The second example of constructing a bottom-up parser

 Given the following production rules that define expressions:

```
    5. E' → <expr>
    6. <expr> → <expr> + <term>
    7. → <expr> - <term>
    8. <term> → (<expr>)
    9. → int
    10. <expr> → <term>
```

• NOTE: we construct the LR(0) states next, but leave the parsing table construction and parsing examples to students as exercises.

We derive the LR(0) states

```
S1: E' \rightarrow . <expr>
                                                                                                       (goto S2, S3, S4, S5)
        \langle expr \rangle \rightarrow . \langle expr \rangle + \langle term \rangle
      \langle expr \rangle \rightarrow . \langle expr \rangle - \langle term \rangle
      \langle expr \rangle \rightarrow . \langle term \rangle
        <term> \rightarrow . int
         \langle \text{term} \rangle \rightarrow . (\langle \text{expr} \rangle)
S2:E' \rightarrow \langle expr \rangle. (accept?)
                                                                                                       (goto S6, S7)
                         \langle expr \rangle \rightarrow \langle expr \rangle. + \langle term \rangle
                         \langle expr \rangle \rightarrow \langle expr \rangle. - \langle term \rangle
S3: \langle \exp r \rangle \rightarrow \langle term \rangle. (r10)
S4: \langle \text{term} \rangle \rightarrow \text{int.} (r9)
S5: \langle \text{term} \rangle \rightarrow (. \langle \text{expr} \rangle)
                                                                                                       (goto S8, S4, S5, S3)
                         \langle expr \rangle \rightarrow . \langle expr \rangle + \langle term \rangle
                         \langle expr \rangle \rightarrow . \langle expr \rangle - \langle term \rangle
                          \langle expr \rangle \rightarrow . \langle term \rangle
                           \langle \text{term} \rangle \rightarrow . int
                            \langle \text{term} \rangle \rightarrow . (\langle \text{expr} \rangle)
S6: \langle \exp r \rangle \rightarrow \langle \exp r \rangle + . \langle term \rangle
                                                                                                       (goto S9, S4, S5)
                          <term> \rightarrow . int
                            \langle \text{term} \rangle \rightarrow . (\langle \text{expr} \rangle)
S7: \langle expr \rangle \rightarrow \langle expr \rangle - . \langle term \rangle
                                                                                                      (goto S10, S4, S5)
                          \langle \text{term} \rangle \rightarrow . \text{ int}
                             \langle \text{term} \rangle \rightarrow . (\langle \text{expr} \rangle)
S8: \langle \text{term} \rangle \rightarrow (\langle \text{expr} \rangle)
                                                                                                                                              (goto S6, S7, S11)
                        \langle expr \rangle \rightarrow \langle expr \rangle. + \langle term \rangle
                        \langle expr \rangle \rightarrow \langle expr \rangle. - \langle term \rangle
S9: \langle \exp r \rangle \rightarrow \langle \exp r \rangle + \langle term \rangle. (r6)
S10: \langle expr \rangle \rightarrow \langle expr \rangle - \langle term \rangle. (r7)
S11: \langle \text{term} \rangle \rightarrow (\langle \text{expr} \rangle). (r8)
```

The parsing table we constructed in class

States	Action					Goto		
	id	=	int	;	\$	L	<stmt></stmt>	<expr></expr>
1	s2					g8	g7	
2		s3						
3			s4					g5
4	r5	r5	r5	r5	r5			
5				s6				
6	r4	r4	r4	r4	r4			
7	s2				r2	g9	g7	
8					acc			
9	r3	r3	r3	r3	r3			

NOTE: r5 means using rule 5 to reduce; acc means accept the input; From this table, one can draw the state diagram that has circles and edges, which we omit here.

Details in each state

- We constructed our parsing table based on "items" we found in each state and deduce all possible transitions.
- If a transition leads to a set of items (including the closure) that hasn't appeared before, we create a new state.
- All transitions from the same state and labeled by the same symbol must have the same state as the target!
- State numbering is arbitrary. In the future, we examine each state, for which we haven't examined the transitions yet, one by one, creating new states as needed. We keep a work list to store the new states. Removing a state from the work list at a time.
- For this example, we introduce new states in "depth-first" manner instead, in order to explain the state transitions in terms of an input example.
- The state tables built "depth-first" and "breadth-first" will be equivalent, differing only in the state numbering.

Applying the parsing table to an input example

- The parser maintains a parsing stack to store the history of shifts, reduces and gotos.
- Given input: "a = 3; b = 0;"

```
Stack
                                              -- next token position
1
                                             -- ^ a = 1; b = 0;
12
                                              -- a ^ = 1; b = 0;
123
                                             -a = ^1; b = 0;
1234
                                             -- a = 1 ^; b = 0;
                 (r5)
123
                 (g5)
1235
12356
                 (r4)
                                             -a = 1; ^ b = 0;
1
          (g7)
17
172
                                             -a = 1; b^{a} = 0;
1723
                                             -a = 1; b = ^0;
17234
                 (r5)
                                             -- a = 1; b = 0 ^;
1723
           (g5)
17235
172356
                 (r4)
                                             -- a = 1; b = 0; ^
17
          (g7)
177
          (r2)
 17
          (g9)
179
          (r3)
1
          (g8)
18
          (acc)
```