

Lecture 05:

Recap Chapter 2

"Motion in 1 dimension"

5th lecture, 2nd chapter, 1st dimension

Erik Lascaris

Announcements

- *Today (and tomorrow):*

Lab #1!

- *Where's the lab?*

SCI-134

- *When?*

Check StudentLink

(first one is tonight 6:30pm)

PY 105
Elementary Physics I

Physics Laboratory Schedule
Week of the 30th of January 2017

Class	Room	Lab
PY104	136	TBA
PY105	134	Position Velocity Acceleration
PY211	B3	Projectile Motion
PY212		No Lab This Week
PY242	B1	E-Fields & Potentials
PY252	B15	Coulomb's Law & Charge
PY313	B11	Millikan Oil Drop
PY352	B15	Oscilloscope Lab
ITOP	136	TBA

Announcements

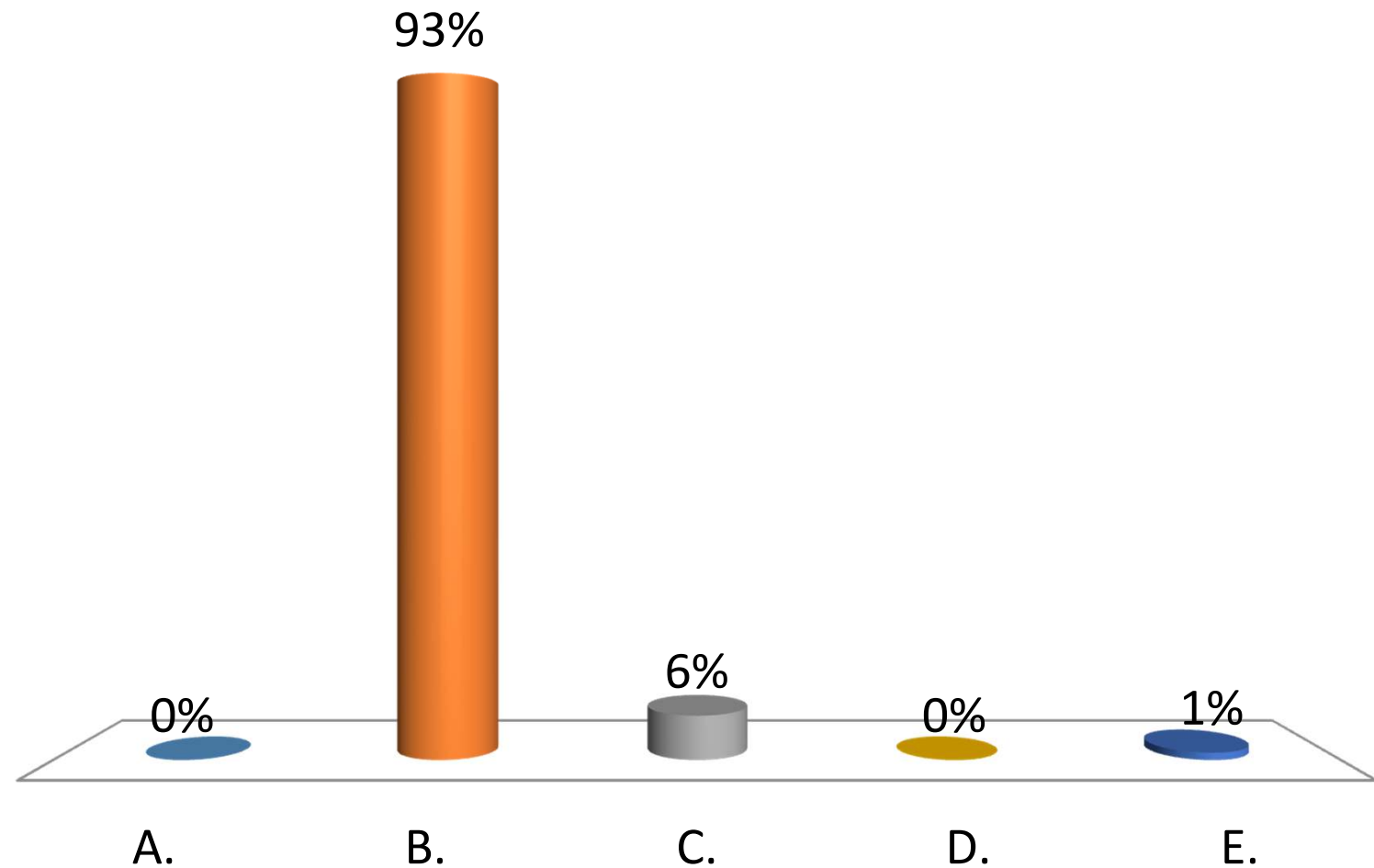
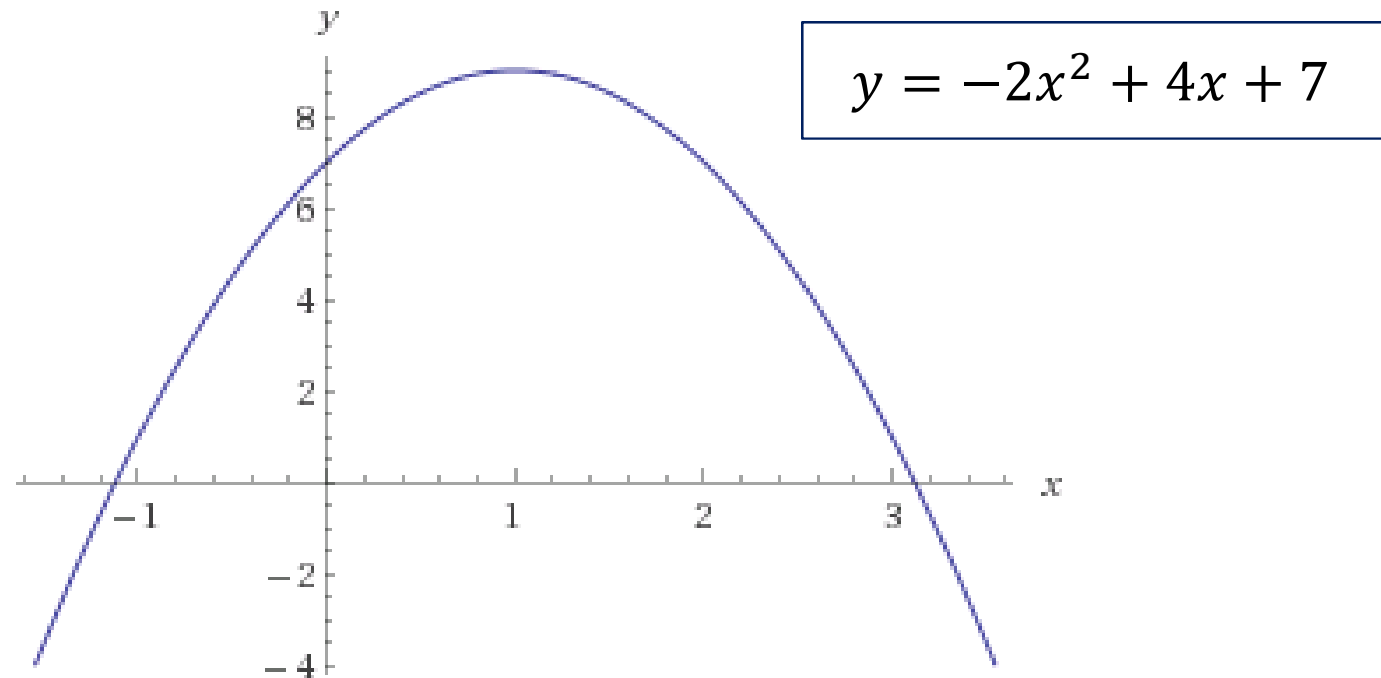
- Homework 2: due tomorrow!
 - Office hours today + tomorrow, 4-6pm.
 - Piazza is full of smart people that can answer your questions!
- Office hours (me): today & tomorrow (Mon & Tue) 4-6pm in SCI-121
- Office hours (TFs & LAs): tell them what times you'd prefer

Plan for today!

