

## 10.1

#10

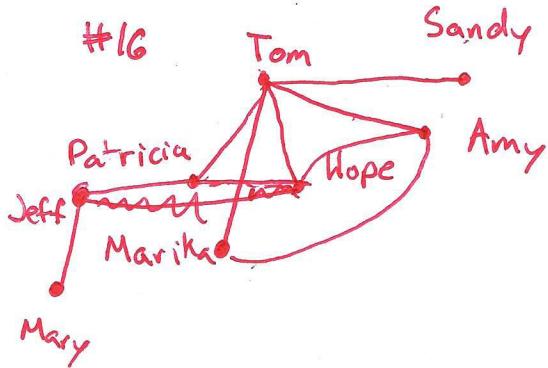
3 - none

4 -  $\overline{ab}$ ,  $\overline{bd}$ ,  $\overline{cd}$

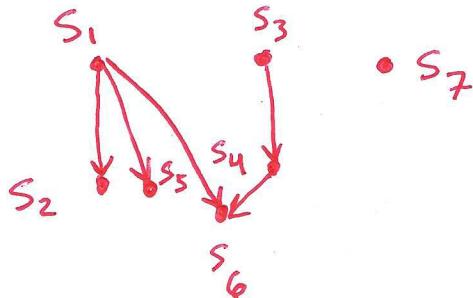
5 -  $\overline{a}$ ,  $\overline{b}$ ,  $\overline{d}$ ,  $\overline{ab}$ ,  $\overline{bd}$ ,  $\overline{cd}$

6 -  $\overline{ac}$ ,  $\overline{bd}$

7.



#33



## 10.2

#5 No, Theorem 2 states that undirected graph has an even number of vertices of odd degree.

#18 Suppose  $G$  is a <sup>simple</sup> graph with  $N$  vertices. ~~Each vertex has degree at most  $N-1$  since  $G$  is simple.~~ Make  $N-1$  boxes. And put each vertex in the box corresponding to its degree. By the pigeon hole principle there must be at least 1 box with more than 1 vertex. Thus there must be at least 2 vertices with the same degree.

26)

a)  $n = 2$

b)  $n \bmod 2 = 0$

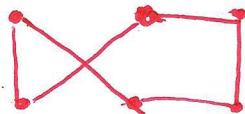
c)  $n = 1$

d) for all  $n$

42) a) odd number of odd deg.

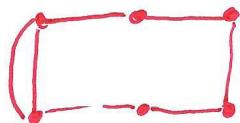
b) " odd number of odd deg "

c)



d) "odd number of od deg "

e)



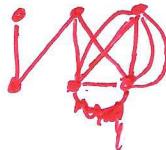
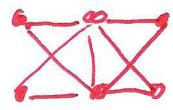
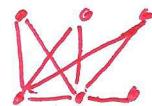
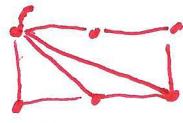
f)



g)



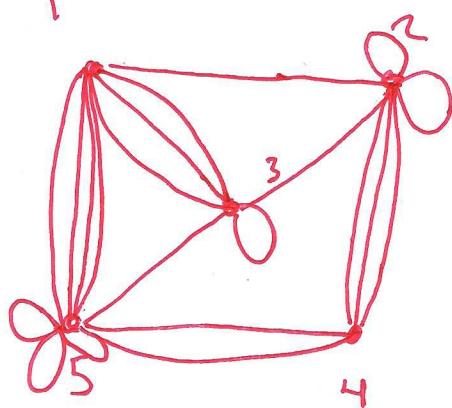
h)



10.38)  $\begin{matrix} & a & b & c & d & e \\ a & [0 & 1 & 0 & 1 & 0 \\ b & 1 & 0 & 1 & 0 & 0 \\ c & 0 & 1 & 1 & 0 & 1 \\ d & 1 & 1 & 0 & 0 & 0 \\ e & 0 & 1 & 0 & 1 & 1 \end{matrix}$ 

]

18)



36) In the first graph There is only 1 vertex of degree 2. In the second there are 2. Since the degree sequence is a graph invariant the 2 graphs can not be isomorphic.

54) a) 2 cases

b) 4 cases

c) 11 cases