Computational Physics Spring 2014, Shoemaker Homework 2 (Due date March 7 end of day)

Email homework as an attachment to (deirdre@gatech.edu and kjani3@gatech.edu). Include a README file that lists the files included with a short description (e.g. programs, plots, etc).

Your homework will be to finish the in-class work on pendulum.m. Specifically, produce a program that solves the non-linear pendulum as discussed in class. Your code must

- 1. take as user input on the command line or as an input file theta0, omega0, tmax, level
- 2. solve the non-linear pendulum for a set of first-order ODEs,
- 3. implement THREE methods: Euler, Runge-Kutta 2 and Rung-Kutta 4 for solving the ODEs,
- 4. run the code for several values of tmax, for each ODE method what is the maximum tmax that you could run before errors began to accumulate?
- 5. using a reasonable value or tmax, compare your result for the linear-case (i.e. when theta is very small) again the linear solution in the lecture notes
- 6. using a reasonable value of tmax, conduct a convergence test over three grids (fine, medium and coarse) for all three methods and plot the result versus time,

$$\frac{\theta_{\ell}(t) - \theta_{\ell+1}(t)}{\theta_{\ell+1}(t) - \theta_{\ell+2}(t)}$$

7. finally, discuss your results (convergence tests, linear test).