- Do some example problems
- Give you some hints for the homework
 - Useful equation for HW 2, problem 10

What is the name of this curve?

- A. Straight line
- B. Parabola
- C. Hyperbola
- D. Cubic
- E. None of the above



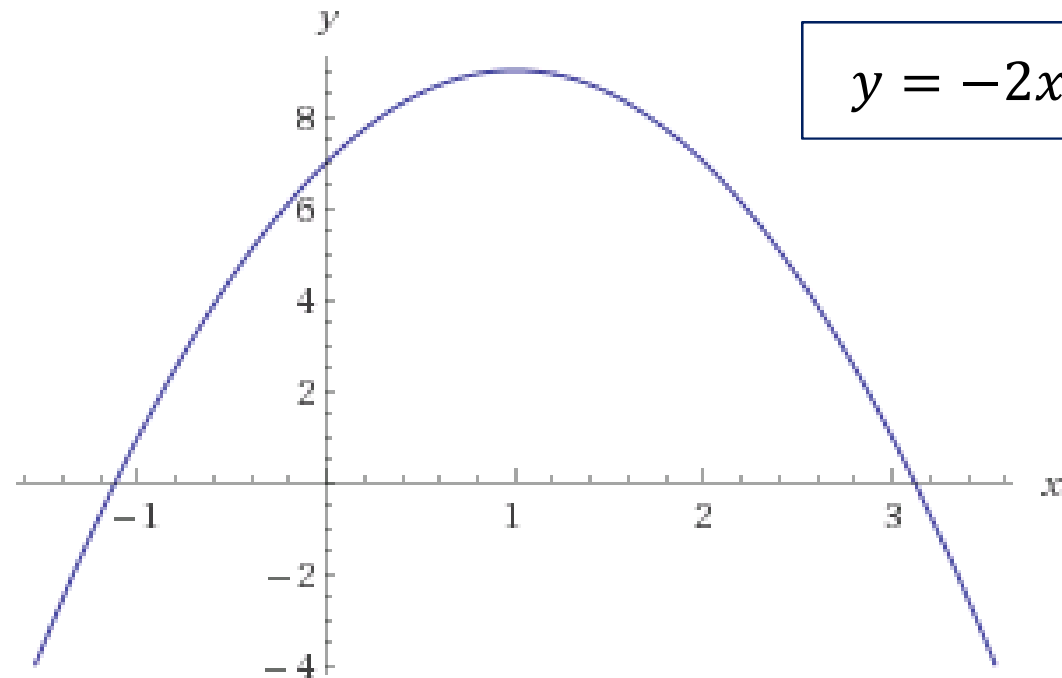
What is the name of this curve?

- A. Straight line
- B. Parabola**
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If you make a graph of a **quadratic equation**,

$$y = ax^2 + bx + c$$

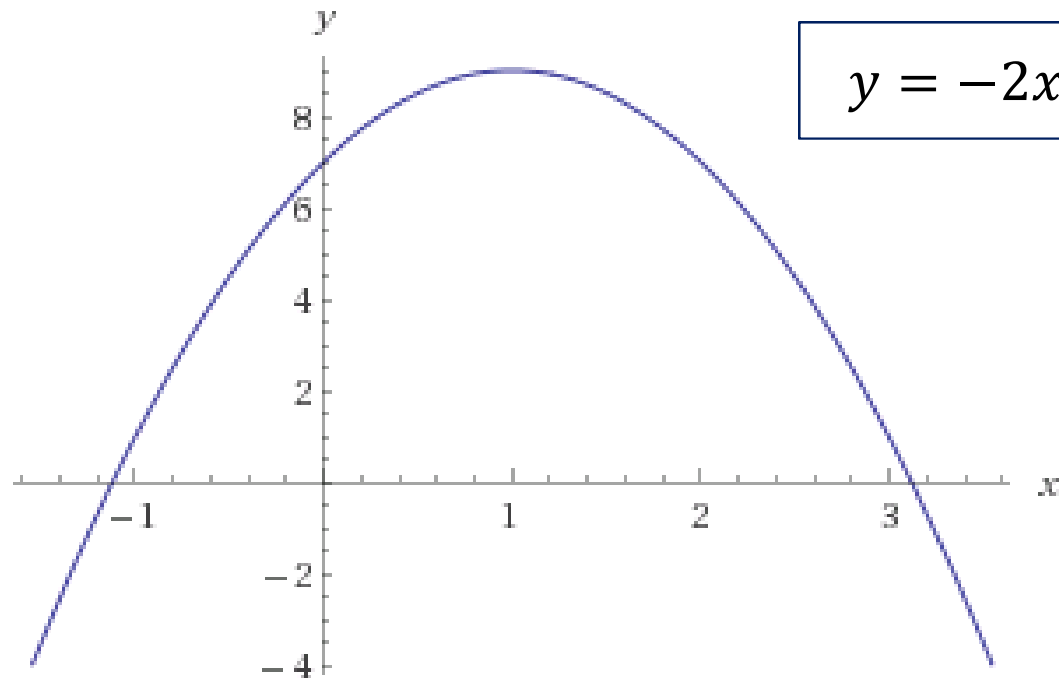
then the shape of that curve is a **parabola**.



$$y = -2x^2 + 4x + 7$$

What is the name of this curve?

