

Transformation-Based Optimization

Basis for a series of optimizer frameworks:
Exodus, Volcano, Cascades, Columbia,
Colombia

Optimize an expression: look for all equivalent plans

- requires optimizing sub-expressions
- "memoize" results for later reuse

Produce logically equivalent expressions via rewrite

(then map them to physical plans and estimate their costs)

Based on Algebraic Equivalences

Example:

$$\sigma_P(u \cap v) \equiv \sigma_P(u) \cap \sigma_P(v)$$

Need to know such equivalences are correct

Usually easiest to work from set-theoretic definition

$$\sigma_P(r) = \{t \mid t \in r \text{ and } P(t)\}$$

$$r \cap s = \{t \mid t \in r \text{ and } t \in s\}$$

Expand Left Side

$$\begin{aligned}\sigma_P(u \cap v) &= \\ \sigma_P(\{t1 \mid t1 \in u \text{ and } t1 \in v\}) &= \\ \{t2 \mid t2 \in \{t1 \mid t1 \in u \text{ and } t1 \in v\} \text{ and } & \\ P(t2)\} &= \\ \{t2 \mid (t2 \in u \text{ and } t2 \in v) \text{ and } P(t2)\} &\end{aligned}$$

Expand Right Side

$$\begin{aligned}\sigma_P(u) \cap \sigma_P(v) &= \\ \{t1 \mid t1 \in u \text{ and } P(t1)\} \cap \{t2 \mid t2 \in v & \\ \text{and } P(t2)\} &= \\ \{t3 \mid t3 \in \{t1 \mid t1 \in u \text{ and } P(t1)\} \text{ and } & \\ t3 \in \{t2 \mid t2 \in v \text{ and } P(t2)\}\} &= \\ \{t3 \mid (t3 \in u \text{ and } P(t3)) \text{ and } & \\ (t3 \in v \text{ and } P(t3))\} &= \end{aligned}$$

Continuing ...

$$\{t3 \mid (t3 \in u \text{ and } P(t3)) \text{ and } (t3 \in v \text{ and } P(t3))\} = \quad [\text{simplify}]$$

$$\{t3 \mid t3 \in u \text{ and } P(t3) \text{ and } t3 \in v\} = \quad [\text{rearrange}]$$

$$\{t3 \mid (t3 \in u \text{ and } t3 \in v) \text{ and } P(t3)\} = \quad [\text{change variable}]$$

$$\{t2 \mid (t2 \in u \text{ and } t2 \in v) \text{ and } P(t2)\}$$

et voila!

Equivalences Can Have Side Conditions

An equivalence may hold only under certain conditions

$$\pi_X(\sigma_P(r)) \equiv \sigma_P(\pi_X(r))$$

if $\text{mentioned}(P) \subseteq X$

$\text{mentioned}(P)$ = set of attributes used in P

$$\pi_{ABC}(\sigma_{A>B}(r)) \equiv \sigma_{A>B}(\pi_{ABC}(r)) \quad \text{OK}$$

$$\pi_{BC}(\sigma_{A>B}(r)) \equiv \sigma_{A>B}(\pi_{BC}(r)) \quad \text{not OK}$$

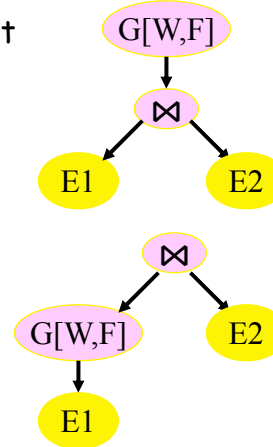
Rewriting Group-by

Initial translation usually puts group-by above join

May be useful to move past other operators

Move down:
makes one of the join inputs smaller

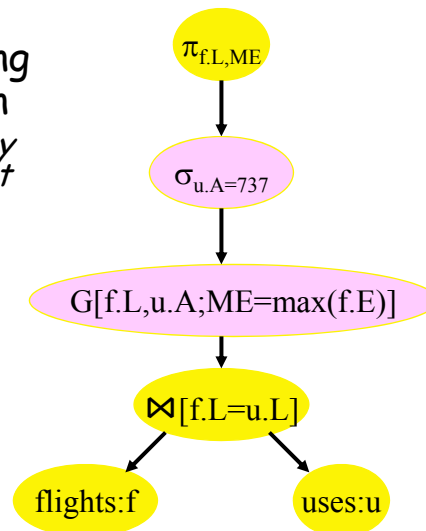
Move up:
might make input to group-by smaller



