**Question 1** Prove that the sum of an irrational number and a rational number is irrational.

**Question 2** Show that these statements about the integer x are equivalent: (i) 3x + 2 is even, (ii) x + 5 is odd, (iii)  $x^2$  is even.

**Question 3** Prove the triangle inequality, which states that if x and y are real numbers, then  $|x| + |y| \ge |x + y|$ .

**Question 4** Prove that there are 100 consecutive positive integers that are not perfect squares. Is your proof constructive or nonconstructive?