

MATH 1115

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FUNDAMENTAL MATHEMATICS FOR THE
GENERAL SCIENCES I (GROUP 1)

ASSIGNMENT 1 SOLUTIONS

- 1) B
- 2) D
- 3) D

- 4) $(3 + 4i) \in \mathbb{C}$ (set of Complex Numbers)
"i" represents $\sqrt{-1}$

TWO APPLICATIONS OF COMPLEX NUMBERS

- Physics - Electromagnetism to represent field strength and electromagnetic strength.
 - Electronics to represent inductance and capacitance e.g. $W = C + iL$
- Electrical - Fourier transforms in understanding engineering oscillations and frequencies
- Fluid dynamics, Quantum Mechanics, Dynamical systems, Computer graphics and so on.

- 5) a) (i) 15.932 (5 s.f.)
(ii) ~~16~~ (2 s.f.)
(iii) 15.9 (3 d.p.)

- b) (i) 100.057 (6 s.f.)
(ii) 100 (2 s.f.)
(iii) 100.057 (3 d.p.)

- c) (i) 0.000114 (3 s.f.)
0.00011 (2 s.f.)
0.000 (3 d.p.)

- d) (i) 308.5998 (7 s.f.)
310 (2 s.f.)
308.600 (3 d.p.)

e) 9.5108 (5 s.f.)
 9.5 (2 s.f.)
 9.511 (3 d.p.)

6 a) $213.49 = 2.1349 \times 10^2$

b) $0.045 \times 10^{-3} = 4.5 \times 10^{-2} \times 10^{-3} = 4.5 \times 10^{-5}$

c) $0.36^2 = \cancel{0.36} (3.6 \times 10^{-1})^2$

$$= 3.6^2 \times 10^{-2}$$

$$= 12.96 \times 10^{-2}$$

$$= 1.296 \times 10 \times 10^{-2}$$

$$= 1.296 \times 10^{-1}$$

OR $0.36^2 = 0.1296$
 $= 1.296 \times 10^{-1}$

d) $0.03249 = 3.249 \times 10^{-2}$

7) $48 \text{ km s}^{-1} \rightarrow \text{m s}^{-1}$

$$1 \text{ km} = 10^3 \text{ m}$$

$$\Rightarrow 48 \text{ km} = 48 \times 10^3 \text{ m}$$

$$\therefore 48 \text{ km s}^{-1} = 48 \times 10^3 \text{ m s}^{-1}$$

$$= 4.8 \times 10 \times 10^3 \text{ m s}^{-1}$$

$$= 4.8 \times 10^4 \text{ m s}^{-1}$$

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8) a) $10.1 \text{ million m} \rightarrow \mu\text{m}$

$$\begin{aligned} 1 \mu\text{m} &= 10^{-6} \text{ m} \Rightarrow 1 \text{ m} = 10^6 \mu\text{m} \\ 10.1 \text{ million m} &= 10.1 \times 10^6 \times 10^6 \mu\text{m} \\ &= 10.1 \times 10^{12} \mu\text{m} \\ &= 1.01 \times 10 \times 10^{12} \mu\text{m} \\ &= 1.01 \times 10^{13} \mu\text{m} \quad (\text{Scientific Notation}) \end{aligned}$$

b) $100.051 \text{ nm} \rightarrow \text{m}$

$$\begin{aligned} 1 \text{ nm} &= 10^{-9} \text{ m} \\ 100.051 \text{ nm} &= 100.051 \times 10^{-9} \text{ m} \\ &= 1.00051 \times 10^2 \times 10^{-9} \text{ m} \\ &= 1.00051 \times 10^{-7} \text{ m} \quad (\text{Scientific Notation}) \\ &\approx 1.00 \times 10^{-7} \text{ m} \end{aligned}$$

c) $30 \times 10^{-6} \text{ km}^2 \rightarrow \text{m}^2$

$$\begin{aligned} 1 \text{ km} &= 10^3 \text{ m} \\ 1 \text{ km}^2 &= (10^3)^2 \text{ m}^2 = 10^6 \text{ m}^2 \\ 30 \times 10^{-6} \text{ km}^2 &= 30 \times 10^{-6} \times 10^6 \text{ m}^2 \\ &= 30 \times 10^0 \text{ m}^2 \quad (\text{Recall: } 10^0 = 1) \\ &= 3.0 \times 10^1 \text{ m}^2 \end{aligned}$$

END