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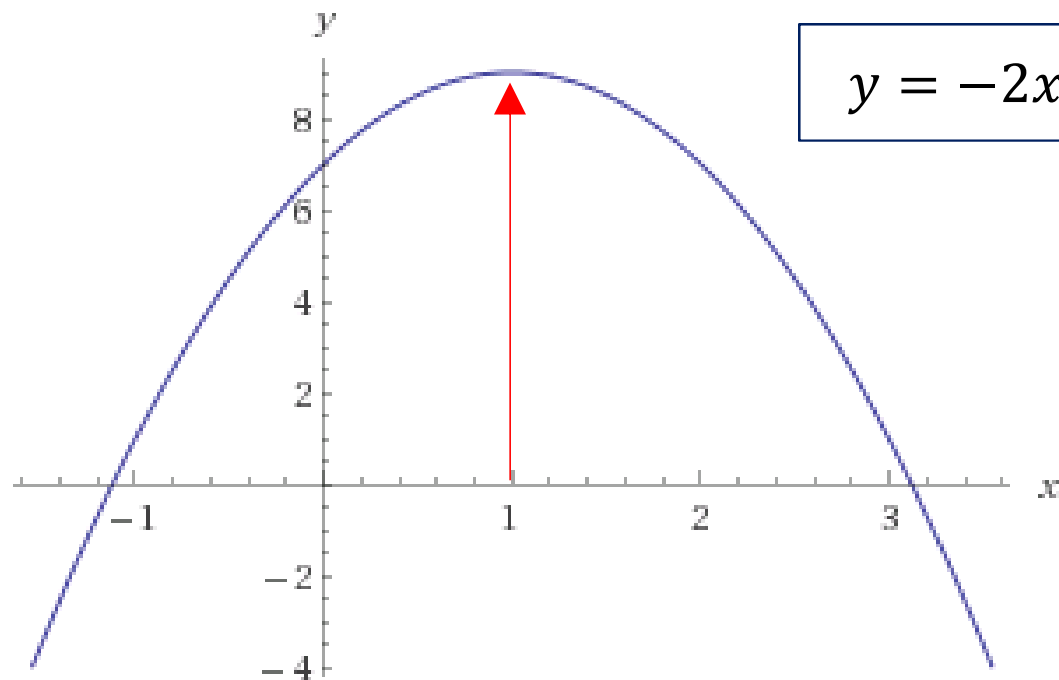
The maximum (or minimum) of a parabola is at:

$$x_{\max} = -\frac{b}{2a}$$

(easy to show using derivatives – or just memorize)

What is the name of this curve?

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In this case:

$$x_{\max} = -\frac{4}{2(-2)} = 1$$

What is the name of this curve?

A. Straight line

B. Parabola

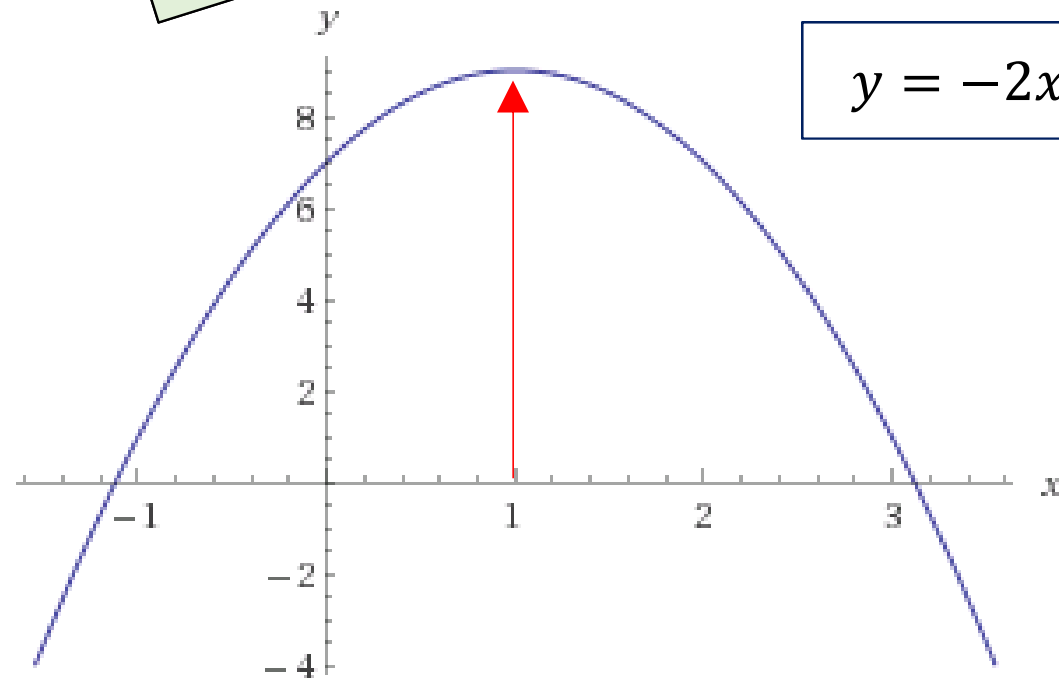
C. Hyperbola

D. Circle

E. None of the above

Quadratic equations and parabolas occur frequently in problems with kinematics

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The kinematic equations

Assuming *constant acceleration* a :

- Position x of object at time t : $x = x_i + v_i t + \frac{1}{2}at^2$
- Speed v of object at time t : $v = v_i + at$
- Also useful, when you don't care about time t : $v^2 = v_i^2 + 2a(x - x_i)$

The kinematic equations

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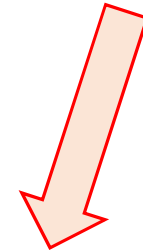
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Combine equations,
eliminate t ,
and solve for v



- Also useful, when you don't care about time t :

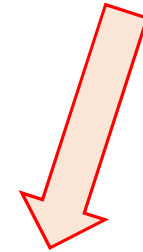
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Let's consider some examples!

Most awesome example of kinematics



Lamborghini Diablo

Capable of accelerating
from 0-60 mph in 5.4 seconds!

