Recurrent Neural Network

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Outline

- 1 нмм
 - Markov Models
 - Hidden Markov Model
- Recurrent neural networks
 - Recurrent neural networks
 - BP on RNN
 - Variants of RNN
- Short-Term Memory recurrent networks
 - Challenge of long-term dependency
 - Combine short and long paths
 - Long short-term memory net
- 4 Applications



Sequential data

- Sequence of words in an English sentence
- Acoustic features at successive time frames in speech recognition
- Successive frames in video classification
- Rainfall measurements on successive days in Hong Kong
- Daily values of current exchange rate
- Nucleotide base pairs in a strand of DNA
- Instead of making independent predictions on samples, assume the dependency among samples and make a sequence of decisions for sequential samples

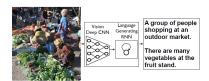


Sample data sequences from a certain distribution

$$P(\mathbf{x}_1,\ldots,\mathbf{x}_T)$$

Generate natural sentences to describe an image

$$P(\mathbf{y}_1,\ldots,\mathbf{y}_T|I)$$



Activity recognition from a video sequence

$$P(\mathbf{y}|\mathbf{x}_1,\ldots,\mathbf{x}_T)$$

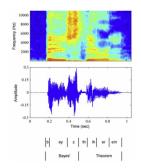


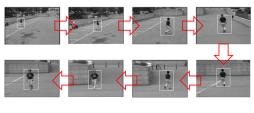
Speech recognition

$$P(\mathbf{y}_1,\ldots,\mathbf{y}_T|\mathbf{x}_1,\ldots,\mathbf{x}_T)$$

Object tracking

$$P(\boldsymbol{y}_1,\dots,\boldsymbol{y}_{T}|\boldsymbol{x}_1,\dots,\boldsymbol{x}_{T})$$





Generate natural sentences to describe a video

$$P(\mathbf{y}_1,\ldots,\mathbf{y}_{T'}|\mathbf{x}_1,\ldots,\mathbf{x}_T)$$

Language translation

$$P(\mathbf{y}_1,\ldots,\mathbf{y}_{T'}|\mathbf{x}_1,\ldots,\mathbf{x}_T)$$

Ulrich UNK, membre du conseil d'administration du constructeur automobile Audi, affirme qu'il s'agit d'une pratique courante depuis des années pour que les téléphones portables puissent être collectés avant les réunions du conseil d'administration afin qu'ils ne soient pas utilisés comme appareils d'écoute à distance.

Ulrich Hackenberg, membre du conseil d'administration du constructeur automobile Audi, déclare que la collecte des téléphones portables avant les réunions du conseil, afin qu'ils ne puissent pas être utilisés comme appareils d'écoute à distance, est une pratique courante depuis des années.

 Use the chain rule to express the joint distribution for a sequence of observations

$$p(\mathbf{x}_1,\ldots,\mathbf{x}_T) = \prod_{t=1}^T p(\mathbf{x}_t|\mathbf{x}_1,\ldots,\mathbf{x}_{t-1})$$

- Impractical to consider general dependence of future dependence on all previous observations $p(\mathbf{x}_t|\mathbf{x}_{t-1},...,\mathbf{x}_0)$
 - Complexity would grow without limit as the number of observations increases
- It is expected that recent observations are more informative than more historical observations in predicting future values

Markov models

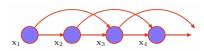
- Markov models assume dependence on most recent observations
- First-order Markov model

$$p(\mathbf{x}_1,\ldots,\mathbf{x}_T) = \prod_{t=1}^T p(\mathbf{x}_t|\mathbf{x}_{t-1})$$



Second-order Markov model

$$p(\mathbf{x}_1,\ldots,\mathbf{x}_T) = \prod_{t=1}^T p(\mathbf{x}_t|\mathbf{x}_{t-1},\mathbf{x}_{t-2})$$



Hidden Markov Model (HMM)

- A classical way to model sequential data
- Sequence pairs h₁, h₂,..., h_T (hidden variables) and x₁, x₂,..., x_T (observations) are generated by the following process
 - Pick h₁ at random from the distribution P(h₁). Pick x₁ from the distribution p(x₁|h₁)
 - For t = 2 to T
 - Choose h_t at random from the distribution $p(h_t|h_{t-1})$
 - Choose \mathbf{x}_t at random from the distribution $p(\mathbf{x}_t|h_t)$
- The joint distribution is

$$P(\mathbf{x}_1,\ldots,\mathbf{x}_T,h_1,\ldots,h_T,\theta) = P(h_1)\prod_{t=2}^T P(h_t|h_{t-1})\prod_{t=1}^T p(\mathbf{x}_t|h_t)$$