Select and Group-by

Consider the following starting expression

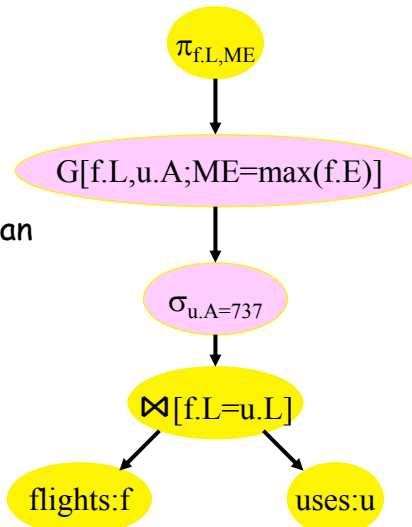
Find max # of economy seats for flights that use a 737



Do Selection Early

Is this okay?

Yes - the select applies to the grouping attributes, which are constant for a group
Want groups to pass in an all-or-nothing manner



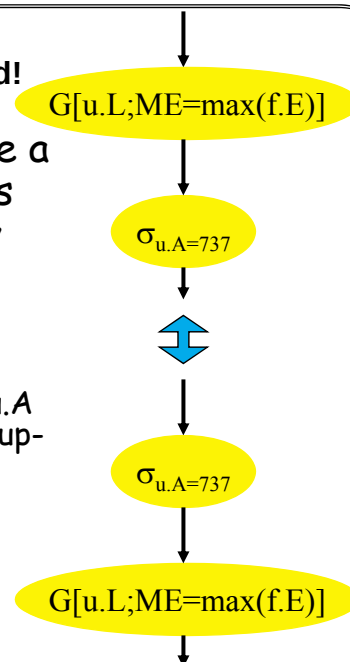
I'm Confused!

Paper* says you can move a select if the attributes it uses are functionally determined by the grouping attributes

Assume $L \rightarrow A$ on uses

Doesn't seem right to me: $u.A$ isn't visible above the group-by

* Orthogonal Optimization of Subqueries and Aggregation



Principles of Database Systems

Add an Attribute?

If we lift a selection above a Group-by, add the attribute to the grouping condition?

- Won't create more groups if $L \rightarrow A$.
- Will need to project away A at some point.

```

graph TD
    A[G[u.L; ME=max(f.E)]] --> B[σu.A=737]
    B --> C[σu.A=737]
    C --> D[G[u.L, u.A; ME=max(f.E)]]
    
```

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Group-by and Join

```

graph TD
    subgraph LeftPlan [Left Plan]
        L1[G[f.L; SE=sum(f.E)]] --> L2[⋈[f.L=u.L]]
        L2 --> L3[flights:f]
        L2 --> L4[σu.A=737]
        L4 --> L5[uses:u]
    end
    subgraph RightPlan [Right Plan]
        R1[πf.L, SE] --> R2[⋈[f.L=u.L]]
        R2 --> R3[G[f.L; SE=sum(f.E)]]
        R2 --> R4[σu.A=737]
        R3 --> R5[flights:f]
        R4 --> R6[uses:u]
    end
    L1 <-->|OK?| R1
    
```

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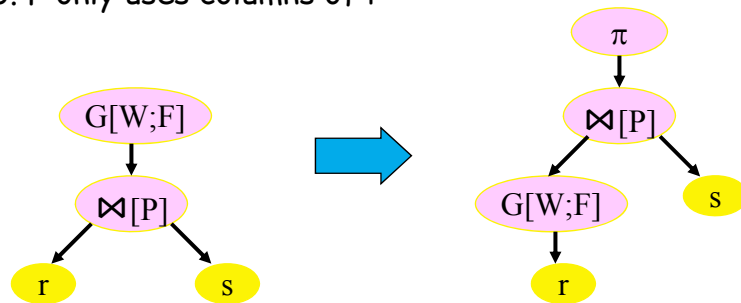
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Side Conditions

Have $r(R)$, $s(S)$, P mentions $X \subseteq R$

Group-by through join okay if

1. X is in W : join columns of R included in grouping columns
2. W contains a key of s
3. F only uses columns of r



Why?

