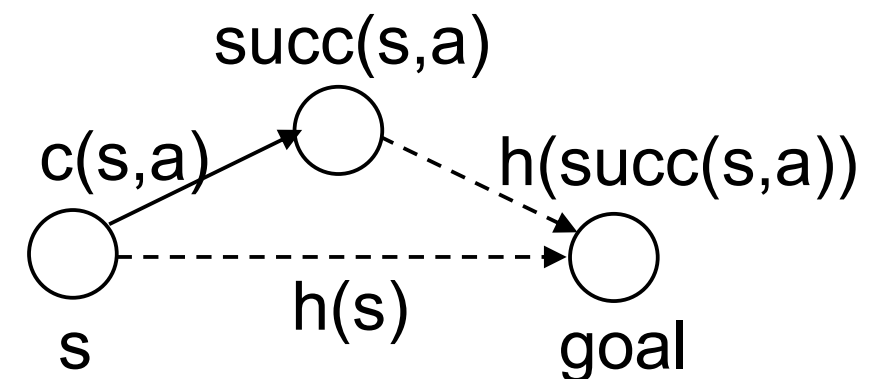
estimated = cost-so-far + heuristic est.

(Forward) A^*

1. Create a search tree that contains only the start.
2. Pick a generated but not yet expanded state s with the smallest f -value.
3. If state s is the goal then stop.
4. Expand state s .
5. Go to 2.

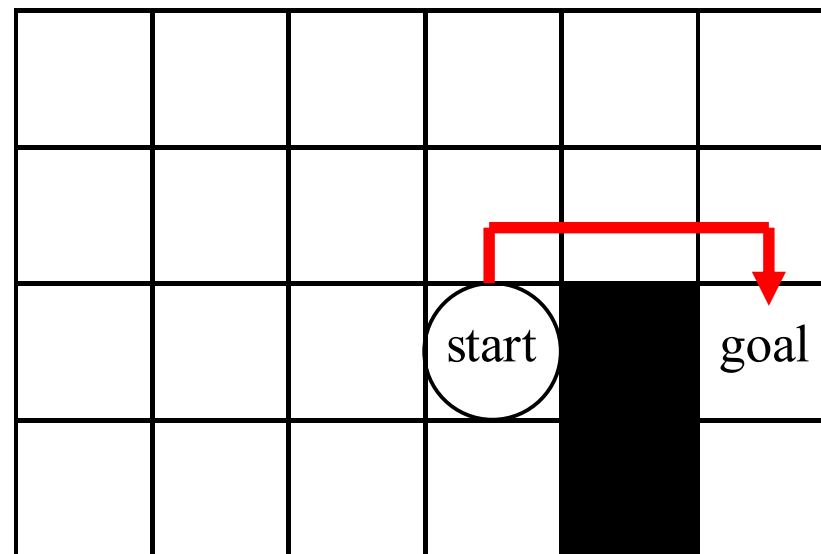
A*

- A* [Hart, Nilsson and Raphael, 1968] uses user-supplied h-values to focus its search.
- The h-values approximate the goal distances.
- We always assume that the h-values are consistent!
- The h-values $h(s)$ are consistent iff they satisfy the triangle inequality:
 $h(s) = 0$ if s is the goal and
 $h(s) \leq c(s,a) + h(\text{succ}(s,a))$ otherwise.