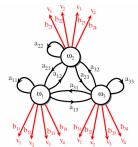


Parameters of HMM

• Initial state parameters $P(h_1 = \omega_i) = \pi_i, \sum_i \pi_i = 1$

Applications

- Transition probabilities $P(h_t = \omega_j | h_{t-1} = \omega_i) = a_{ij}, \sum_j a_{ij} = 1$. **A** = $[a_{ij}]$ is transition matrix
- Emission probabilities $p(\mathbf{x}_t|h_t)$
 - If \mathbf{x}_t is a single discrete variable, $\mathbf{x}_t = x_t \in \{v_1, \dots, v_m\}$, $P(x_t = v_k | z_t = \omega_l) = b_{ik}$, $\sum_k b_{ik} = 1$



Parameters of HMM

 Evaluation problem: determine the probability that a particular data sequence x₁,...,x_T was generated by that model,

$$P(\mathbf{x}_1,\ldots,\mathbf{x}_T)$$

 Decoding problem: given a set of observations x₁,..., x_T, determine the most likely sequence of hidden states h₁,..., h_T that lead to the observations

$$(h_1^*,\ldots,h_T^*) = \operatorname{argmax}_{(h_1,\ldots,h_T)} P(h_1,\ldots,h_T | \mathbf{x}_1,\ldots,\mathbf{x}_T)$$

 Learning problem: given a set of training observations of visible variables, without knowing the hidden variables, determine the parameters of HMM.

$$\theta^* = P(\mathbf{x}_1, \dots, \mathbf{x}_T; \theta)$$

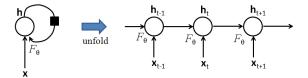


Recurrent neural networks (RNN)

- While HMM is a generative model RNN is a discriminative model
- Model a dynamic system driven by an external signal x_t

$$\mathbf{h}_t = F_{\theta}(\mathbf{h}_{t-1}, \mathbf{x}_t)$$

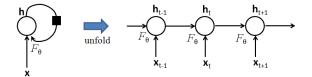
• \mathbf{h}_t contains information about the whole past sequence. The equation above implicitly defines a function which maps the whole past sequence $(\mathbf{x}_t, \dots, \mathbf{x}_1)$ to the current sate $\mathbf{h}_t = G_t(\mathbf{x}_t, \dots, \mathbf{x}_1)$



Left: physical implementation of RNN, seen as a circuit. The black square indicates a delay of 1 time step. Right: the same seen as an unfolded flow graph, where each node is now associated with one particular time instance.

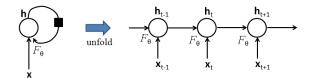
Recurrent neural networks (RNN)

- The summary is lossy, since it maps an arbitrary length sequence $(\mathbf{x}_t, \dots, \mathbf{x}_1)$ to a fixed length vector \mathbf{h}_t . Depending on the training criterion, \mathbf{h}_t keeps some important aspects of the past sequence.
- Sharing parameters: the same weights are used for different instances of the artificial neurons at different time steps
- Share a similar idea with CNN: replacing a fully connected network with local connections with parameter sharing
- It allows to apply the network to input sequences of different lengths and predict sequences of different lengths



Recurrent neural networks (RNN)

• Sharing parameters for any sequence length allows more better generalization properties. If we have to define a different function G_t for each possible sequence length, each with its own parameters, we would not get any generalization to sequences of a size not seen in the training set. One would need to see a lot more training examples, because a separate model would have to be trained for each sequence length.



A vanilla RNN to predict sequences from input

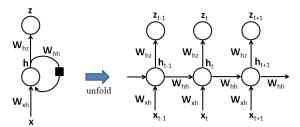
$$P(y_1,\ldots,y_T|\mathbf{x}_1,\ldots,\mathbf{x}_T)$$

 Forward propagation equations, assuming that hyperbolic tangent non-linearities are used in the hidden units and softmax is used in output for classification problems

$$\mathbf{h}_{t} = \tanh(\mathbf{W}_{xh}\mathbf{x}_{t} + \mathbf{W}_{hh}\mathbf{h}_{t-1} + \mathbf{b}_{h})$$

$$\mathbf{z}_{t} = \operatorname{softmax}(\mathbf{W}_{hz}\mathbf{h}_{t} + \mathbf{b}_{z})$$