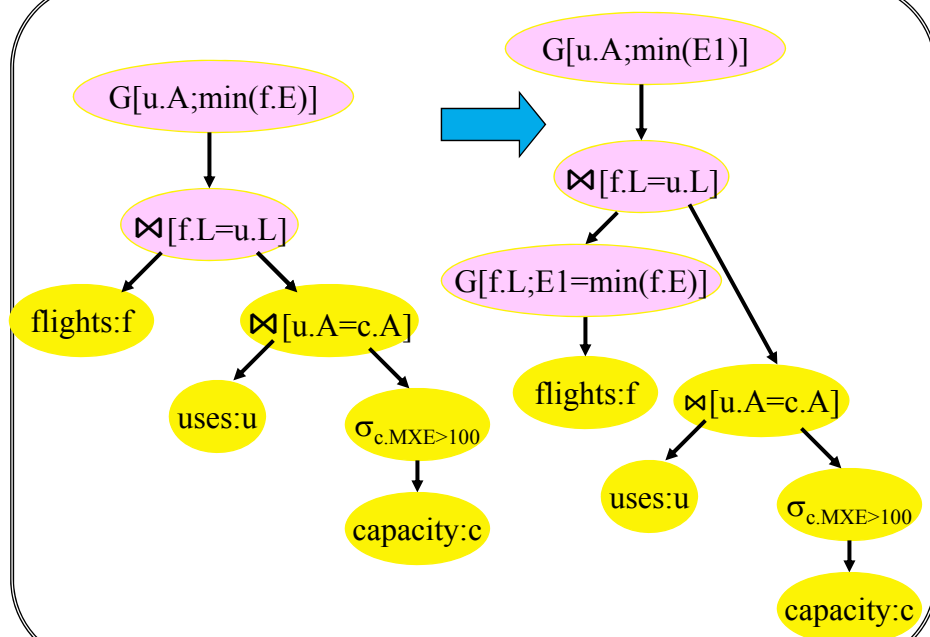
1. Can't lose the join columns
2. Need to have only one s tuple per row of $G[W;F]$
Can relax for max and min
3. Only have r available

Transforming from right to left,
conditions 1 and 3 come for free
Given that the initial expression is well formed

Splitting a Group-by

Can do partial grouping (local group-by), then a join, then rest of grouping

```
select u.A, min(f.E)
from flight as f, uses as u,
     capacity as c
where f.L = u.L and u.A = c.A
     and c.MXE > 100
group-by u.A
```



CS 589, Principles of Database Systems, Lecture 3-2

Principles of Database Systems

Min of Mins = Min of all

<u>u.A</u>	<u>f.L</u>	<u>f.E</u>	<u>u.A</u>	<u>f.L</u>	<u>E1</u>	<u>u.A</u>	<u>min(E1)</u>
737	115	65	737	115	65	737	65
737	115	70					
737	115	75					
737	80	95	737	80	75		
737	80	75					

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Works for Sum, Too

<u>u.A</u>	<u>f.L</u>	<u>f.E</u>	<u>u.A</u>	<u>f.L</u>	<u>E1</u>	<u>u.A</u>	<u>sum(E1)</u>
737	115	65	737	115	210	737	380
737	115	70					
737	115	75					
737	80	95	737	80	170		
737	80	75					

$E1 = \text{sum}(f.E)$

What about count? Does count of counts = count of all?
What about average??