Most awesome example of kinematics



Lamborghini Diablo

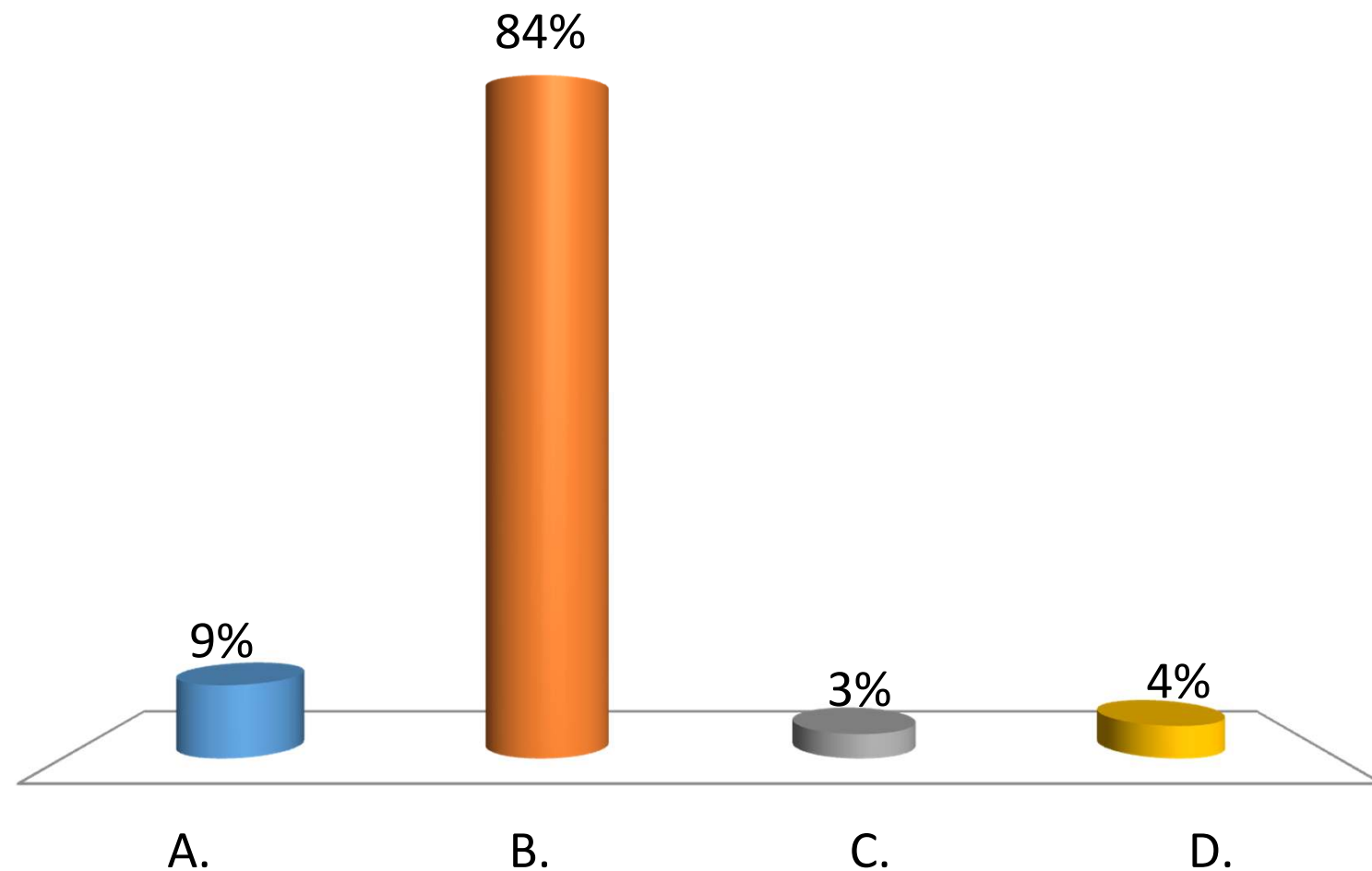
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What is its acceleration in m/s^2 ?

Which equation should we use?

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- B. Use $v = v_i + at$
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Diablo does 0-60 mph in 5.4 sec.
What is its acceleration in m/s²?



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- D. None of the above, use something else

But why?

Diablo does 0-60 mph in 5.4 sec.
What is its acceleration in m/s²?

How fast does a Lamborghini Diablo accelerate?



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What is its acceleration in m/s^2 ?

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How to solve a physics problem:

1. Make a list of things given to us, and what we are looking for.
(And convert to SI units!)
2. Find the right equation(s).
3. Solve!

How fast does a Lamborghini Diablo accelerate?



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- Initial speed: $v_i = 0$
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Convert mph to m/s:

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Convert mph to m/s:

$$v = \frac{60 \text{ miles}}{\text{hour}} \times \frac{1609.34 \text{ m}}{1 \text{ mile}} \times \frac{1 \text{ hour}}{60 \text{ min}} \times \frac{1 \text{ min}}{60 \text{ sec}}$$

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- Initial speed: $v_i = 0$
- Speed at time $t = 5.4 \text{ s}$: $v = 60 \text{ mph} = 26.822 \text{ m/s}$
- Looking for: a

Convert mph to m/s:

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$$26.822 = 0 + a(5.4)$$

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- Looking for: a

$$v = v_i + at$$
$$26.822 = 0 + a(5.4)$$

$$a = 4.97 \text{ m/s}^2$$

Maybe that problem was too simple,
but it gives you an idea of what the best approach is.

Example problem #2a

You drop a coin in a wishing well. After 3 seconds you hear a "plop". How deep is the well?



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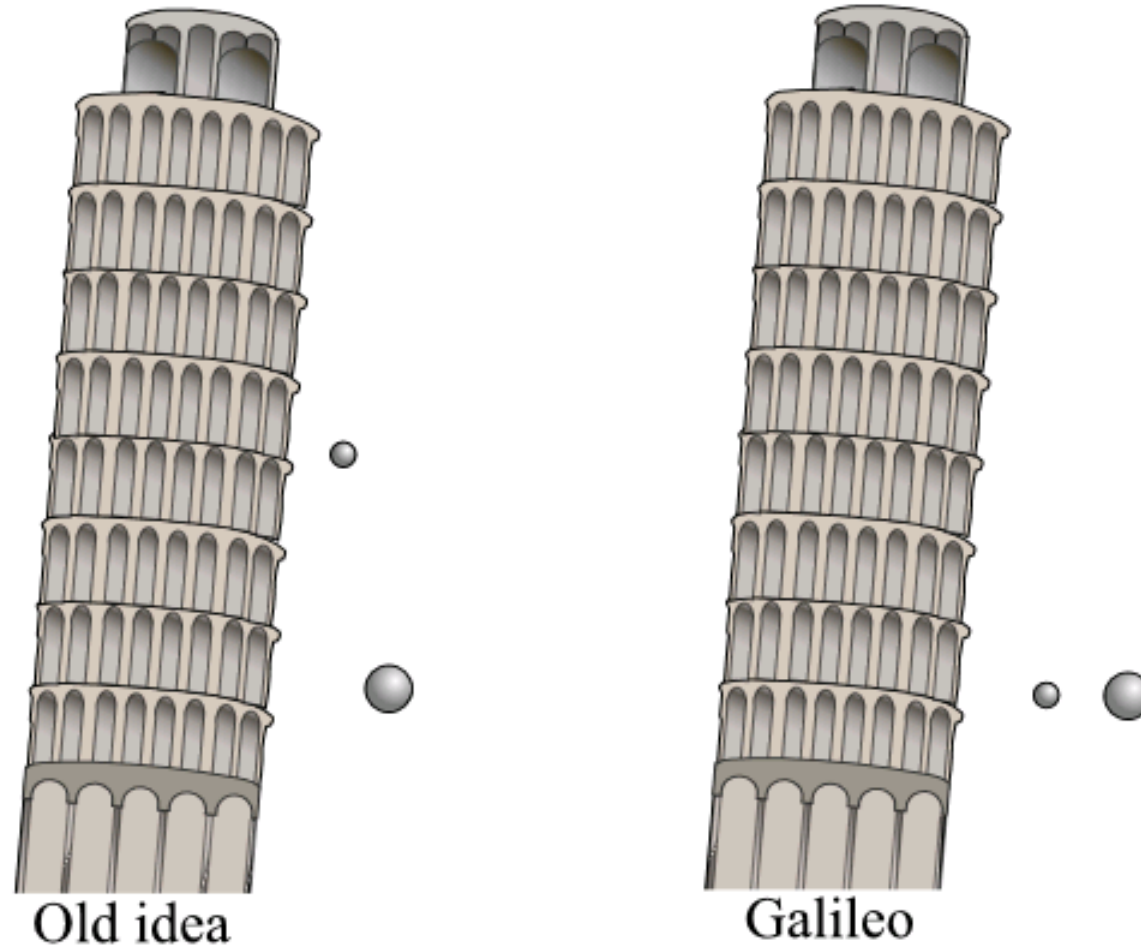
NOTICE: you do not need to know how heavy the coin is!