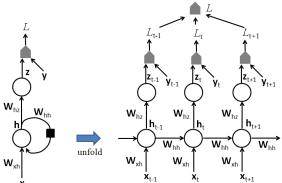
$$p(y_{t} = c) = z_{t,c}$$



Cost function

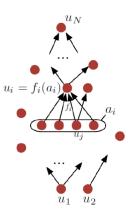
 The total loss for a given input/target sequence pair (x, y), measured in cross entropy

$$L(\mathbf{x},\mathbf{y}) = \sum_{t} L_{t} = \sum_{t} -\log z_{t,y_{t}}$$



Backpropagation on RNN

Review BP on flow graph



$$\begin{array}{l} \frac{\partial u_N}{\partial u_N} \leftarrow 1 \\ \text{for } j = N-1 \text{ down to } 1 \text{ do} \\ \frac{\partial u_N}{\partial u_j} \leftarrow \sum_{i:j \in \text{parents}(i)} \frac{\partial u_N}{\partial u_i} \frac{\partial u_i}{\partial u_j} \\ \text{end for} \\ \text{return} \left(\frac{\partial u_N}{\partial u_i}\right)_{i=1}^M \end{array}$$

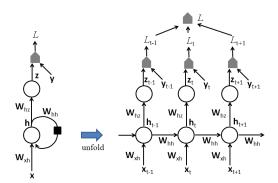
(Bengio et al. Deep Learning 2014)

$$\frac{\partial u_N}{\partial w_{ji}} = \frac{\partial u_N}{\partial u_i} \frac{\partial u_i}{\partial net_i} \frac{\partial net_i}{\partial w_{ji}}$$

Gradients on \mathbf{W}_{hz} and \mathbf{b}_z

$$\tfrac{\partial L}{\partial L_t} = 1, \qquad \tfrac{\partial L}{\partial \boldsymbol{z}_t} = \tfrac{\partial L}{\partial L_t} \tfrac{\partial L_t}{\partial \boldsymbol{z}_t} = \tfrac{\partial L_t}{\partial \boldsymbol{z}_t}$$

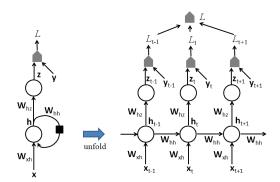
$$\frac{\partial L}{\partial \mathbf{W}_{hz}} = \sum_{t} \frac{\partial L_{t}}{\partial \mathbf{z}_{t}} \frac{\partial \mathbf{z}_{t}}{\partial \mathbf{W}_{hz}}, \qquad \frac{\partial L}{\partial \mathbf{b}_{z}} = \sum_{t} \frac{\partial L_{t}}{\partial \mathbf{z}_{t}} \frac{\partial \mathbf{z}_{t}}{\partial \mathbf{b}_{z}}$$



Gradients on \mathbf{W}_{hh} and \mathbf{W}_{xh}

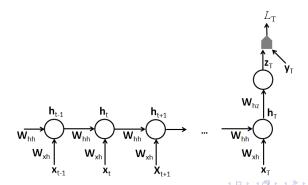
$$\frac{\partial L}{\partial \mathbf{W}_{hh}} = \sum_{t} \frac{\partial L}{\partial \mathbf{h}_{t}} \frac{\partial \mathbf{h}_{t}}{\partial \mathbf{W}_{hh}}$$

$$\frac{\partial L}{\partial \mathbf{h}_t} = \frac{\partial L}{\partial \mathbf{h}_{t+1}} \frac{\partial \mathbf{h}_{t+1}}{\partial \mathbf{h}_t} + \frac{\partial L}{\partial \mathbf{z}_t} \frac{\partial \mathbf{z}_t}{\partial \mathbf{h}_t}$$



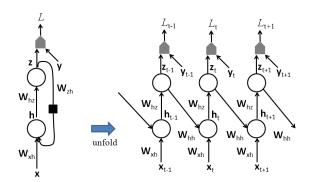
Predict a single output at the end of the sequence

 Such a network can be used to summarize a sequence and produce a fixed-size representation used as input for further processing. There might be a target right at the end or the gradient on the output z_t can be obtained by backpropagation from further downsteam modules



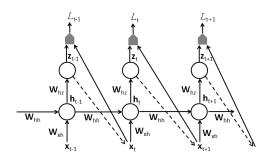
Network with output recurrence

 Memory is from the prediction of the previous target, which limits its expressive power but makes t easier to train



Generative RNN modeling $P(\mathbf{x}_1, \dots, \mathbf{x}_T)$

- It can generate sequences from this distribution
- At the training stage, each x_t of the observed sequence serves both as input (for the current time step) and as target (for the previous time step)
- The output z_t encodes the parameters of a conditional distribution P(x_{t+1}|x₁,...,x_t) = P(x_{t+1}|z_t) for x_{t+1} given the past sequence x₁,...,x_t