A^*

- Search problem with uniform cost



A*

■ Possible consistent h-values

7	6	5	4	3	2
6	5	4	3	2	1
5	4	3	2	1	0
6	5	4	3	2	1

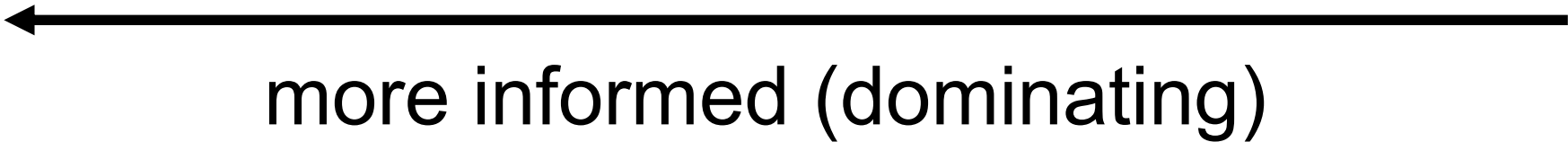
Manhattan Distance

5	4	3	2	2	2
5	4	3	2	1	1
5	4	3	2	1	0
5	4	3	2	1	1

Octile Distance

0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0

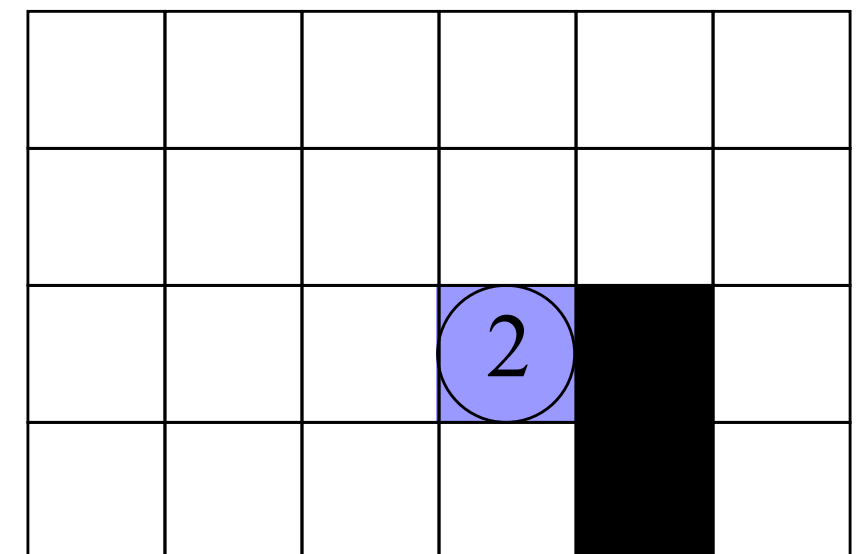
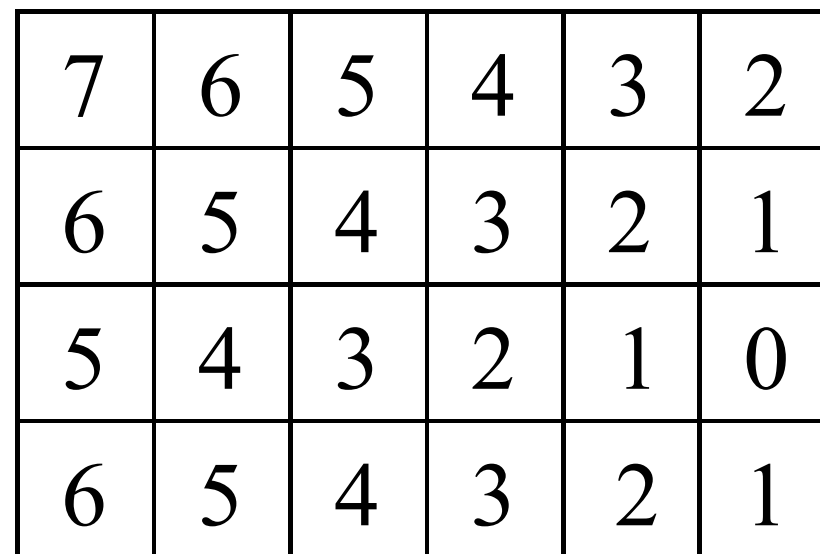
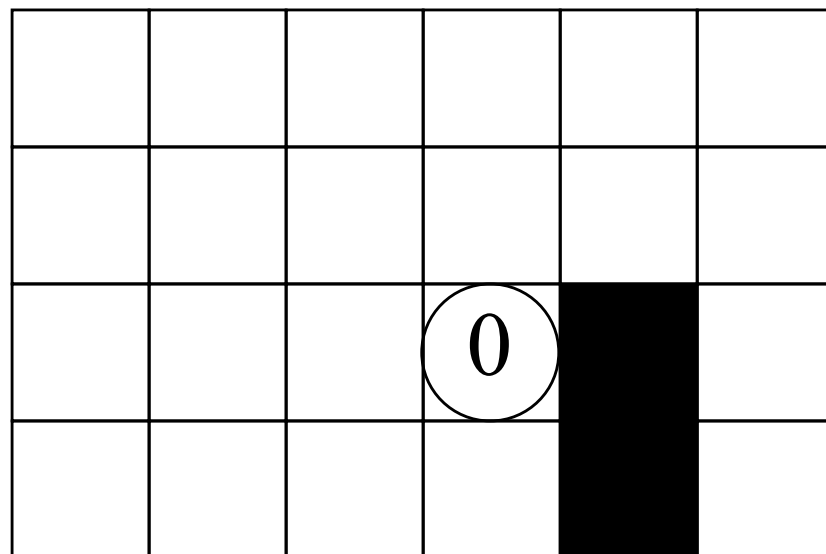
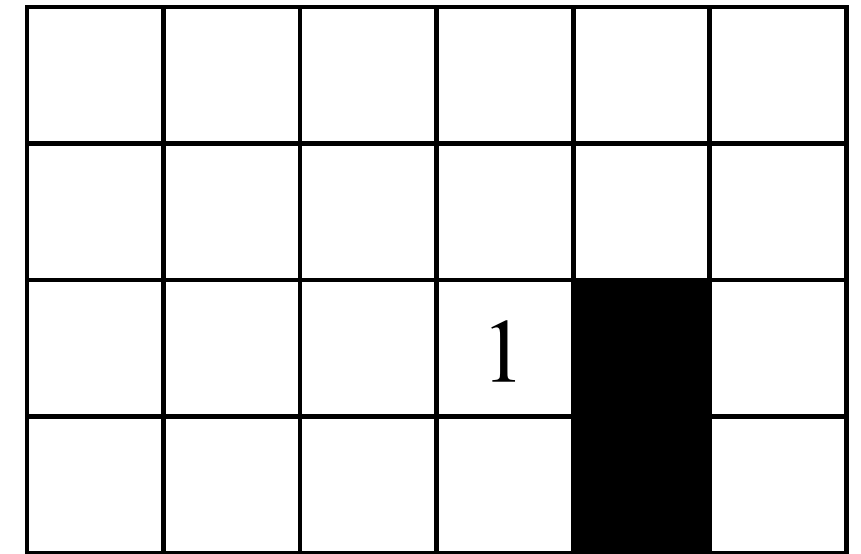
Zero h-values



A^*

■ First iteration of A^*

order of expansions



g-values

+

h-values

=

f-values

cost of the shortest path
in the search tree from the
start to the given state



generated but not expanded state (OPEN list)



expanded state (CLOSED list)

4-neighbor grid

A^*

■ Second iteration of A^*

order of expansions

			1		
			2		

			1		
		1	0		
			1		

7	6	5	4	3	2
6	5	4	3	2	1
5	4	3	2	1	0
6	5	4	3	2	1

			4		
		4	2		
			4		

g-values

+

h-values

=

f-values

cost of the shortest path
in the search tree from the
start to the given state



generated but not expanded state (OPEN list)



expanded state (CLOSED list)

4-neighbor grid

A^*

■ Third iteration of A^*

order of expansions

		3	1		
			2		

			1		
		1	0		
		2	1		

7	6	5	4	3	2
6	5	4	3	2	1
5	4	3	2	1	0
6	5	4	3	2	1

			4		
		4	2		
		6	4		

g-values

+

h-values

=

f-values

cost of the shortest path
in the search tree from the
start to the given state



generated but not expanded state (OPEN list)



expanded state (CLOSED list)