Any object (regardless of its mass)
falls with the same acceleration to the ground*



* if we'd ignore air resistance

Galileo's Leaning Tower of Pisa experiment



Didn't really happen,
but still makes a great story.

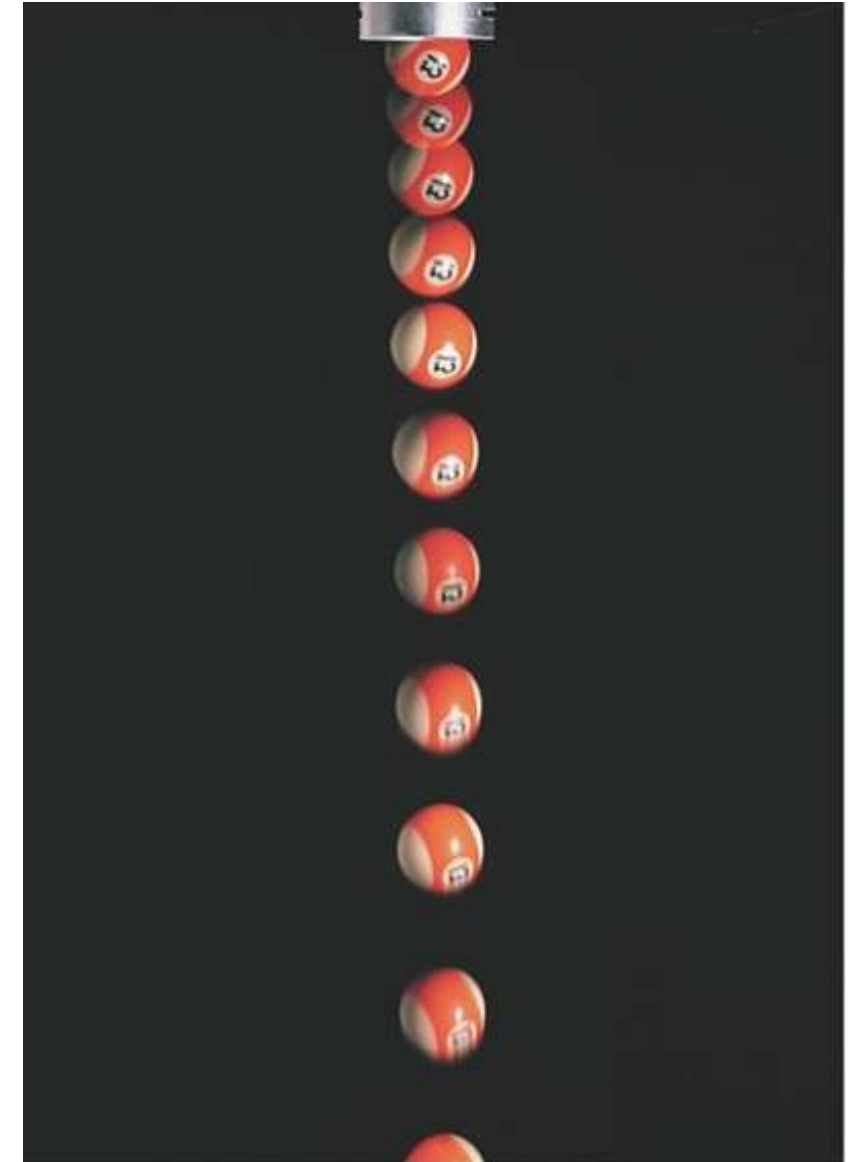
Gravity!

- When an object falls, it always accelerates with a constant acceleration of

$$a_{\text{gravity}} = 9.81 \text{ m/s}^2$$

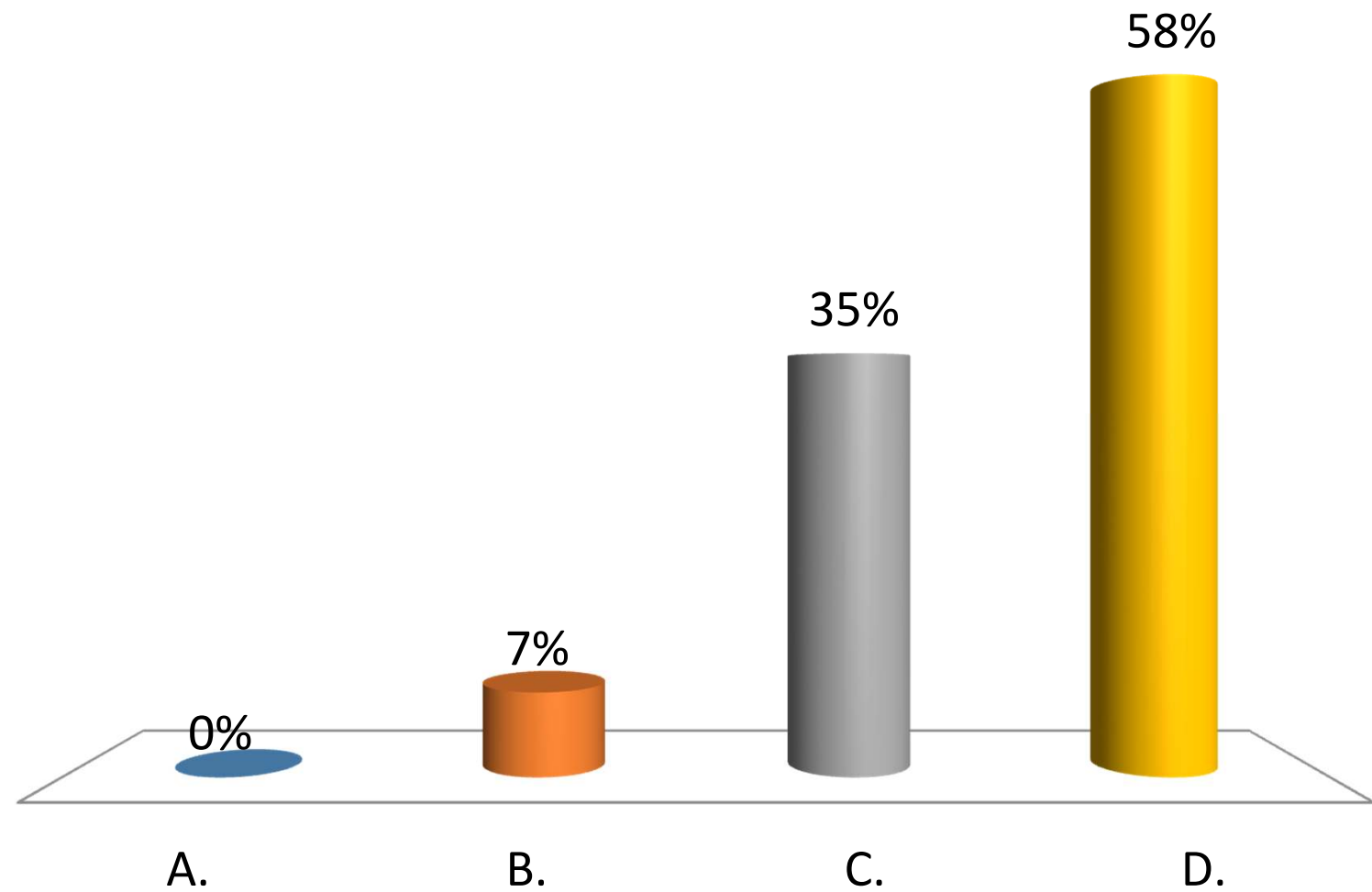
- We will use this number a lot, so we give it a special symbol:

$$g = 9.81 \text{ m/s}^2$$



Which object hits the bottom first?