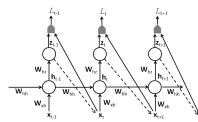
Generative RNN modeling $P(\mathbf{x}_1, \dots, \mathbf{x}_T)$

• Cost function: negative log-likelihood of \mathbf{x} , $L = \sum_t L_t$

$$P(\mathbf{x}) = P(\mathbf{x}_1, \dots, \mathbf{x}_T) = \prod_{t=1}^T P(\mathbf{x}_t | \mathbf{x}_{t-1}, \dots, \mathbf{x}_1)$$

$$L_t = -\log P(\mathbf{x}_t | \mathbf{x}_{t-1}, \dots, \mathbf{x}_1)$$

In generative mode, x_{t+1} is sampled from the conditional distribution P(x_{t+1}|x₁,...,x_t) = P(x_{t+1}|z_t) (dashed arrows) and then that generated sample x_{t+1} is fed back as input for computing the next state h_{t+1}



Generative RNN modeling $P(\mathbf{x}_1, \dots, \mathbf{x}_T)$

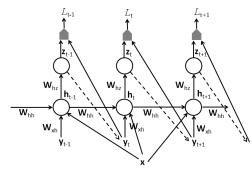
- If RNN is used to generate sequences, one must also incorporate in the output information allowing to stochastically decide when to stop generating new output elements
- In the case when the output is a symbol taken from a vocabulary, one can add a special symbol corresponding to the end of a sequence
- One could also directly directly model the length T of the sequence through some parametric distribution. $P(\mathbf{x}_1, \dots, \mathbf{x}_T)$ is decomposed into

$$P(\mathbf{x}_1,\ldots,\mathbf{x}_T)=P(\mathbf{x}_1,\ldots,\mathbf{x}_T|T)P(T)$$



RCNNs to represent conditional distributions $P(\mathbf{y}|\mathbf{x})$

- If x is a fixed-sized vector, we can simply make it an extra input of the RNN that generates the y sequence. Some common ways of providing the extra input
 - as an extra input at each time step, or
 - as the initial state h₀, or
 - both
- Example: generate caption for an image

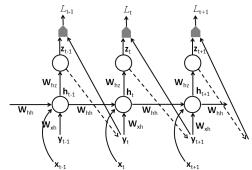


RCNNs to represent conditional distributions $P(\mathbf{y}|\mathbf{x})$

- The input x is a sequence of the same length as the output sequence y
- Removing the dash lines, it assumes y_t's are independent of each other when the past input sequence is given, i.e.

$$P(\mathbf{y}_t|\mathbf{y}_{t-1},\ldots,\mathbf{y}_1,\mathbf{x}_t,\ldots,\mathbf{x}_1)=P(\mathbf{y}_t|\mathbf{x}_t,\ldots,\mathbf{x}_1)$$

 Without the conditional independence assumption, add the dash lines and the prediction of y_{t+1} is based on both the past x's and past y's



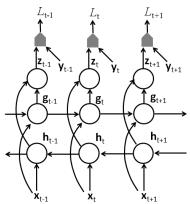
Bidirectional RNNs

- In some applications, we want to output at time t a prediction regarding an output which may depend on the whole input sequence
 - In speech recognition, the correct interpretation of the current sound as a phoneme may depend on the next few phonemes because co-articulation and may depend on the next few words because of the linguistic dependencies between words
- Bidirectional recurrent neural network was proposed to address such need
- It combines a forward-going RNN and a backward-going RNN
- The idea can be extended to 2D input with four RNN going in four directions



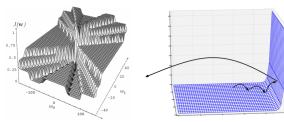
Bidirectional RNNs

g_t summaries the information from the past sequence, and h_t summaries the information from the future sequence



Plateaus and cliffs

- The error surfaces of training deep neural networks include local minima, plateaus (regions where error varies only slightly as a function of weights), and cliffs (regions where the gradients rise sharply)
- Plateaus and cliffs are more important barriers to training neural networks than local minima
 - It is very difficult (or slow) to effectively update the parameters in plateaus
 - When the parameters approach a cliff region, the gradient update step can move the learner towards a very bad configuration, ruining much progress made during recent training iterations.