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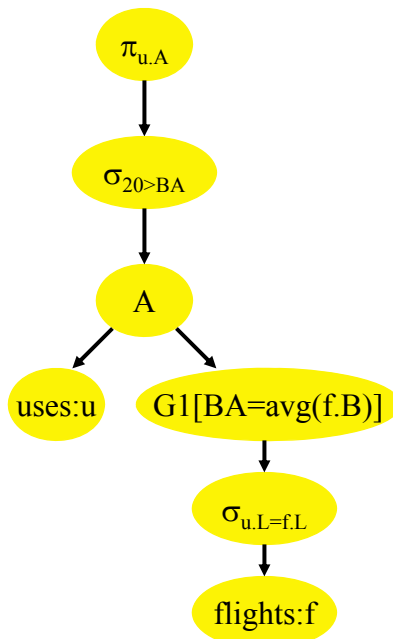
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Removing Sub-queries

We introduced "apply" to translate subqueries

```
select u.A
from uses as u
where 20 > [BA]
      (select avg(f.B) [as BA]
       from flights as f
       where f.L = u.L)
```



Apply Options

Can have a direct (for-loop)
implementation of apply as a physical
operator

But it is also possible to remove apply
via rewriting

Strategy:

Use push-down transforms that move apply
towards bottom of expression tree

Until its right input no longer depends on the
left input

Then, convert apply to a join

Example: Apply through Scalar Group-by

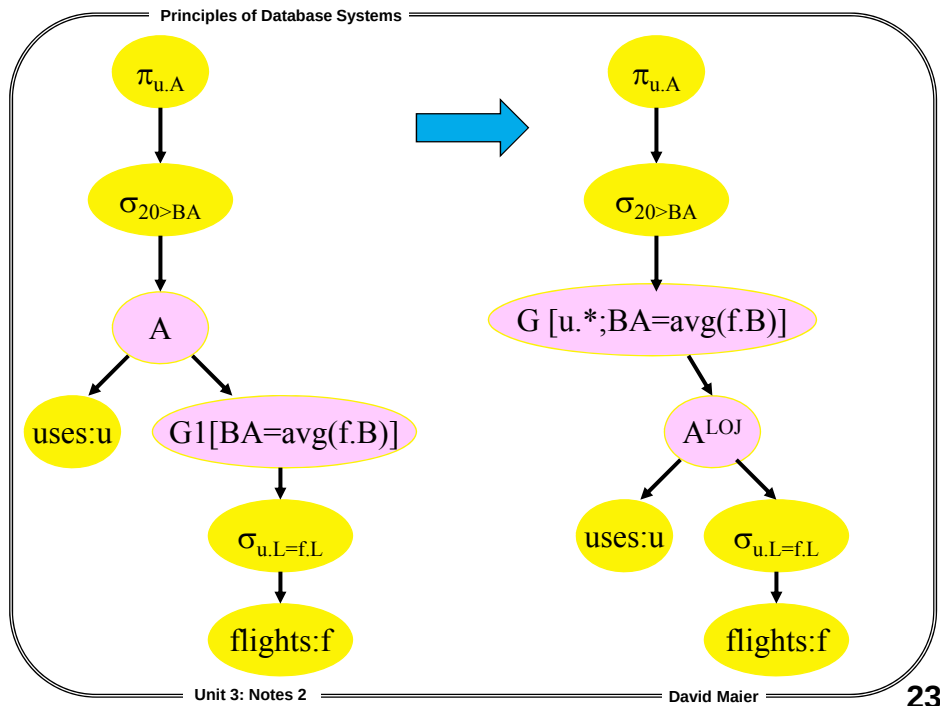
$r \bowtie G1[F](e(x)) \rightarrow G[r.*, F](r \bowtie^{LOJ} e(x))$

$\bowtie^{LOJ}$ keeps every tuple t in r , even if
 $e(t)$ is empty

need it because $G1$ always produces a row

$r \bowtie^{LOJ} e(x) =$

$r \bowtie^{LOJ} (DE(r) \bowtie e(x))$



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Example: Apply-to-Join Conversion