- A. Feather first
- B. Coin first
- C. Both at the same time
- D. It depends



Which object hits the bottom first?

- A. Feather first
- B. Coin first <-- if there's air
- C. Both at the same time <-- without air!
- D. It depends



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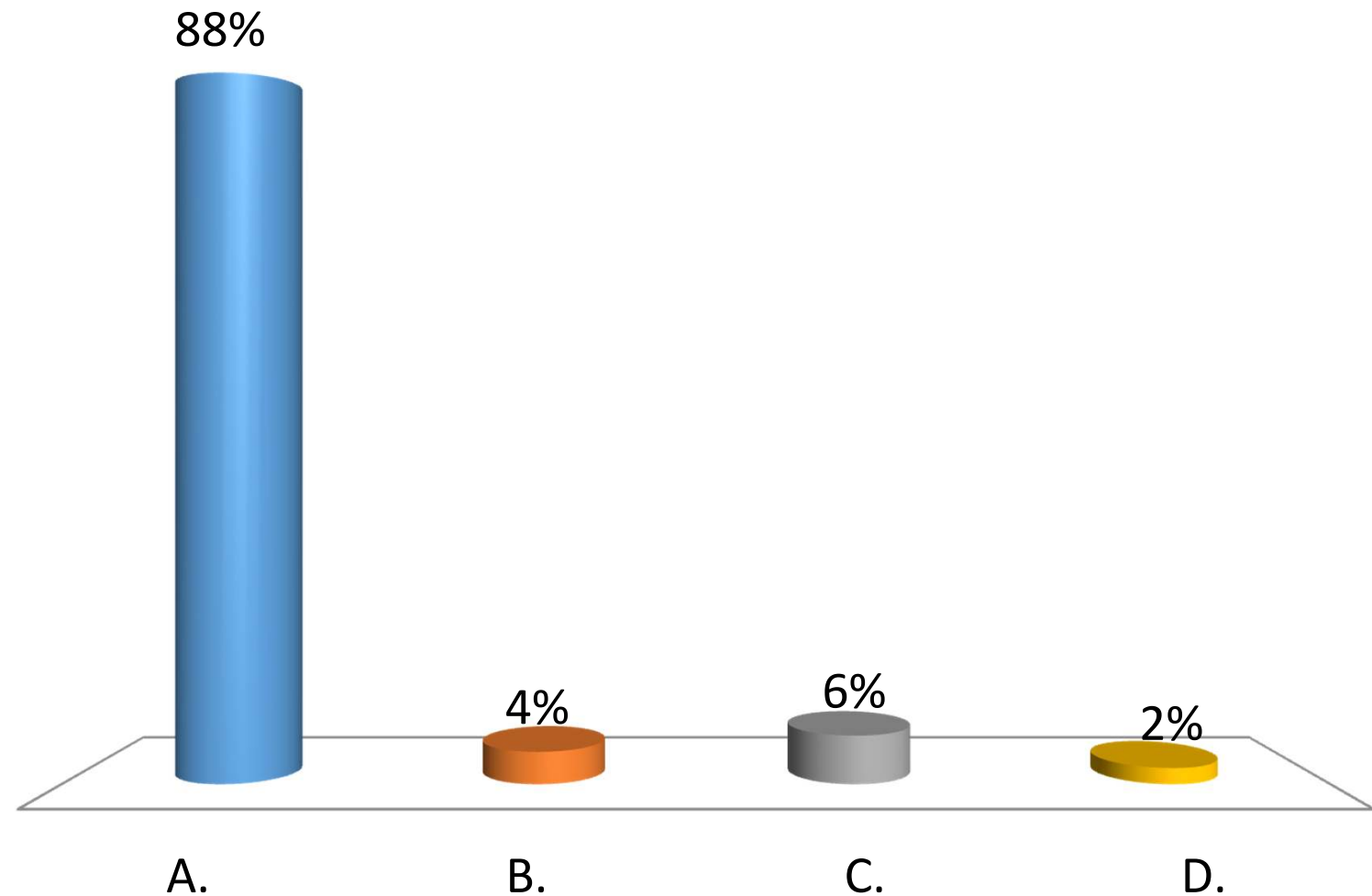
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List of things given / to find:

- You "drop" the coin (not thrown): $v_i = 0$
- Time between drop and plop: $t = 3 \text{ sec.}$
- We are looking for a distance: y
- We are free to choose $y_i = 0$
- Coin accelerates because of gravity: $a = 9.81 \text{ m/s}^2 \text{ (down)}$

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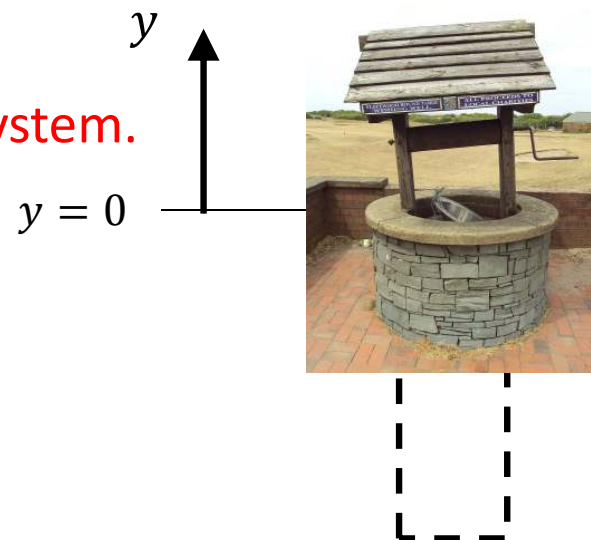
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Choose a coordinate system.