- Training a very deep net makes the problem even more serious, since after BP through many layers, the gradients become either very small or very large
- RNN can be treated as a deep net when modeling long term dependency

- In very deep nets and recurrent nets, the final output is composed of a large number of non-linear transformations
- Even though each of these non-linear stages may be relatively smooth, their composition is going to be much "more non-linear", in the sense that the derivatives through the whole composition will tend to be either very small or very large, with more ups and downs



When composing many non-linearities (like the activation non-linearity in a deep or recurrent neural network), the result is highly non-linear, typically with most of the values associated with a tiny derivative, some values with a large derivative, and many ups and downs (not shown here)

This arises because the Jacobian (matrix of derivatives) of a composition is the product of the Jacobian of each stage, i.e. if

$$f = f_T \circ f_{T-1} \circ \dots f_2 \circ f_1$$

The Jacobian matrix of derivatives of f(x) with respect to its input vector **x** is

$$f' = f'_T f'_{T-1} \dots f'_2 f'_1$$

where

$$f' = \frac{\partial f(\mathbf{x})}{\partial \mathbf{x}}$$

and

$$f_t' = \frac{\partial f_t(\boldsymbol{\alpha}_t)}{\partial \boldsymbol{\alpha}_t}$$

where $\alpha_t = f_{t-1}(f_{t-1}(\dots f_2(f_1(\mathbf{x}))))$, i.e. composition has been replaced by matrix multiplication

- In the scalar case, we can imagine that multiplying many numbers together tends to be either very large or very small
- In the special case where all the numbers in the product have the same value α , this is obvious, since α^T goes to 0 if α < 1 and to ∞ if α > 1 as T increases
- The more general case of non-identical numbers be understood by taking the logarithm of these numbers, considering them to be random, and computing the variance of the sum of these logarithms. Although some cancellation can happen, the variance grows with T. If those numbers are independent, it grows linearly with T, which means that the product grows roughly as e^T.
- This analysis can be generalized to the case of multiplying square matrices

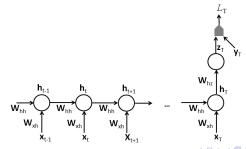


Difficulty of Learning Long-Term Dependencies

• Consider the gradient of a loss L_T at time T with respect to the parameter θ of the recurrent function F_{θ}

$$\frac{\mathbf{h}_{t} = F_{\theta}(\mathbf{h}_{t-1}, \mathbf{x}_{t})}{\partial \theta} = \sum_{t < T} \frac{\partial L_{T}}{\partial \mathbf{h}_{T}} \frac{\partial \mathbf{h}_{T}}{\partial \mathbf{h}_{t}} \frac{\partial F_{\theta}(\mathbf{h}_{t-1}, \mathbf{x}_{t})}{\partial \theta}$$

 $\frac{\partial L_{\mathcal{I}}}{\partial \mathbf{h}_{\mathcal{I}}} \frac{\partial \mathbf{h}_{\mathcal{I}}}{\partial \mathbf{h}_{\mathcal{I}}} \frac{\partial F_{\theta}(\mathbf{h}_{t-1}, \mathbf{x}_{t})}{\partial \theta}$ encodes long-term dependency when $\mathcal{T} - t$ is large



Difficulty of Learning Long-Term Dependencies

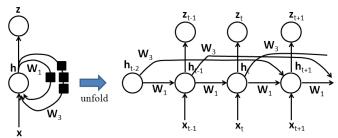
$$\frac{\partial \mathbf{h}_{T}}{\partial \mathbf{h}_{t}} = \frac{\partial \mathbf{h}_{T}}{\partial \mathbf{h}_{T-1}} \frac{\partial \mathbf{h}_{T-1}}{\partial \mathbf{h}_{T-2}} \cdots \frac{\partial \mathbf{h}_{t+1}}{\partial \mathbf{h}_{t}}$$

- Each layer-wise Jacobian $\frac{\partial \mathbf{h}_{t+1}}{\partial \mathbf{h}_t}$ is the product of two matrices: (a) the recurrent matrix \mathbf{W} and (b) the diagonal matrix whose entries are the derivatives of the non-linearities associated with the hidden units, which variy depending on the time step. This makes it likely that successive Jacobians have simliar eigenvectors, making the product of these Jacobians explode or vanish even faster
- $\frac{\partial L_T}{\partial \theta}$ is a weighted sum of terms over spans T-t, with weights that are exponentially smaller (or larger) for long-term dependencies relating the state at t to the state at T
- The signal about long term dependecies will tend to be hidden by the smallest fluctuations arising from short-term dependenties



Combine short and long paths in unfolded flow graph

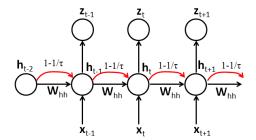
- Longer-delay connections allow to connect the past states to future states through short paths
- Gradients will vanish exponentially with respect to the number of time steps
- If we have recurrent connections with a time-delay of D, the instead of the vanishing or explosion going as $O(\lambda^T)$ over T steps (where λ is largest eigenvalue of the Jacobians $\frac{\partial \mathbf{h}_t}{\partial \mathbf{h}_{t-1}}$), the unfolded recurrent network now has paths through which gradients grow as $O(\lambda^{T/D})$ because the number of effective steps is T/D



