

LLVM passes and Intro to Loop Transformation Frameworks

Announcements

- This class is recorded and will be in D2L panapto.
- No quiz Monday after spring break.
- Will be doing mid-semester class feedback.

Today

- LLVM passes
- Skewing Smith-Waterman
- Automating transformations like skewing
 - Iteration space representation
 - Transformation representation
 - Applying the transformation to the iteration space
 - Generating code for the new iteration space

LLVM Passes: Example Skeleton Pass

LLVM documentation

- on writing a pass
- assumes you have control over the llvm source hierarchy

Skeleton example (running it on rose computer)

- `git clone https://github.com/sampsyo/llvm-pass-skeleton.git`
- `cd llvm-pass-skeleton`
- Edit the Skeleton.cpp file
- In llvm-pass-skeleton:
 - `mkdir build; cd build; cmake ..; make VERBOSE=1`
 - Create a test.c file.
 - `clang -S -emit-llvm test.c`
 - `opt -load build/skeleton/libSkeletonPass.so -skeleton < test.ll > /dev/null`

Then what?

LLVM 3.9.1 documentation

- <http://releases.llvm.org/3.9.0/docs/>
- Programmers Manual

Helpful Hints for Common Operations

- <http://releases.llvm.org/3.9.0/docs/ProgrammersManual.html>
- Iterate over basic blocks in a function
- Iterate in instructions in a basic block
- Creating and inserting new Instructions
- Deleting instructions
- Etc.

The Core LLVM Class hierarchy

- Instruction class
- Value class

Automating Loop Transformations with Frameworks

Currently

- Frameworks used *in compiler* to ...
 - abstract loops, memory accesses, and data dependences in loop
 - specify the effect of a sequence of loop transformations on the loop, its memory accesses, and its data dependences
 - generate code from the transformed loop
- Loop transformations affect the *schedule* of the loop

Future

- How can framework technology be exposed in the programming model?

Frameworks we will discuss this semester

- Unimodular
- Polyhedral
- Presburger
- Sparse Polyhedral

Protein String Matching Example (smithWaterman.c)

```
for (i=1;i<=a[0];i++) {
    for (j=1;j<=b[0];j++) {
        diag      = h[i-1][j-1] + sim[a[i]][b[j]];
        down      = h[i-1][j] + DELTA;
        right     = h[i][j-1] + DELTA;
        max=MAX3(diag,down,right);
        if (max <= 0) {
            h[i][j]=0; xTraceback[i][j]=-1; yTraceback[i][j]=-1;
        } else if (max == diag) {
            h[i][j]=diag; xTraceback[i][j]=i-1; yTraceback[i][j]=j-1;
        } else if (max == down) {
            h[i][j]=down; xTraceback[i][j]=i-1; yTraceback[i][j]=j;
        } else {
            h[i][j]=right; xTraceback[i][j]=i; yTraceback[i][j]=j-1;
        }
        if (max > Max){
            Max=max; xMax=i; yMax=j;
        }
    }
}
```

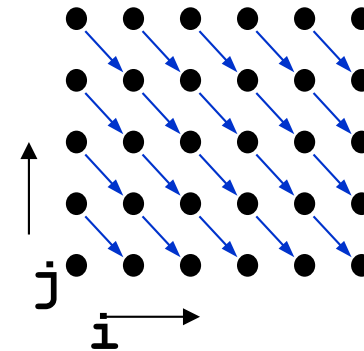
Skewing (smithWaterman.c)

```
// Let j'=i+j and i'=i.
for (i'=1;i'<=a[0];i'++) {
    for (j'=i'+1;j'<=i'+b[0];j'++) {
        diag      = h[i'-1][j'-i'-1] + sim[a[i']][b[j'-i']];
        down      = h[i'-1][j'-i']   + DELTA;
        right     = h[i'][j'-i'-1]   + DELTA;
        max=MAX3(diag,down,right);
        if (max <= 0) {
            h[i'][j'-i']=0; xTraceback[i'][j'-i']=-1; yTraceback[i'][j'-i']=-1;
        } else if (max == diag) {
            h[i'][j'-i']=diag; xTraceback[i'][j'-i']=i'-1;
            yTraceback[i'][j'-i']=j'-i'-1;
        } else if (max == down) {
            h[i'][j'-i']=down; xTraceback[i'][j'-i']=i'-1;
            yTraceback[i'][j'-i']=j'-i';
        } else {
            h[i'][j'-i']=right; xTraceback[i'][j'-i']=i';
            yTraceback[i'][j'-i']=j'-i'-1;
        }
        if (max > Max){ Max=max; xMax=i'; yMax=j'-i';
        }
    }
}
```

