

**Name:**

**Collaborators:**

**Outside resources:**

Math 2106, Foundations of Mathematical Proof  
HW 1 — Due January 20, 2017 (Fri)

Turn in the following problems from Hammack's book.

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|------------------------|-------------------|
| 1.1: 16, 28, 52        | 2.3: 2, 6, 10, 12 |
| 1.2: 20                | 2.5: 10           |
| 1.3: 2, 10, 14         | 2.6: 12, 14       |
| 1.4: 6, 14, 16, 18, 20 | 2.7: 4, 6, 8, 10  |
| 1.8: 4, 8, 14          | 2.9: 6, 10        |
|                        | 2.10: 4, 6, 8     |

**Additional exercises** (to be turned in)

A1 Describe the following sets using the set builder notation.

- (a) the set of odd integers
- (b) the set of rational numbers that may be written with denominator greater than 100
- (c) the set of rational numbers that may be written with positive denominator less than 4

A2 Using truth tables, prove that each of the following compound propositions is a tautology.

- (a)  $[p \wedge (p \Rightarrow q)] \Rightarrow q$
- (b)  $[\sim q \wedge (p \Rightarrow q)] \Rightarrow \sim p$
- (c)  $[(p \Rightarrow q) \wedge (q \Rightarrow r)] \Rightarrow (p \Rightarrow r)$
- (d)  $[(p \vee q) \wedge \sim p] \Rightarrow q$

*These implications are four of the most important “rules of inference” in propositional logic. Each rule gives a conclusion which follows logically from a set of hypotheses. As such, these rules are the building blocks of a correct proof.*

A3 Prove that each of the following propositions is *not* a tautology, with or without using truth tables.

- (a)  $[(p \Rightarrow q) \wedge q] \Rightarrow p$
- (b)  $[(p \Rightarrow q) \wedge \sim p] \Rightarrow \sim q$

*These implications are common logical fallacies (errors in reasoning) since the conclusion does not follow logically from the set of hypotheses.*