4-neighbor grid

A^*

■ Fourth iteration of A^*

order of expansions

			4		
		3	1		
			2		

		2	1		
	2	1	0		
		2	1		

7	6	5	4	3	2
6	5	4	3	2	1
5	4	3	2	1	0
6	5	4	3	2	1

		6	4		
	6	4	2		
		6	4		

g-values

+

h-values

=

f-values

cost of the shortest path
in the search tree from the
start to the given state



generated but not expanded state (OPEN list)



expanded state (CLOSED list)

4-neighbor grid

A^*

■ Fifth iteration of A^*

order of expansions

			4	5	
		3	1		
			2		

			2		
		2	1	2	
	2	1	0		
		2	1		

7	6	5	4	3	2
6	5	4	3	2	1
5	4	3	2	1	0
6	5	4	3	2	1

			6		
		6	4	4	
	6	4	2		
		6	4		

g-values

+

h-values

=

f-values

cost of the shortest path
in the search tree from the
start to the given state



generated but not expanded state (OPEN list)



expanded state (CLOSED list)

4-neighbor grid

A^*

■ Sixth iteration of A^*

order of expansions

			4	5	6
		3	1		
			2		

			2	3	
		2	1	2	3
	2	1	0		
		2	1		

7	6	5	4	3	2
6	5	4	3	2	1
5	4	3	2	1	0
6	5	4	3	2	1

			6	6	
		6	4	4	4
	6	4	2		
		6	4		

g-values

+

h-values

=

f-values

cost of the shortest path
in the search tree from the
start to the given state



generated but not expanded state (OPEN list)



expanded state (CLOSED list)

4-neighbor grid

A^*

- Seventh and last iteration of A^*

order of expansions

			4	5	6
		3	1		(7)
			2		

			2	3	4
		2	1	2	3
	2	1	0		4
		2	1		

7	6	5	4	3	2
6	5	4	3	2	1
5	4	3	2	1	0
6	5	4	3	2	1

			6	6	6
		6	4	4	4
	6	4	2		(4)
		6	4		

g-values

+

h-values

=

f-values

cost of the shortest path
in the search tree from the
start to the given state



generated but not expanded state (OPEN list)



expanded state (CLOSED list)

4-neighbor grid

A*

7	6	5	4	3	2
6	5	4	3	2	1
5	4	3	2	1	0
6	5	4	3	2	1

5	4	3	2	2	2
5	4	3	2	1	1
5	4	3	2	1	0
5	4	3	2	1	1

Uniform-cost search
Breadth-first search

0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0

Manhattan Distance

Octile Distance

Zero h-values

			4	5	6
		3	1		(7)
			2		

			6		
			3	4	7
		5	1		(8)
			2		

	18	13	8	14	19
17	12	7	4	9	15
11	6	3	1		(20)
16	10	5	2		



more informed (dominating)

4-neighbor grid

Incremental Heuristic Search

search task 1	slightly different search task 2	slightly different search task 3
---------------	-------------------------------------	-------------------------------------