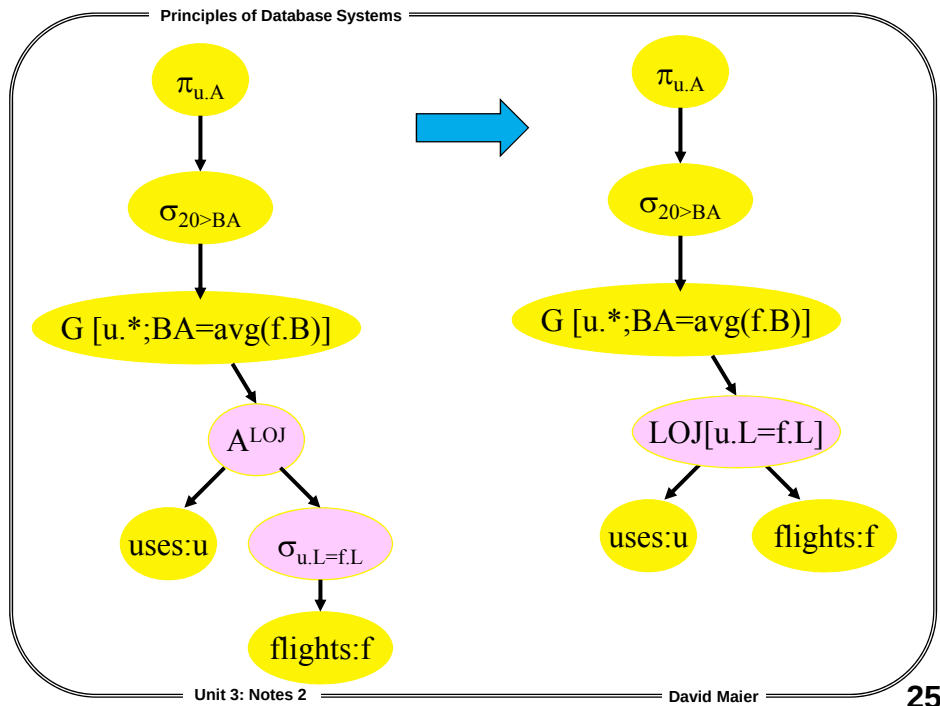
$$r A^{LOJ} \sigma_p(e) \rightarrow r LOJ[P] e$$

if e does not depend on r
(okay for P to depend on r)

Can think of apply as a "catalyst": used in transforming algebra, but doesn't show up in the end product

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What Was I Lying About?

Not all query plans are created equal
They differ in *physical properties*

- sort order
- distribution
- compression

Some physical operators need inputs with certain properties in order to work correctly

Sort-merge join: needs inputs sorted on attributes in an equality join condition

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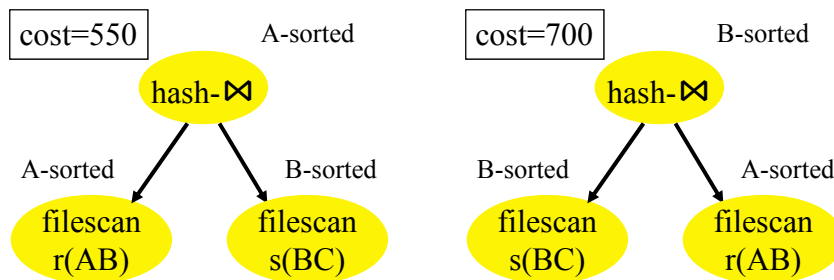
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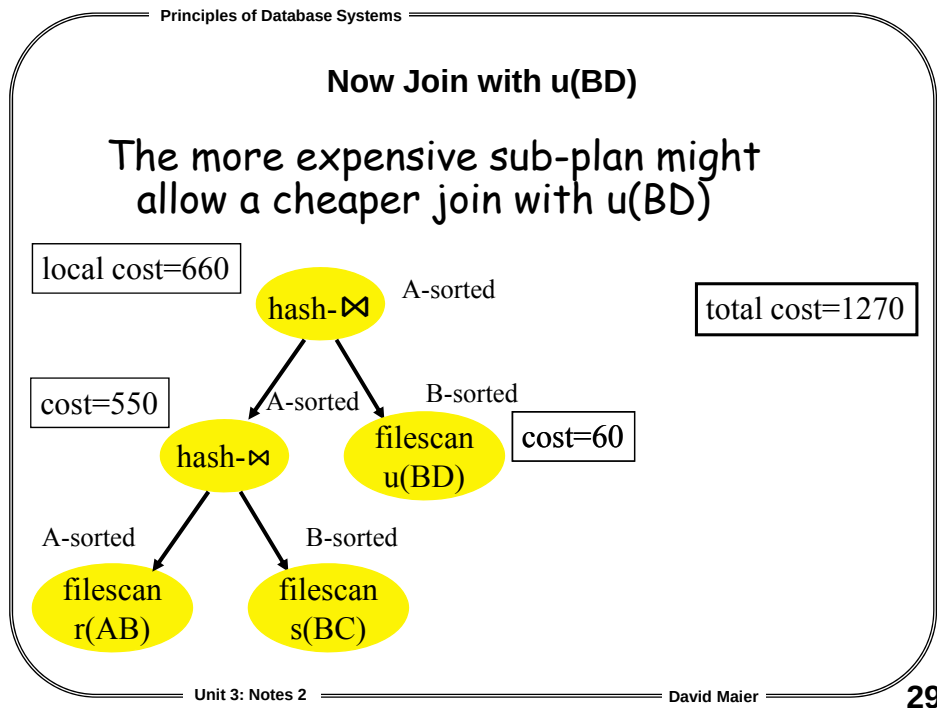
Physical Properties Can Affect Cost