Leaky units with self-connections

$$\mathbf{h}_{t+1} = (1 - \frac{1}{\tau_i})\mathbf{h}_t + \frac{1}{\tau_i} \tanh(\mathbf{W}_{xh}\mathbf{x}_t + \mathbf{W}_{hh}\mathbf{h}_t + \mathbf{b}_h)$$

- $lackbox{f \bullet}$ The new value of the state $f h_{t+1}$ is a combination of linear and non-linear parts of $f h_t$
- The errors are easier to be back propagated through the paths of red lines, which are linear



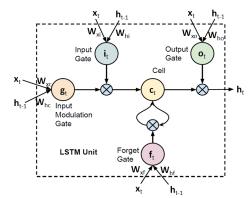
Leaky units with self-connections

- When $\tau=1$, there is no linear self-recurrence, only the nonlinear update which we can find in ordinary recurrent networks
- When $\tau >$ 1, this linear recurrence allows gradients to propagate more easily. When τ is large, the sate changes very slowly, integrating the past values associated with the input sequence
- ullet controls the rate of forgetting old states. It can be viewed as a smooth variant of the idea of the previous model
- ullet By associating different time scales au with different units, one obtains different paths corresponding to different forgetting rates
- Those time constants can be fixed manually or can be learned as free parameters

- In the leaky units with self-connections, the forgetting rate is constant during the whole sequence.
- The role of leaky units is to accumulate information over a long duration.
 However, once that information gets used, it might be useful for the neural network to forget the old state.
 - For example, if a video sequence is composed as subsequences corresponding to different actions, we want a leaky unit to accumulate evidence inside each subsequence, and we need a mechanism to forget the old state by setting it to zero and starting to count from fresh when starting to process the next subsequence
- The forgetting rates are expected to be different at different time steps, depending on their previous hidden sates and current input (conditioning the forgetting on the context)
- Parameters controlling the forgetting rates are learned from train data

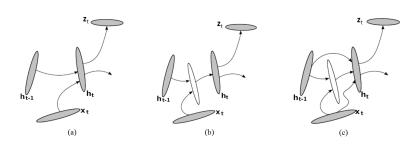


$$\begin{split} &\mathbf{f}_t = \sigma(\mathbf{W}_{xt}\mathbf{x}_t + \mathbf{W}_{ht}\mathbf{h}_{t-1} + \mathbf{b}_t), \ \mathbf{i}_t = \sigma(\mathbf{W}_{xi}\mathbf{x}_t + \mathbf{W}_{ht}\mathbf{h}_{t-1} + \mathbf{b}_i), \\ &\mathbf{o}_t = \sigma(\mathbf{W}_{xo}\mathbf{x}_t + \mathbf{W}_{ho}\mathbf{h}_{t-1} + \mathbf{b}_o) \\ &\mathbf{g}_t = \tanh(\mathbf{W}_{xc}\mathbf{x}_t + \mathbf{W}_{hc}\mathbf{h}_{t-1} + \mathbf{b}_c), \ \mathbf{c}_t = \mathbf{f}_t \odot \mathbf{c}_{t-1} + \mathbf{i}_t \odot \mathbf{g}_t \\ &\mathbf{h}_t = \mathbf{o}_t \odot \tanh(\mathbf{c}_t), \ \mathbf{z}_t = \mathrm{softmax}(\mathbf{W}_{hz}\mathbf{h}_t + \mathbf{b}_z) \end{split}$$

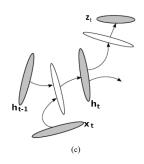


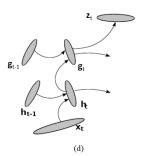
- The core of LSTM is a memory cell c_t which encodes, at every time step, the knowledge of the inputs that have been observed up to that step.
- The memory cell \mathbf{c}_t has the same inputs $(\mathbf{h}_{t-1}$ and $\mathbf{x}_t)$ and outputs (\mathbf{h}_t) as a normal recurrent network, but has more parameters and a system of gating units that controls the flow of information
- \mathbf{c}_t has a linear self-connection similar to the leaky units, but the self-connection weight is controlled by a forget gate unit \mathbf{f}_t , that sets this weight to a value between 0 and 1 via a sigmoid unit $\mathbf{f}_t = \sigma(\mathbf{W}_{xt}\mathbf{x}_t + \mathbf{W}_{ht}\mathbf{h}_{t-1} + \mathbf{b}_t)$
- The input gate unit i_t is computed similarly to the forget gate, but with its own parameters
- The output h_t of the LSTM cell can also be shut off, via the output gate o_t (h_t = o_t ⊙ tanh(c_t)), which is also a sigmoid unit for gating o_t = σ(W_{x0}x_t + W_{h0}h_{t-1} + b_o)