Incremental Heuristic Search

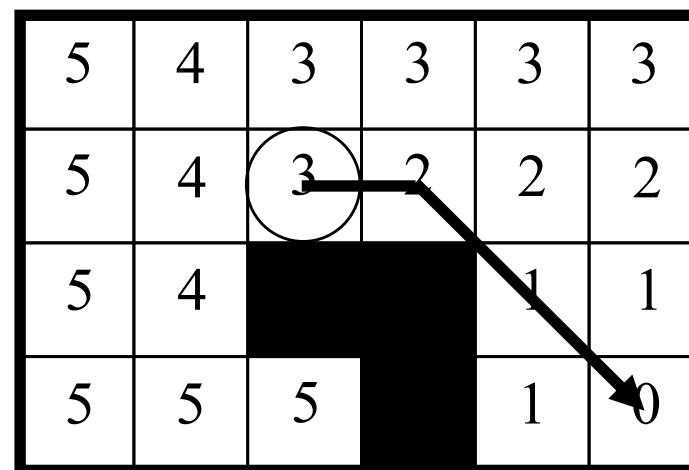
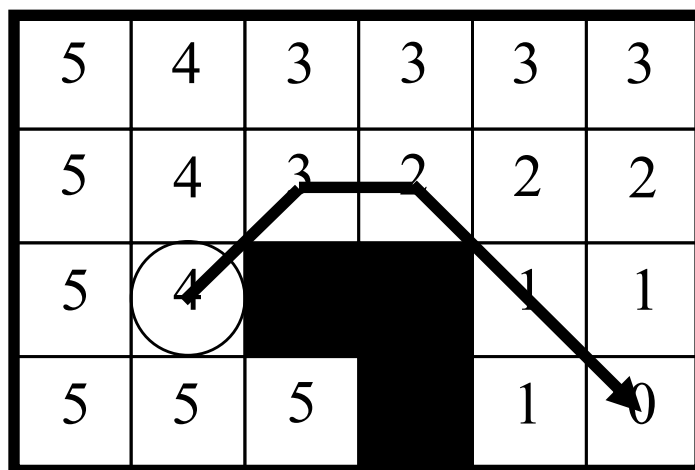
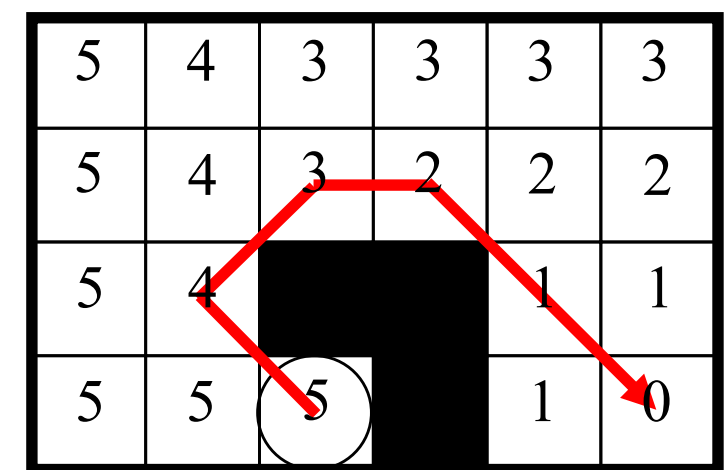
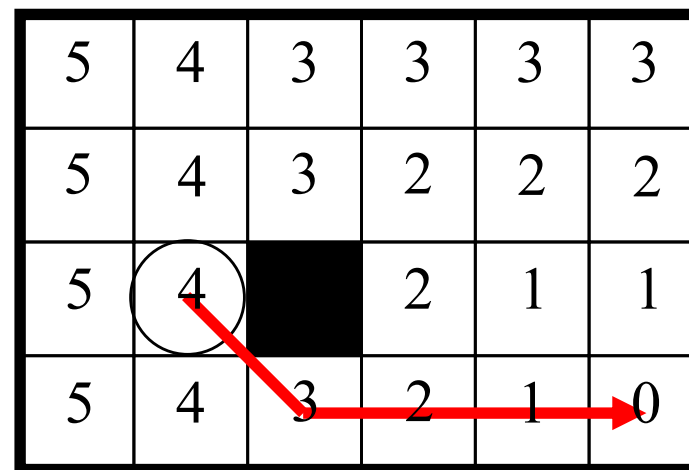
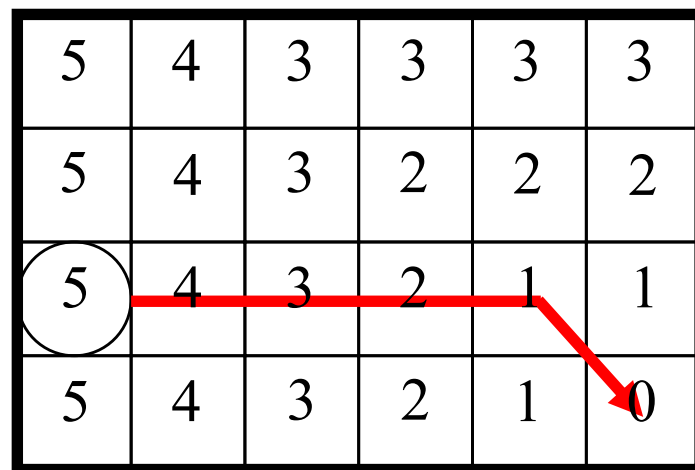
- Incremental heuristic search speeds up A^* searches for a sequence of similar search problems by exploiting experience with earlier search problems in the sequence. It finds shortest paths.
- In the worst case, incremental heuristic search cannot be more efficient than A^* searches from scratch
[Nebel and Koehler 1995].

Incremental Heuristic Search

- Fringe Saving A* (FSA*)
- Adaptive A* (AA*)
- Lifelong Planning A* (LPA*), D* Lite and Minimax LPA*
- Comparison of D* Lite and Adaptive A*
- Eager and Lazy Moving-Target Adaptive A* (MTAA*)
- Anytime Replanning A* (ARA*)
- Anytime D*

D* Lite

goal
distance



...