Union, project might be faster on
compressed inputs
Fewer bytes to deal with

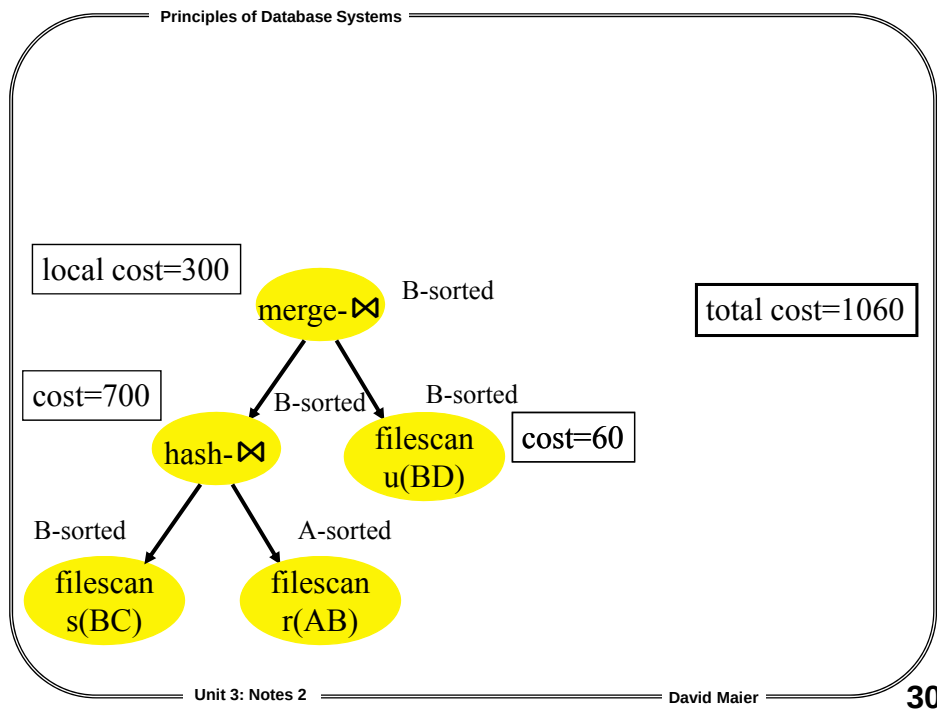
Physical Properties and Optimization

Because of differing physical
properties, cheapest sub-plan might
not be best choice in overall plan.
consider join of r , s and u





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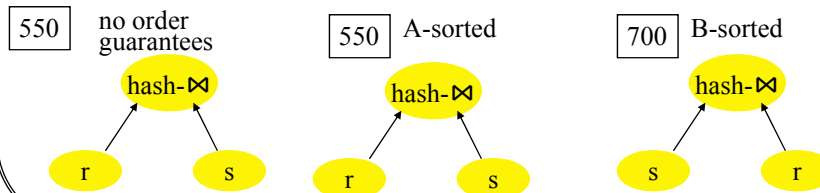
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So, Do We Forget the Optimality Principle?