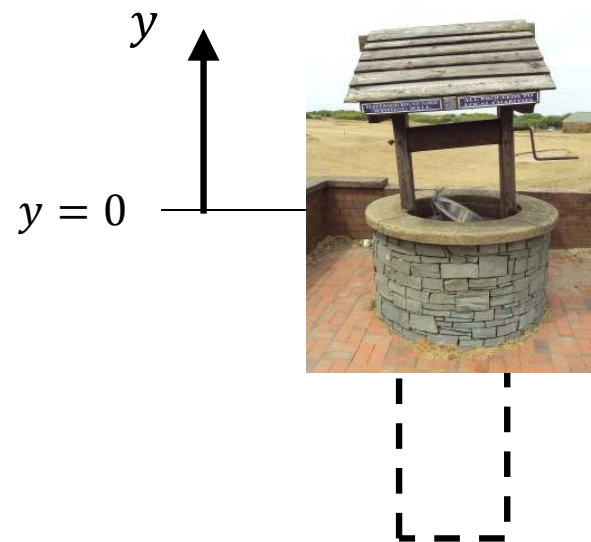
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$$y = y_i + v_i t + \frac{1}{2}at^2$$

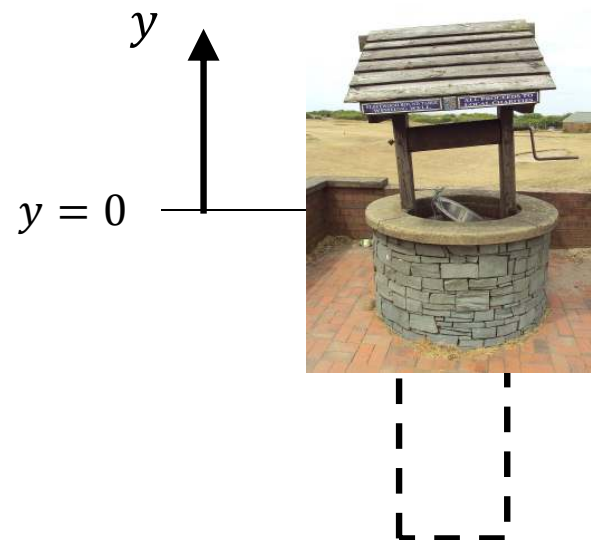
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$$\begin{aligned} y &= y_i + v_i t + \frac{1}{2}at^2 \\ &= 0 + (0)(3) + \frac{1}{2}(-9.81)(3)^2 \end{aligned}$$

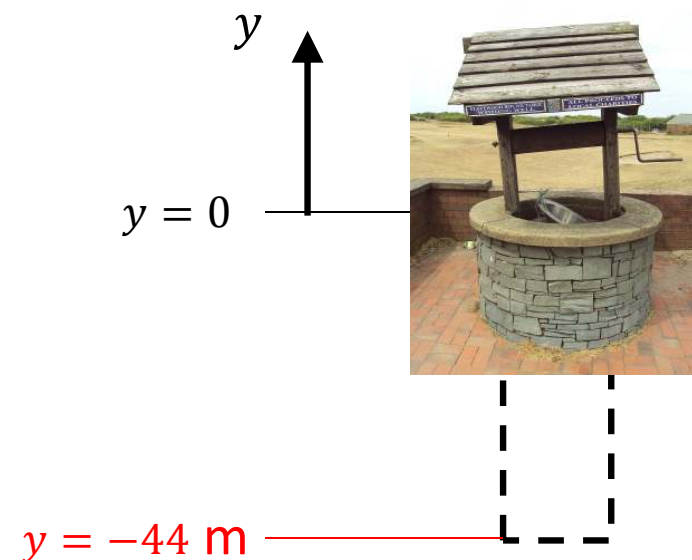
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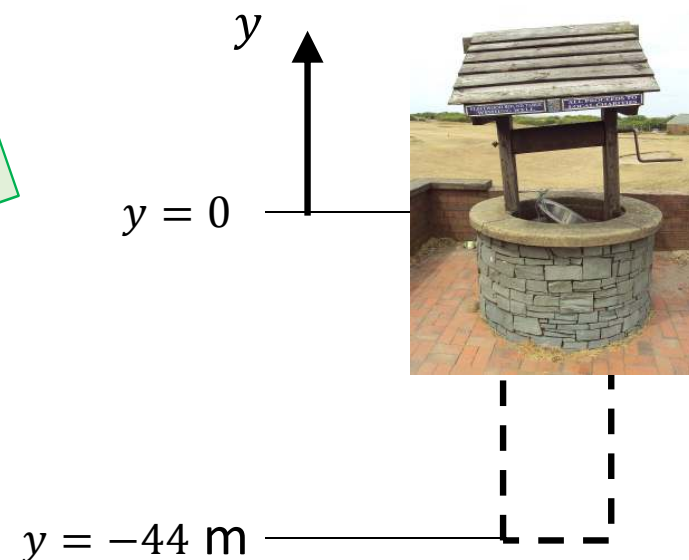
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We could have chosen a smarter coordinate system!



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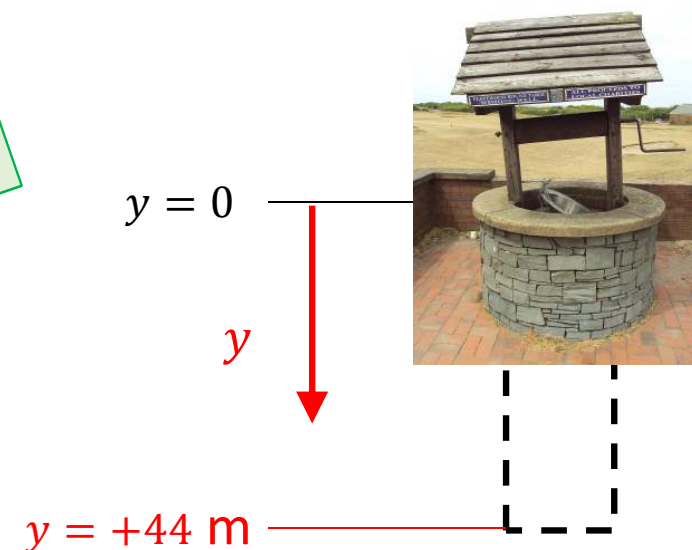
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We could have chosen a smarter coordinate system!



$$\begin{aligned} y &= y_i + v_i t + \frac{1}{2}at^2 \\ &= 0 + (0)(3) + \frac{1}{2}(+9.81)(3)^2 \\ &= +44.15 \text{ m} \end{aligned}$$

- Another one!

Example problem #2b

You drop a coin in a wishing well. After 3 seconds you hear a "plop".
How fast does it hit the water?



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List of things given / to find:

- You "drop" the coin (not thrown): $v_i = 0$
- Time between drop and plop: $t = 3 \text{ sec.}$
- We are looking for a speed: v
- We are free to choose $y_i = 0$
- Coin accelerates because of gravity: $a = 9.81 \text{ m/s}^2 \text{ (down)}$



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$$x = x_i + v_i t + \frac{1}{2} a t^2$$

$$v = v_i + a t$$

$$v^2 = v_i^2 + 2a(x - x_i)$$



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If you choose up to be positive:

$$v = 0 + (-9.81)(3) = -29.4 \text{ m/s} \quad (29.4 \text{ m/s going down})$$



- One more!

Example problem 3

You throw a ball straight up into the air, releasing it with a speed of 30 m/s. Assuming $g = 10 \text{ m/s}^2$, you catch the ball 6.0 seconds later at the same point from which you let it go. Neglect air resistance.

How high does the ball go?

Example problem 3

You throw a ball straight up into the air, releasing it with a speed of 30 m/s. Assuming $g = 10 \text{ m/s}^2$, you catch the ball 6.0 seconds later at the same point from which you let it go. Neglect air resistance.

How high does the ball go?