D* Lite

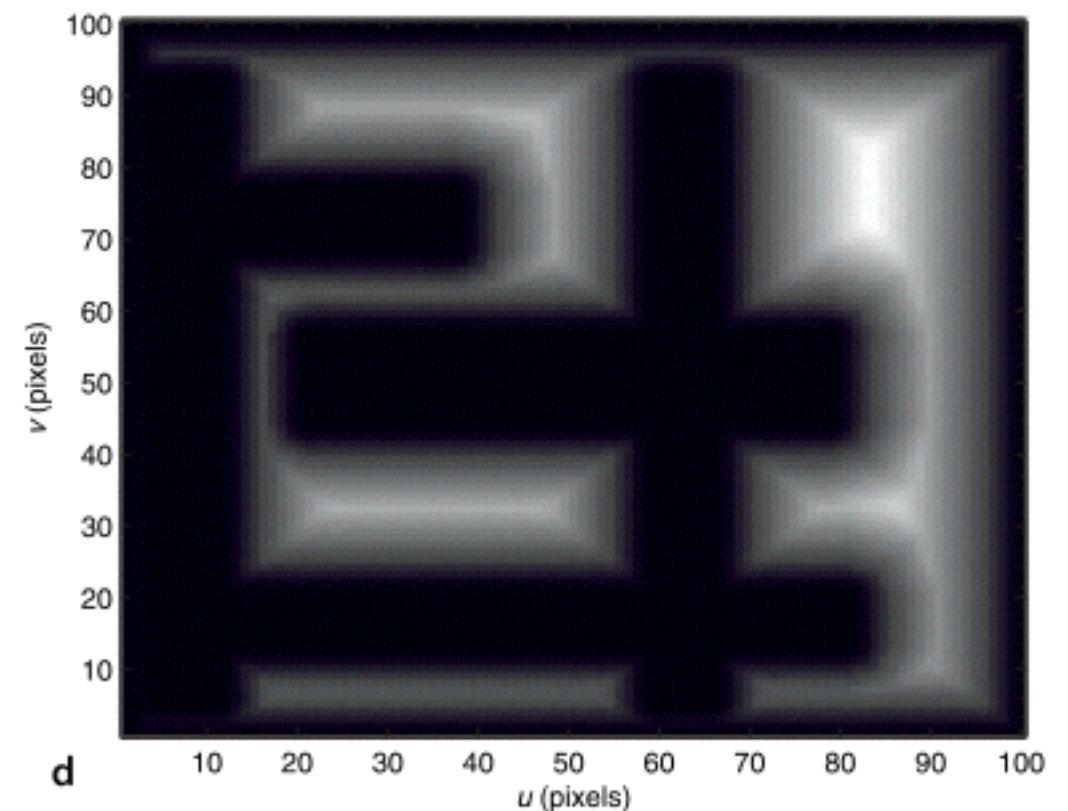
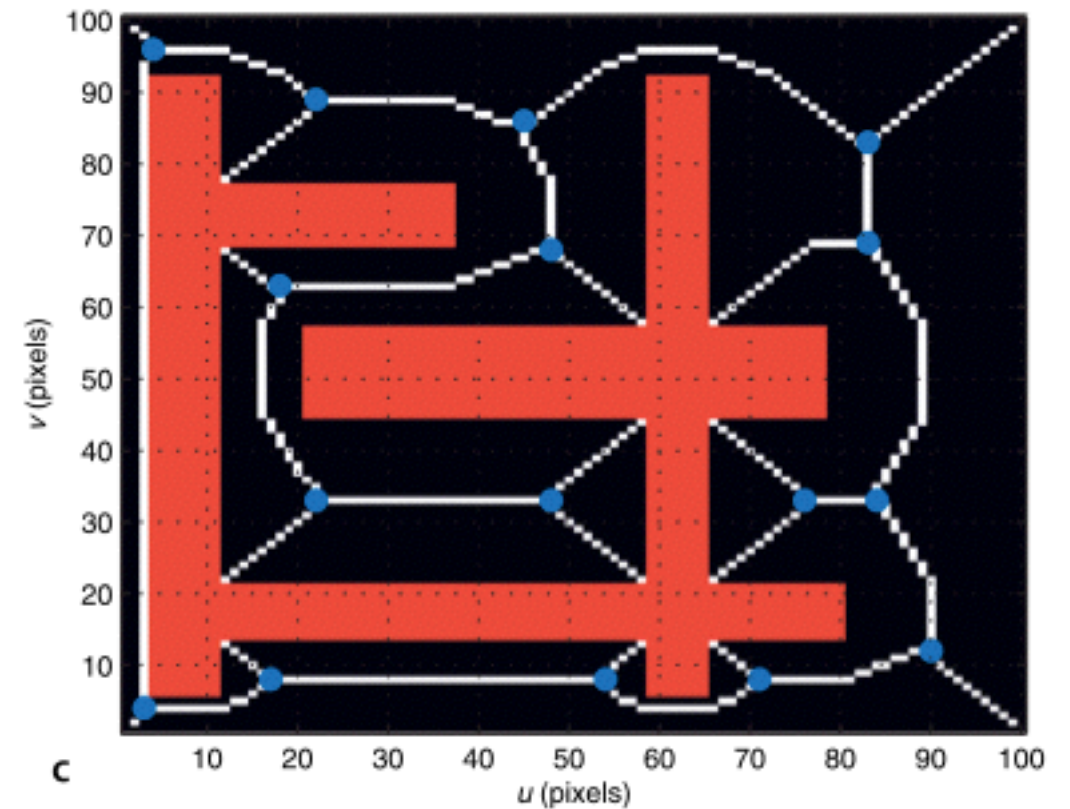
- Random grids of size 129 x 129



	replanning time
uninformed search from scratch	296.0 ms
heuristic search from scratch	10.5 ms
incremental uninformed search	6.1 ms
incremental heuristic search D* [Stentz, 1995] D* was probably the first true incremental heuristic search algorithm, way ahead of its time.	4.2 ms
D* Lite	2.7 ms

ROADMAP METHODS

- Do some setup work
- Make queries cheap
- Two methods:
 - *Voronoi Roadmap*
 - PRM