Iteration Space Representation

Original code

```
do i = 1, 6
  do j = 1, 5
    A(i, j) = A(i-1, j+1) + 1
  enddo
enddo
```



Represent the iteration space

- As an intersection of inequalities
- The iteration space is the integer tuples within the intersection

Bounds:

$$\begin{array}{lll} 1 & \leq & i \\ i & \leq & 6 \\ 1 & \leq & j \\ j & \leq & 5 \end{array}$$

$$\begin{bmatrix} -1 & 0 \\ 1 & 0 \\ 0 & -1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} i \\ j \end{bmatrix} \leq \begin{bmatrix} -1 \\ 6 \\ -1 \\ 5 \end{bmatrix}$$

Lexicographical Order as Schedule

Iteration point

- Integer tuple with dimensionality d

$$(i_0, i_1, \dots, i_d)$$

Lexicographical Order

- First order the iteration points by i_0 , then i_1 , ... and finally i_d .

$$(i_0, i_1, \dots, i_{d-1}) \prec (j_0, j_1, \dots, j_{d-1}) \equiv \\ (i_0 < j_0) \vee (i_0 = j_0 \wedge i_1 < j_1) \vee \dots (i_0 = j_0 \wedge i_1 = j_1 \wedge \dots i_{d-1} < j_{d-1})$$

Frameworks for Loop Transformations

Loop Transformations as functions

$$\vec{i}' = f(\vec{i})$$

Unimodular Loop Transformations [Banerjee 90], [Wolf & Lam 91]

- can represent loop permutation, loop reversal, and loop skewing
- unimodular linear mapping (determinant of matrix is + or - 1)

$$\vec{i}' = T\vec{i}$$

- T is a matrix, i and i' are iteration vectors
- example

$$\begin{bmatrix} i' \\ j' \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} i \\ j \end{bmatrix}$$

- limitations
 - only perfectly nested loops
 - all statements are transformed the same

Loop Skewing

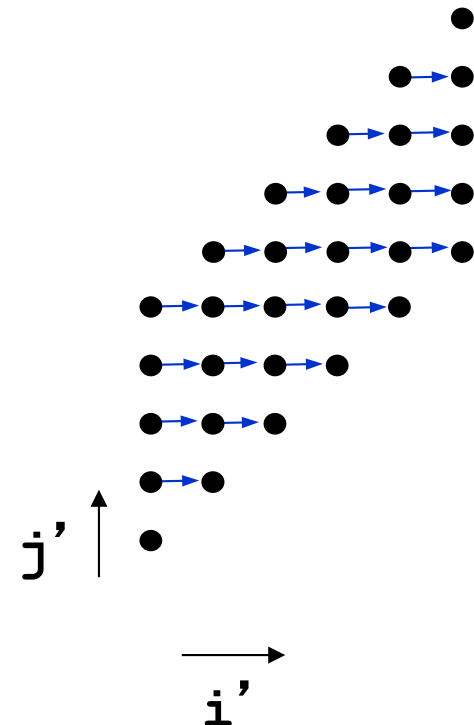
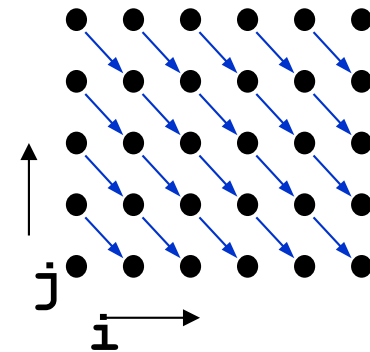
Original code

```
do i = 1,6
  do j = 1,5
    A(i,j) = A(i-1,j+1)+1
  enddo
enddo
```

Distance vector: (1, -1)

Skewing:

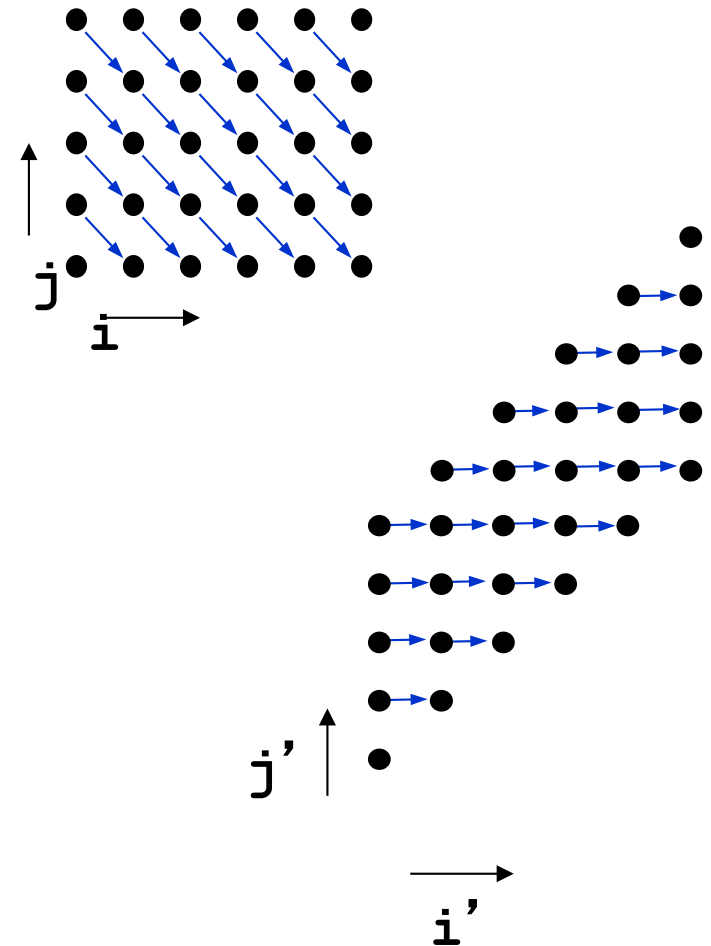
$$\begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} i \\ j \end{bmatrix} = \begin{bmatrix} i \\ i + j \end{bmatrix}$$



Transforming the Dependences and Array Accesses

Original code

```
do i = 1,6
  do j = 1,5
    A(i,j) = A(i-1,j+1)+1
  enddo
enddo
```



Dependence vector:

$$\begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} 1 \\ -1 \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

New Array Accesses:

$$A\left(\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} i \\ j \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \end{bmatrix}\right) = A(i, j)$$

$$A\left(\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} i' \\ j' \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \end{bmatrix}\right) = A(i', j' - i')$$

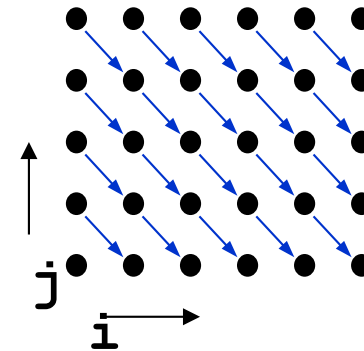
$$A\left(\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} i \\ j \end{bmatrix} + \begin{bmatrix} -1 \\ 1 \end{bmatrix}\right) = A(i - 1, j + 1)$$

$$A\left(\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} i' \\ j' \end{bmatrix} + \begin{bmatrix} -1 \\ 1 \end{bmatrix}\right) = A(i' - 1, j' - i' + 1)$$

Transforming the Loop Bounds

Original code

```
do i = 1, 6
  do j = 1, 5
    A(i, j) = A(i-1, j+1) + 1
  enddo
enddo
```



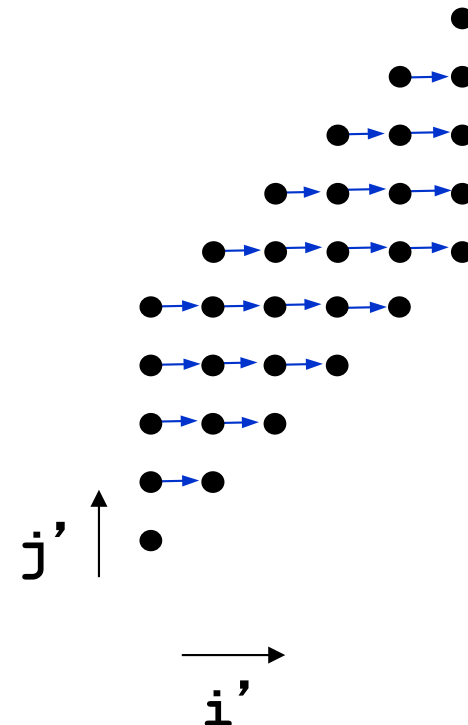
Bounds:

$$\begin{bmatrix} -1 & 0 \\ 1 & 0 \\ 0 & -1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} i \\ j \end{bmatrix} \leq \begin{bmatrix} -1 \\ 6 \\ -1 \\ 5 \end{bmatrix}$$

$$\begin{bmatrix} -1 & 0 \\ 1 & 0 \\ 0 & -1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} i' \\ j' \end{bmatrix} \leq \begin{bmatrix} -1 \\ 6 \\ -1 \\ 5 \end{bmatrix}$$

Transformed code

```
do i' = 1, 6
  do j' = 1+i', 5+i'
    A(i', j'-i') = A(i'-1, j'-i'+1) + 1
  enddo
enddo
```



Revisiting (smithWaterman.c)

```
for (i=1;i<=a[0];i++) {  
    for (j=1;j<=b[0];j++) {  
        diag      = h[i-1][j-1] + sim[a[i]][b[j]];  
        down      = h[i-1][j]   + DELTA;  
        right     = h[i][j-1]   + DELTA;  
        ...  
    }  
}
```

Let $j'=i+j$ and $i'=i$.

```
for (i'=1;i'<=a[0];i'++) {  
    for (j'=i'+1;j'<=i'+b[0];j'++) {  
        diag      = h[i'-1][j'-i'-1] + sim[a[i']][b[j'-i']];  
        down      = h[i'-1][j'-i']   + DELTA;  
        right     = h[i'][j'-i'-1]   + DELTA;  
        ...  
    }  
}
```

Transformation Legality

Recall ...

- A dependence vector is legal if it is lexicographically non-negative.
- Applying the transformation function to each dependence vector produces a dependence vector for the new iteration space.

When is a transformation legal assuming a lexicographical schedule?

What about parallelism?

Skewing smithWaterman.c (Is this transformation legal?)

```
for (i=1;i<=a[0];i++) {  
    for (j=1;j<=b[0];j++) {  
        diag      = h[i-1][j-1] + sim[a[i]][b[j]];  
        down      = h[i-1][j]   + DELTA;  
        right     = h[i][j-1]   + DELTA;  
        ...  
    }  
}
```

Let $j'=i$ and $i'=i+j$.

Thus $i=j'$ and $j=i'-j'$.

```
for (i'=2;i'<=a[0]+b[0];i'++) {  
    for (j'=max(1,i'-b[0]); j'<=min(a[0],i'-1); j'++) {  
        diag      = h[j'-1][i'-j'-1] + sim[a[i']][b[i'-j']];  
        down      = h[j'-1][i'-j']   + DELTA;  
        right     = h[j'] [i'-j'-1]  + DELTA;  
        ...  
    }  
}
```

Converting C loops to iteration space representation

Analyses needed

- Loop analysis
 - Loop bounds from AST or control-flow graph
 - Induction variable detection
- Pointer analysis
 - Do pointers point at same or overlapping memory?
 - Note that in C can cast a pointer to an integer and back and can do pointer arithmetic.
 - In general requires whole program analysis.
- Dependence analysis

Is this even possible?

- Current tools make the optimistic pointer assumption
- We need programming models that simplify or remove the need for such analyses

Concepts

Parallelism and Memory Usage tradeoff

Transformation Frameworks

- Representing the iteration space
- Representing transformations
- Applying transformations to the iteration space, dependences, and array accesses
- Testing the legality of a transformation

Compiler analyses needed in C to obtain an iteration space representation

References

[Banerjee90] Uptal Banerjee, “Unimodular transformations of double loops,” In Advances in Languages and Compilers for Parallel Computing, 1990.

[Wolf & Lam 91] Wolf and Lam, “A Data Locality Optimizing Algorithm,” In Programming Languages Design and Implementation, 1991.

Next Time

Reading assignment

- Unifying Framework for Iteration Reordering Transformations by Kelly and Pugh (read all but Section 5)

Lecture

- More loop transformation frameworks