No - it still holds, relative to plans with the same physical properties.

So - need to keep best plan for each physical property

For example, dynamic programming approach keeps the best plan for each collection of physical properties

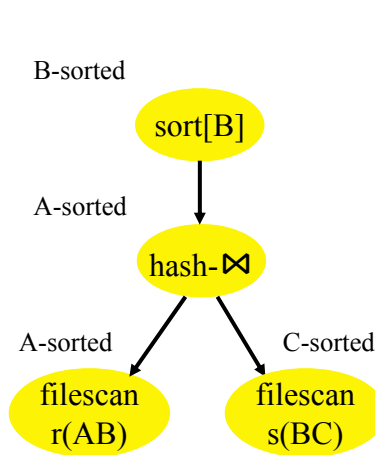


Do We Need Plans for Every Possible Property?

Probably not. For example, System R only keeps best plans for each *interesting order* (sort orders that might be useful in rest of query)

- attributes in a join predicate
- grouping attributes in an aggregate
- order-by clause in original query

Can Enforce Properties



Even if a sub-plan doesn't produce a particular physical property, usually possible to modify output to do so.

Enforcer: physical operator that enforces a physical property, but is a "no-op" at the logical level

Usually incurs some cost

Mapping Logical to Physical

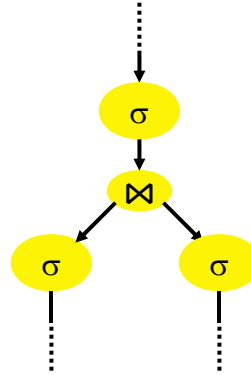
Not a one-to-one correspondence
generally between logical and physical operators

- Can have several physical ops that correspond to a given logical op
join: nested-loops join, index-nested-loops join, hash join, merge join

- One physical op might implement several logical ops

Have flags on hash join for regular join, outer-join, semi-join

- One physical op might translate a tree of logical ops



hash-join(join-pred, pre-left,
pre-right, post-pred)

Cost Estimation

Can view operators under alternative interpretations

Normal view

- $\sigma_{A>B}$: relation $\rightarrow$ relation

Alternative interpretations

Properties

- $\sigma_{A>B}$: order $\rightarrow$ order, FDs $\rightarrow$ FDs

Stats

- $\sigma_{A>B}$: column histogram $\rightarrow$ column histogram

Costs

- $\sigma_{A>B}$: CPU secs $\rightarrow$ CPU secs

Also for Selection and Join Predicates

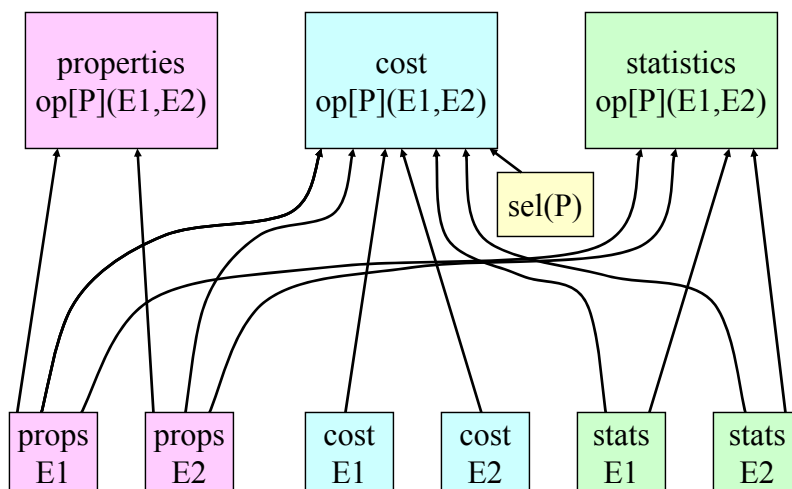
Interpret predicates as a *selectivity*.
% of tuples (or tuple pairs) expected
to satisfy the condition