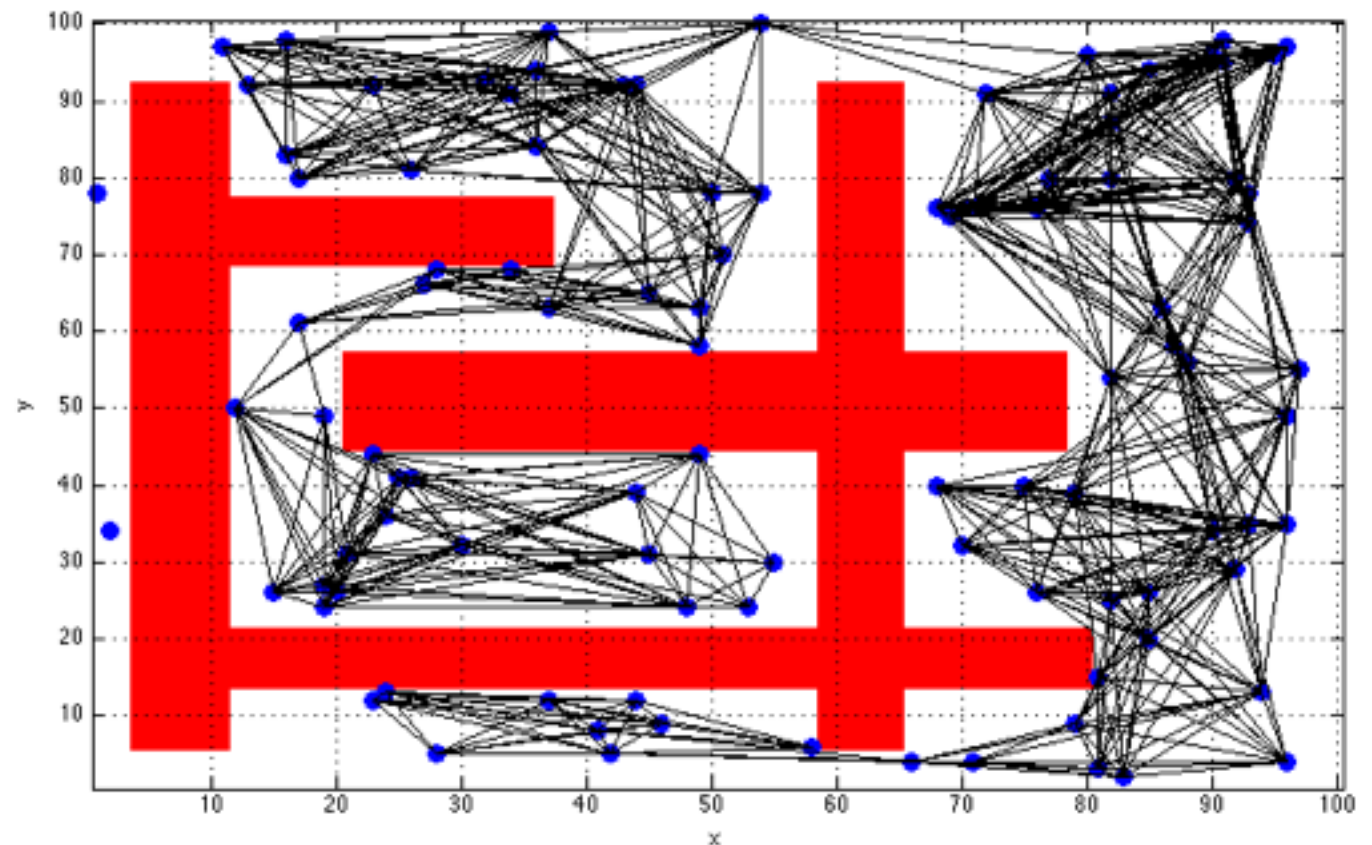


PROBABILISTIC ROADMAPS



Lydia E. Kavraki

- Randomly sample points
- Connect if no obstacle
- Plan using graph-search
- Disadvantages?



```
randinit  
prm = PRM(map)  
prm.plan()  
prm.plot()  
prm.path([20;10],[50;35]);
```

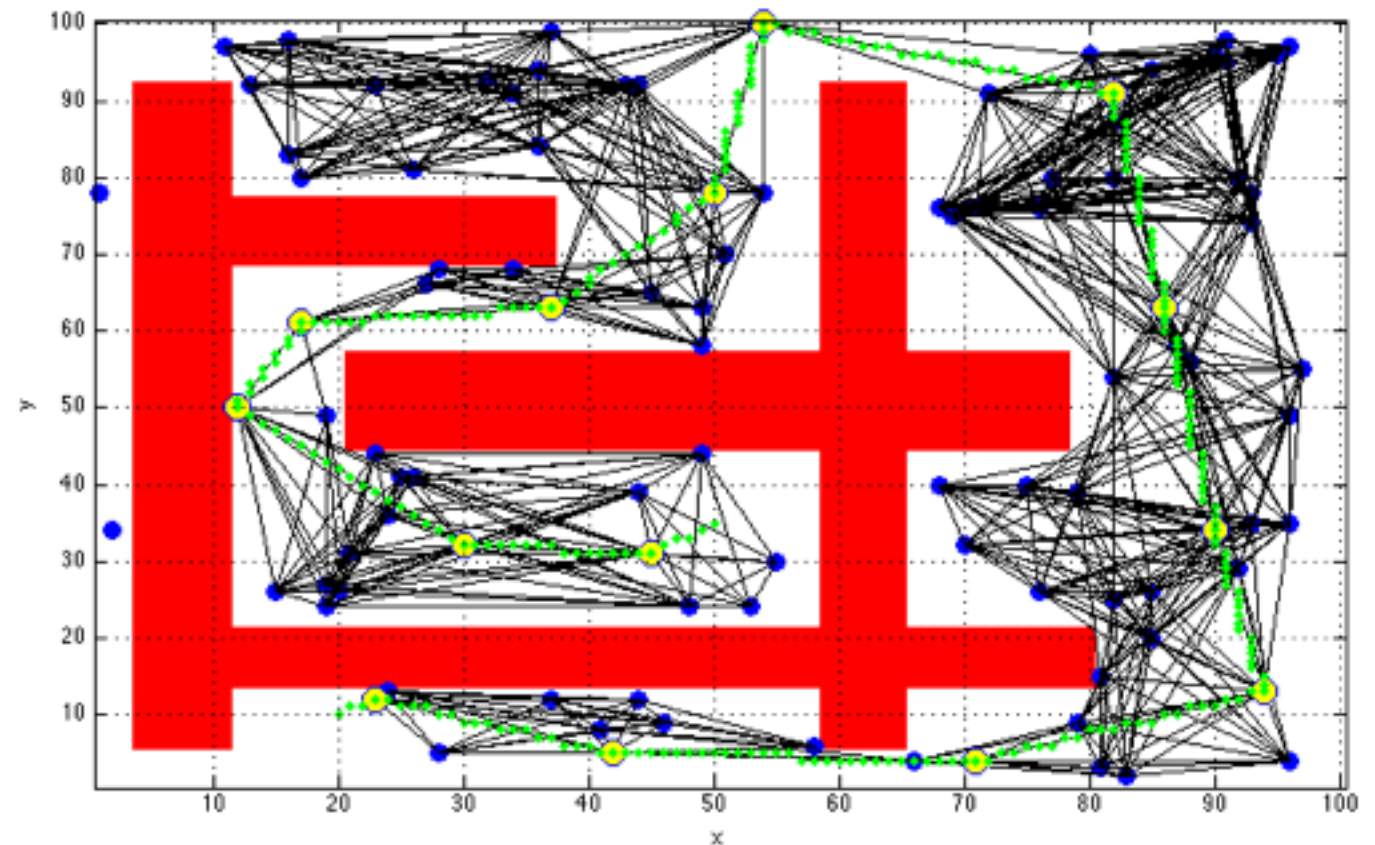
<http://www.youtube.com/watch?v=SG6BlmrHGk4>

PROBABILISTIC ROADMAPS



Lydia E. Kavraki

- Randomly sample points
- Connect if no obstacle
- Plan using graph-search
- Disadvantages?