- (a): A vanilla RNN with input sequence and an output sequence
- (b): Add a deep hidden-to-hidden transformation
- (c): Skip connections and allow gradients to flow more easily backwards in spite of the extra non-linearity due to the intermediate hidden layer



- (c): Depth can also be added in the hidden-to-output transform
- (d): A hierarchy of RNNs, which can be stacked on top of each other



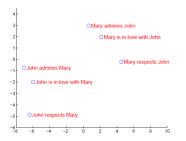


- Sutskever, Vinyals, and Le NIPS 2014
- Model $P(\mathbf{y}_1, \dots, \mathbf{y}_{T'} | \mathbf{x}_1, \dots, \mathbf{x}_T)$. The input and output sequences have different lengths, are not aligned, and even do not have monotonic relationship
- Use one LSTM to read the input sequence (x₁,...,x_T), one timestep at a time, to obtain a large fixed-dimensional vector representation v, which is given by the last hidden sate of the LSTM
- Then conditioned on \mathbf{v} , a second LSTM generates the output sequence $(\mathbf{y}_1, \dots, \mathbf{y}_{T'})$ and computes its probability

$$\rho(\mathbf{y}_{1},\ldots,\mathbf{y}_{T'}|\mathbf{v}) = \prod_{t=1}^{W} \rho(\mathbf{y}_{t}|v,\mathbf{y}_{1},\ldots,\mathbf{y}_{t-1})$$

The model reads an input sentence "ABC" and produces "WXYZ" as the output sentence. The model stops making predictions after outputting the end-of-sentence token.

- It requires each sentence ends with a special end-of-sequence symbol "<EOS>", which enables the model to define a distribution over sequences of all possible lengths
- It is valuable to reverse the order of the words of the input sequence. For example, instead of mapping the sentence a, b, c to the sentence α, β, γ , the LSTM is asked to map c, b, a to α, β, γ , where α, β, γ is the translation of a, b, c. This way, a is in close proximity to α, b is fairly close to β , and so on, a fact that makes it easy for stochastic gradient descent to "establish communication" between the input and the output. It introduces many short term dependencies in the data that make the optimization problem much easier.





The figure shows a 2-dimensional PCA projection of the LSTM hidden states that are obtained after processing the phrases in the figures. The phrases are clustered by meaning, which in these examples is primarily a function of word order, which would be difficult to capture with a bag-of-words model. The figure clearly shows that the representations are sensitive to the order of words, while being fairly insensitive to the replacement of an active voice with a passive voice.

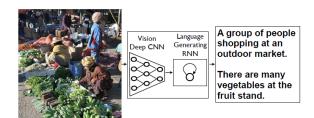


LSTM can correctly translate very long sentences

Type	Sentence
Our model	Ulrich UNK, membre du conseil d' administration du constructeur automobile Audi, affirme qu' il s' agit d' une pratique courante depuis des années pour que les téléphones portables puissent être collectés avant les réunions du conseil d' administration afin qu' ils ne soient pas utilisés comme appareils d' écoute à distance.
Truth	Ulrich Hackenberg , membre du conseil d' administration du constructeur automobile Audi , déclare que la collecte des téléphones portables avant les réunions du conseil , afin qu' ils ne puissent pas être utilisés comme appareils d' écoute à distance , est une pratique courante depuis des années .
Our model	"Les téléphones cellulaires, qui sont vraiment une question, non seulement parce qu'ils pourraient potentiellement causer des interférences avec les appareils de navigation, mais nous savons, selon la FCC, qu'ils pourraient interférer avec les tours de téléphone cellulaire lorsqu'ils sont dans l'air", dit UNK.
Truth	"Les téléphones portables sont véritablement un problème, non seulement parce qu'ils pourraient éventuellement créer des interférences avec les instruments de navigation, mais parce que nous savons, d'après la FCC, qu'ils pourraient perturber les antennes-relais de téléphonie mobile s'ils sont utilisés à bord ", a déclaré Rosenker.
Our model	Avec la crémation , il y a un " sentiment de violence contre le corps d' un être cher " , qui sera " réduit à une pile de cendres " en très peu de temps au lieu d' un processus de décomposition " qui accompagnera les étapes du deuil " .
Truth	Il y a , avec la crémation , "une violence faite au corps aimé ", qui va être " réduit à un tas de cendres " en très peu de temps , et non après un processus de décomposition , qui " accompagnerait les phases du deuil ".