System R

$\text{sel}(A=5) = 10\%$

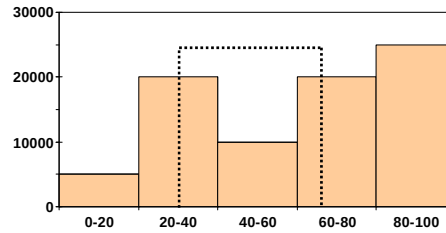
$\text{sel}(A<5) = 50\%$

These Interpretations Make Use of Each Other

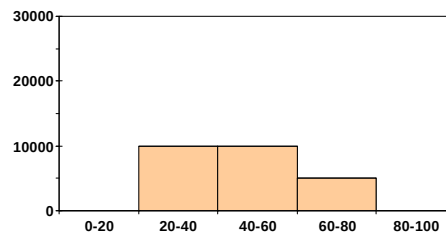


Histogram Example (on Attribute A)

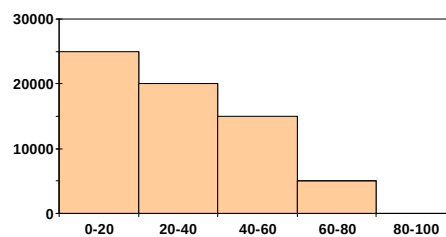
$r(AB)$



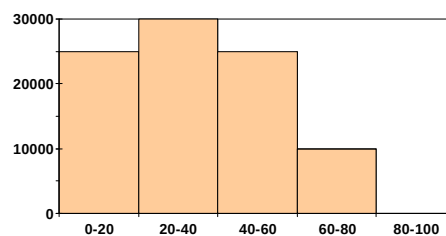
$\sigma_{30 \leq A \leq 65}(r(AB))$

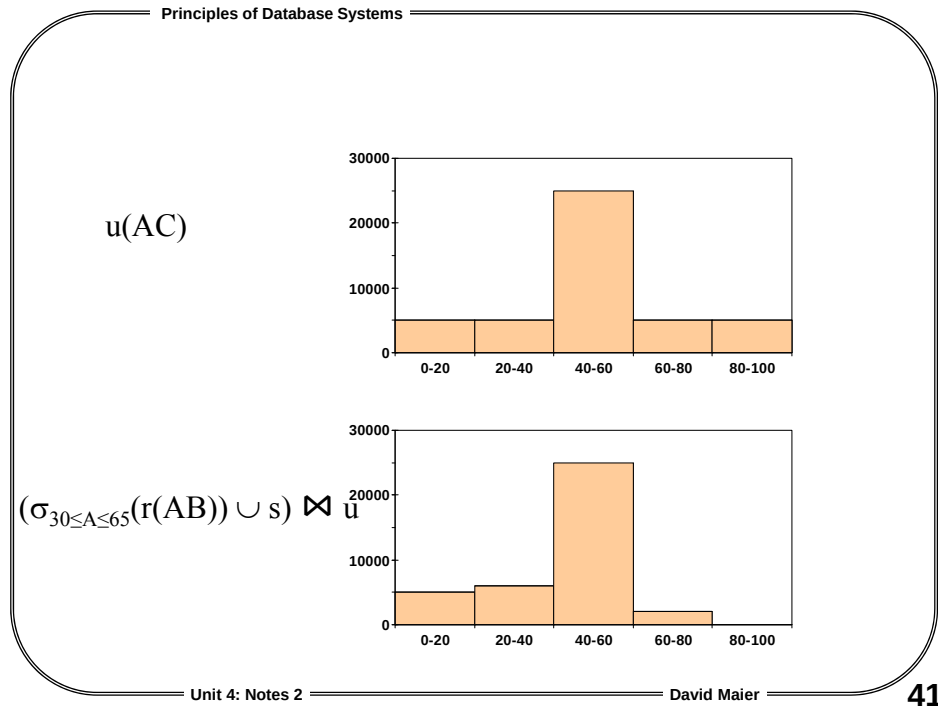


$s(AB)$



$\sigma_{30 \leq A \leq 65}(r(AB)) \cup s$





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