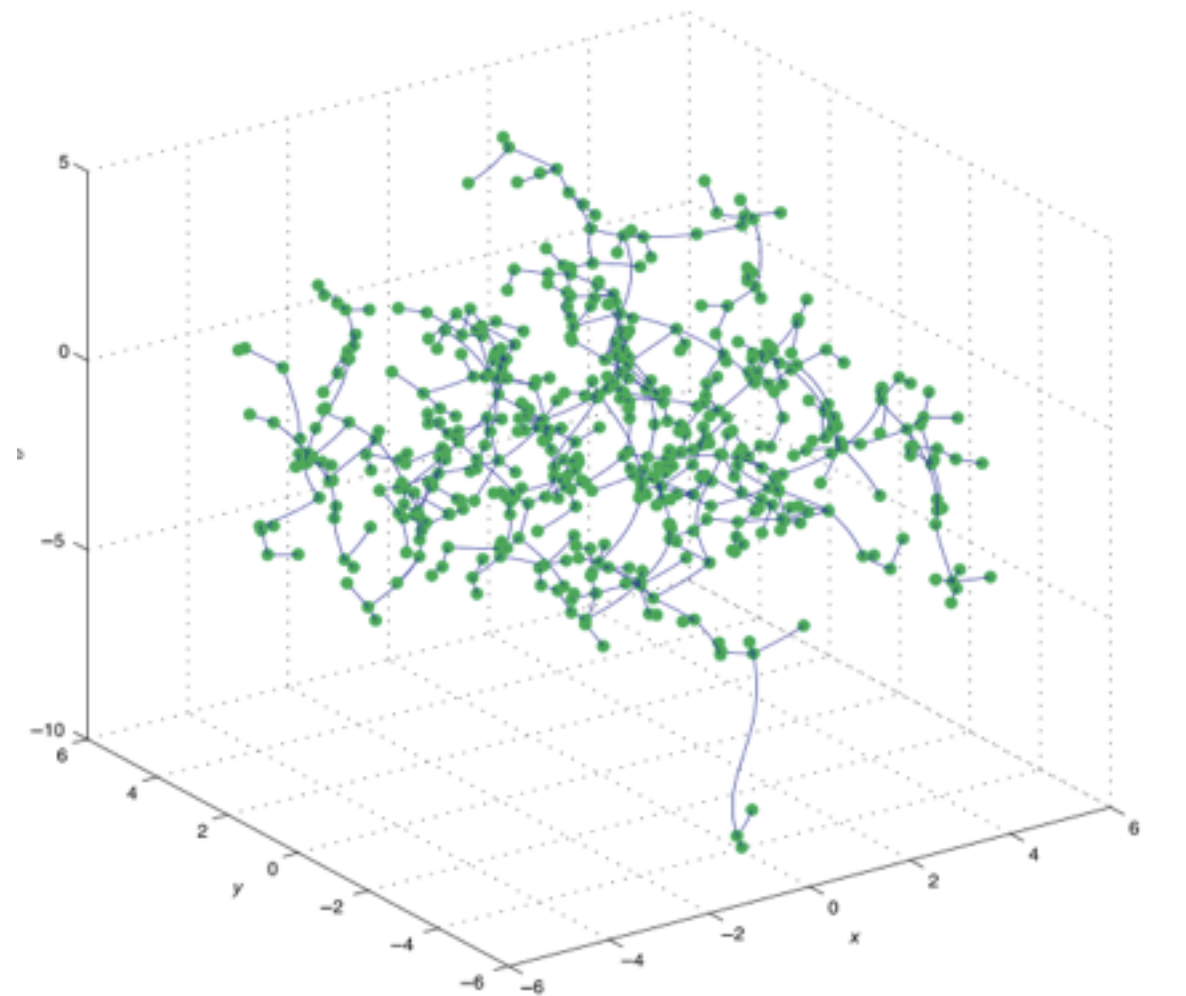
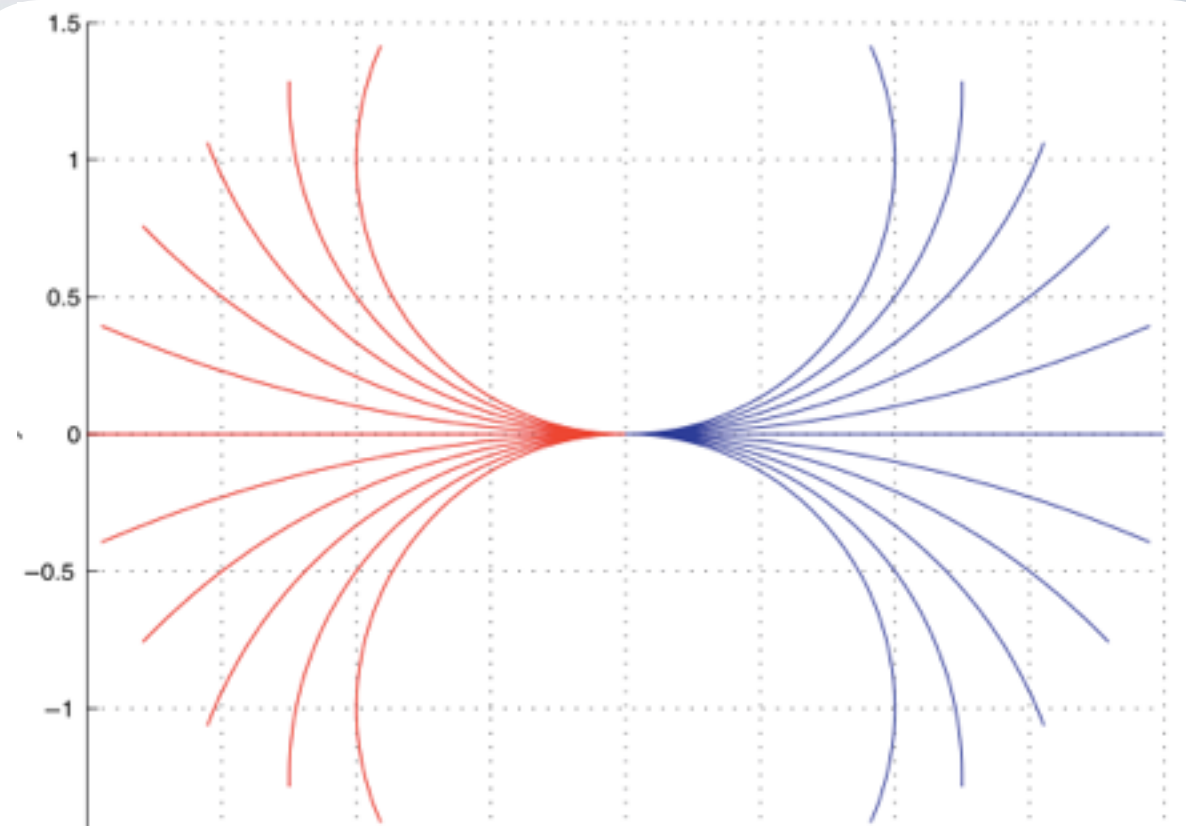


```
randinit  
prm = PRM(map)  
prm.plan()  
prm.plot()  
prm.path([20;10],[50;35]);
```