Generate image caption

- Vinyals et al. arXiv 2014
- Use a CNN as an image encoder and transform it to a fixed-length vector
- It is used as the initial hidden state of a "decoder" RNN that generates the target sequence

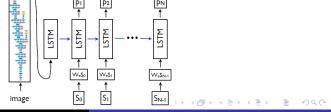


Generate image caption

 The learning process is to maximize the probability of the correct description given the image

$$\begin{aligned} \theta^* &= \arg\max \sum_{(\mathbf{I},\mathbf{S})} \log P(\mathbf{S}|\mathbf{I};\theta) \\ \log P(\mathbf{S}|\mathbf{I}) &= \sum_{l=0}^N \log P(\mathbf{S}_l|I,\mathbf{S}_0,\dots,\mathbf{S}_{l-1}) \end{aligned}$$

I is an image and S is its correct description



Generate image caption

- Denote by S_0 a special start work and by S_N a special stop word
- Both the image and the words are mapped to the same space, the image by using CNN, the words by using word embedding W_e
- The image I is only input once at t 1 to inform the LSTM about the image contents
- Sampling: sample the first word according to P₁, then provide the corresponding embedding as input and sample P₂, continuing like this until it samples the special end-of-sentence token

$$\begin{aligned} \mathbf{x}_{-1} &= \mathsf{CNN}(\mathbf{I}) \\ \mathbf{x}_t &= \mathbf{W}_{\theta} \mathbf{S}_t, t \in \{0, \dots, N-1\} \\ P_{t+1} &= \mathsf{LSTM}(\mathbf{x}_t), t \in \{0, \dots, N-1\} \\ L(\mathbf{I}, \mathbf{S}) &= -\sum_{t=1}^N \log P_t(\mathbf{S}_t) \end{aligned}$$

- Venugopalan et al. arXiv 2014
- The challenge is to capture the joint dependencies of a sequence of frames and a corresponding sequence of words
- Previous works simplified the problem by detecting a fixed set of semantic roles, such as subject, verb, and object, as an intermediate representation and adopted oversimplified rigid sentence templates.

Input video:



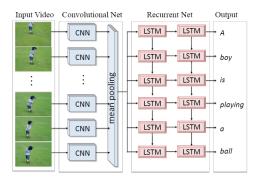




Machine output: A cat is playing with toy.

Humans: A Ferret and cat fighting with each other. / A cat and a ferret are playing. / A kitten and a ferret are playfully wresting.

- Each frame is modeled as CNN pre-trained on ImageNet
- The meaning sate and sequence of words is modeled by a RNN pre-trained on images with associated with sentence captions



- Use CNN to convert a video to a fixed length representation vector v
- Use RNN to decode the vector into a sentence just like language translation

$$\rho(\mathbf{y}_1,\ldots,\mathbf{y}_{T'}|\mathbf{v})=\prod_{t=1}^{T'}\rho(\mathbf{y}_t|v,\mathbf{y}_1,\ldots,\mathbf{y}_{t-1})$$

Use two layers of LSTMs (one LSTM stacked on top of another)



FGM: A person is playing a guitar in the

- YT: A group of performing on stage. YT C: A man is doing a trick. YT_CF: A man is jumping on a pole.
- GT: Two men working on a high building.



FGM: A person is playing a guitar in the house.

- YT: A boy is walking. YT C: A man is doing a women.
- YT CF: A man is talking on a wall. GT: A man is doing algebraic equations on a white board.



FGM: A person is riding the horse YT: A group of running. YT C: A group of elephants. YT CF: A group of elephants are walking on a horse.



GT: An elephant leads it's young. FGM: A person playing the goal of the



road.

- YT: A player player in a goal. YT_C: A man playing a soccer ball. YT CF: A soccer player is running.
- GT: Two teams are playing soccer.



FGM: A person is running a race on the road.

- YT: A group of running. YT C: A group of people are running.
- YT CF: A man is running.

GT: Eight men are running a race on a track.

FGM: factor graph model, using templates to generate sentences

YT: LSTM trained on the YouTube video dataset

YT C: LSTM with pre-training on the Coco image dataset

YT CF: LSTM with pre-training on the CoCo and Flicker image datasets GT: Ground truth from human description



Reading Materials

- R. O. Duda, P. E. Hart, and D. G. Stork, "Pattern Classification," Chapter 6, 2000.
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