List of things given / to find:

- You throw the ball up: $v_i = 30 \text{ m/s}$ (up)
- Total time: $t = 6 \text{ sec}$.
- We are looking for a height: y
- We are free to choose $y_i = 0$
- Ball accelerates because of gravity: $a = g = 10 \text{ m/s}^2$ (down)

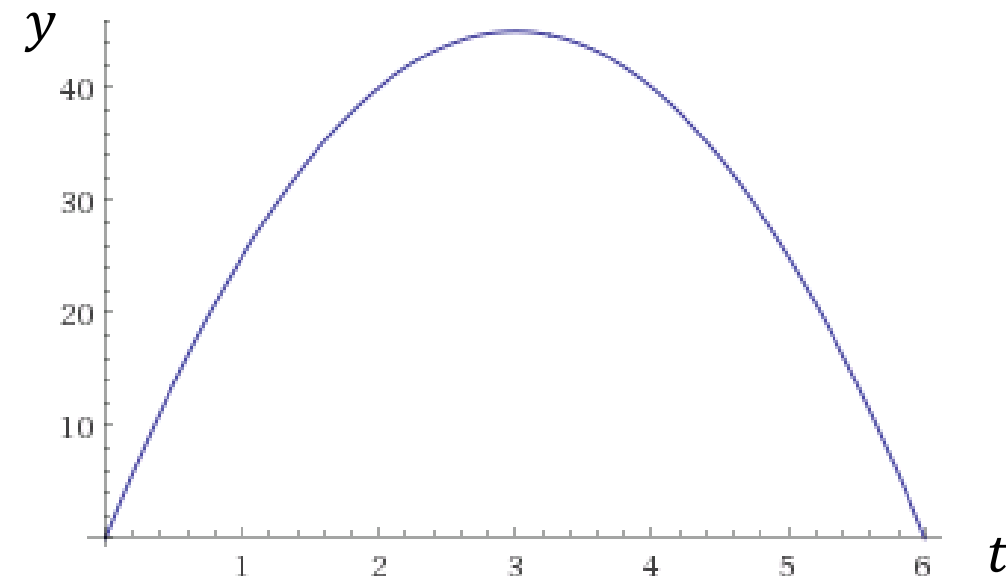
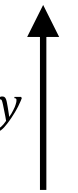
$$x = x_i + v_i t + \frac{1}{2} a t^2$$

$$v = v_i + a t$$

$$v^2 = v_i^2 + 2a(x - x_i)$$

Where the ball is at time t , is given by:

$$y = y_i + v_i t - \frac{1}{2} g t^2$$



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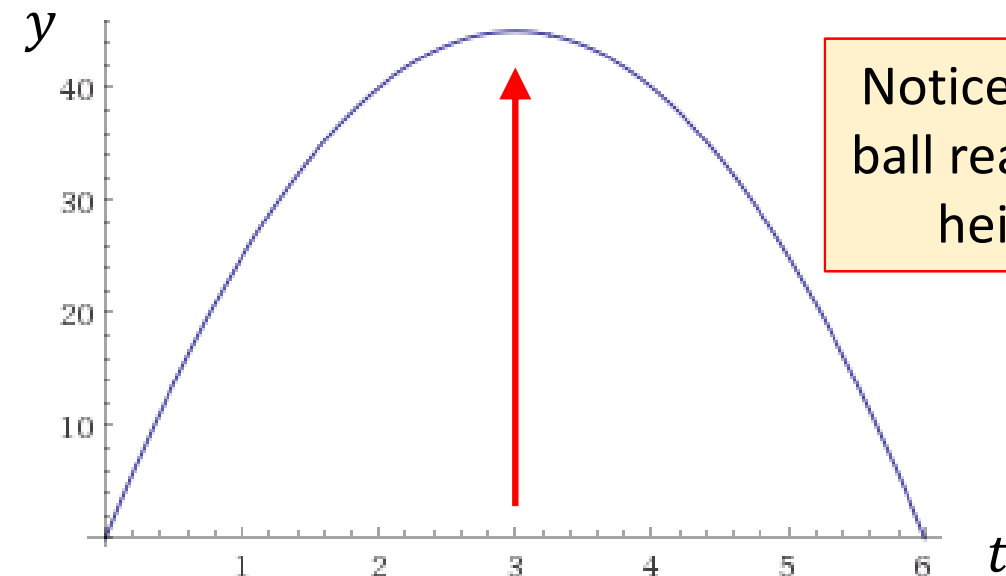
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y ↑



Notice the symmetry:
ball reaches maximum
height at 3 sec.

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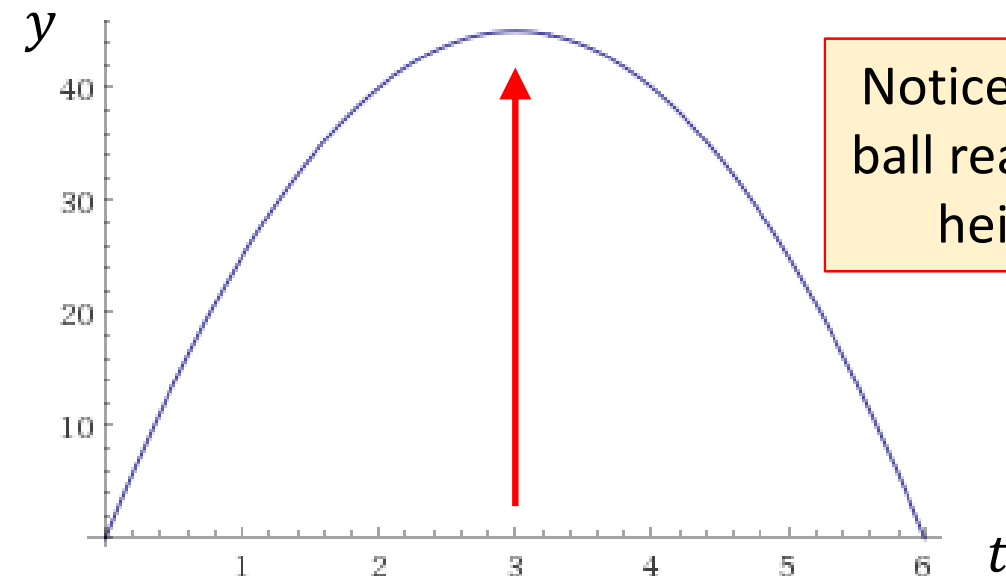
$$v = v_i + a t$$

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$$y = y_i + v_i t - \frac{1}{2} g t^2 = 0 + (30)(3) - \frac{1}{2}(10)(3^2) = 90 - 45 = 45 \text{ m}$$

Where the ball is at time t , is given by:

$$y = y_i + v_i t - \frac{1}{2} g t^2$$



Notice the symmetry:
ball reaches maximum
height at 3 sec.

- Time for another one?

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How high does the ball go?

How fast does it hit the ground?

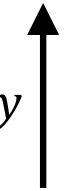
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$$v = v_i + a t = 30 - (10)(6) = -30 \text{ m/s}$$

- Come to office hours if you have more questions:
 - Today 4-5pm in SCI-121
- Or ask on Piazza!
- HW 2 is due tomorrow at midnight (Tuesday 31 Jan at 11:59pm)

Thank you!

See you next time: Wednesday 1 Feb. at 2:30pm