<http://www.youtube.com/watch?v=SG6BlmrHGk4>

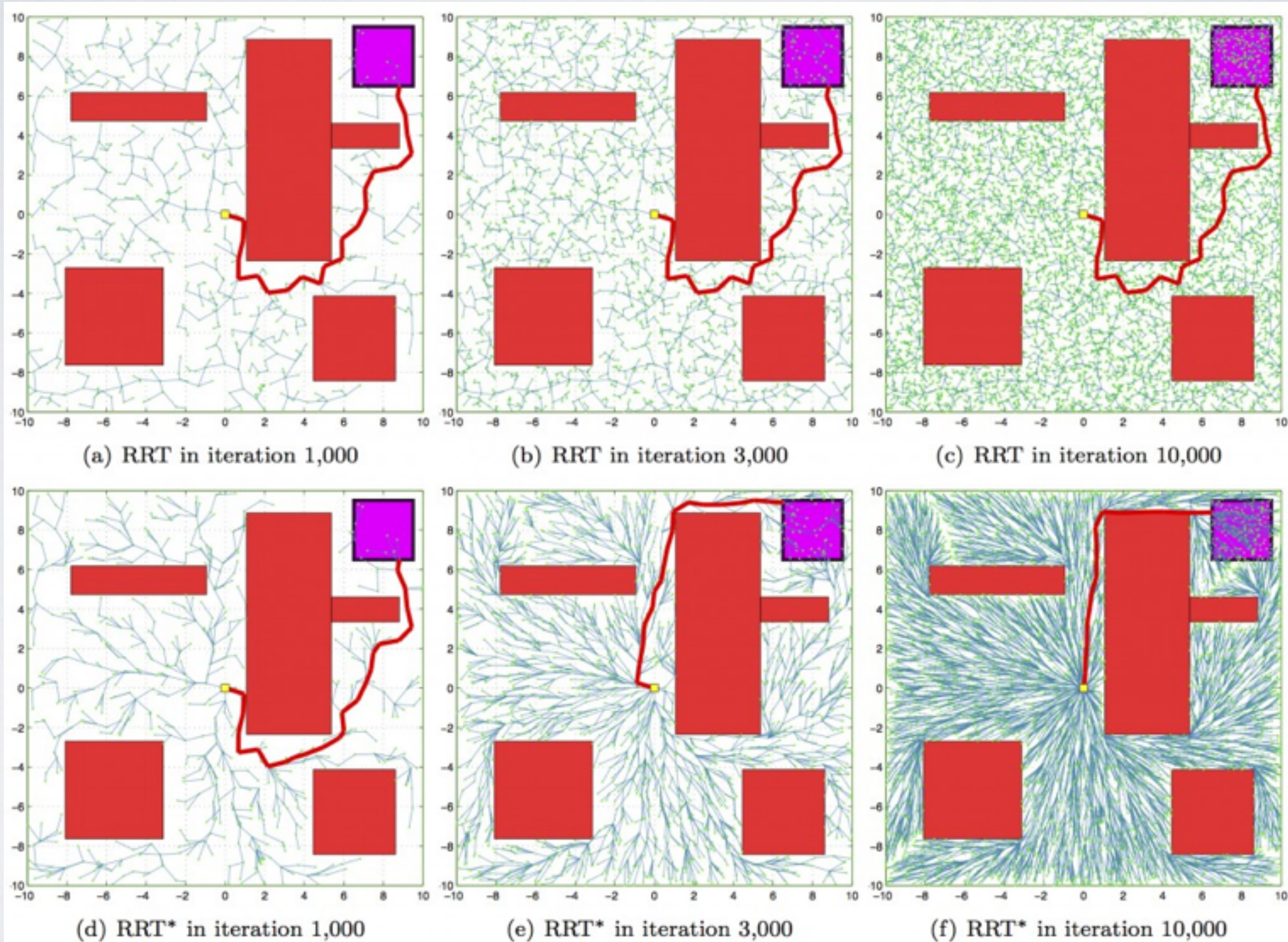
RRT

- Rapidly-exploring Random Tree
- Uses exact kinematic model
- Start with initial pose ξ_0
- At each time:
 - pick random pose ξ_{rand}
 - find nearest pose ξ_{near}
 - move towards it for fixed time, reaching ξ_{new}



see also <http://msl.cs.uiuc.edu/rrt/gallery.html>

RRT*



- Rewires the tree if shorter paths can be found