



Introduction to Computer Graphics with WebGL

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Programming with WebGL

Part 3: Shaders

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Objectives

- Simple Shaders
 - Vertex shader
 - Fragment shaders
- Programming shaders with GLSL
- Finish first program



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Vertex Shader Applications

- Moving vertices
 - Morphing
 - Wave motion
 - Fractals
- Lighting
 - More realistic models
 - Cartoon shaders



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Fragment Shader Applications

Per fragment lighting calculations



per vertex lighting



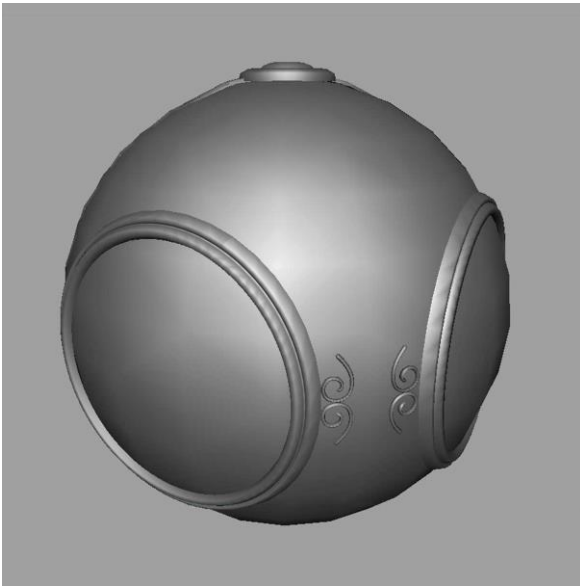
per fragment lighting



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Fragment Shader Applications

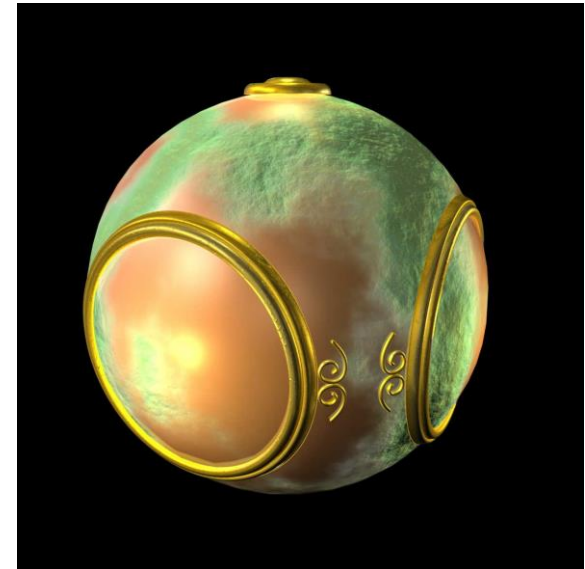
Texture mapping



smooth shading



environment
mapping



bump mapping



Writing Shaders

- First programmable shaders were programmed in an assembly-like manner
- OpenGL extensions added functions for vertex and fragment shaders
- Cg (C for graphics) C-like language for programming shaders
 - Works with both OpenGL and DirectX
 - Interface to OpenGL complex
- OpenGL Shading Language (GLSL)



GLSL

-
- OpenGL Shading Language
 - Part of OpenGL 2.0 and up
 - High level C-like language
 - New data types
 - Matrices
 - Vectors
 - Samplers
 - As of OpenGL 3.1, application must provide shaders



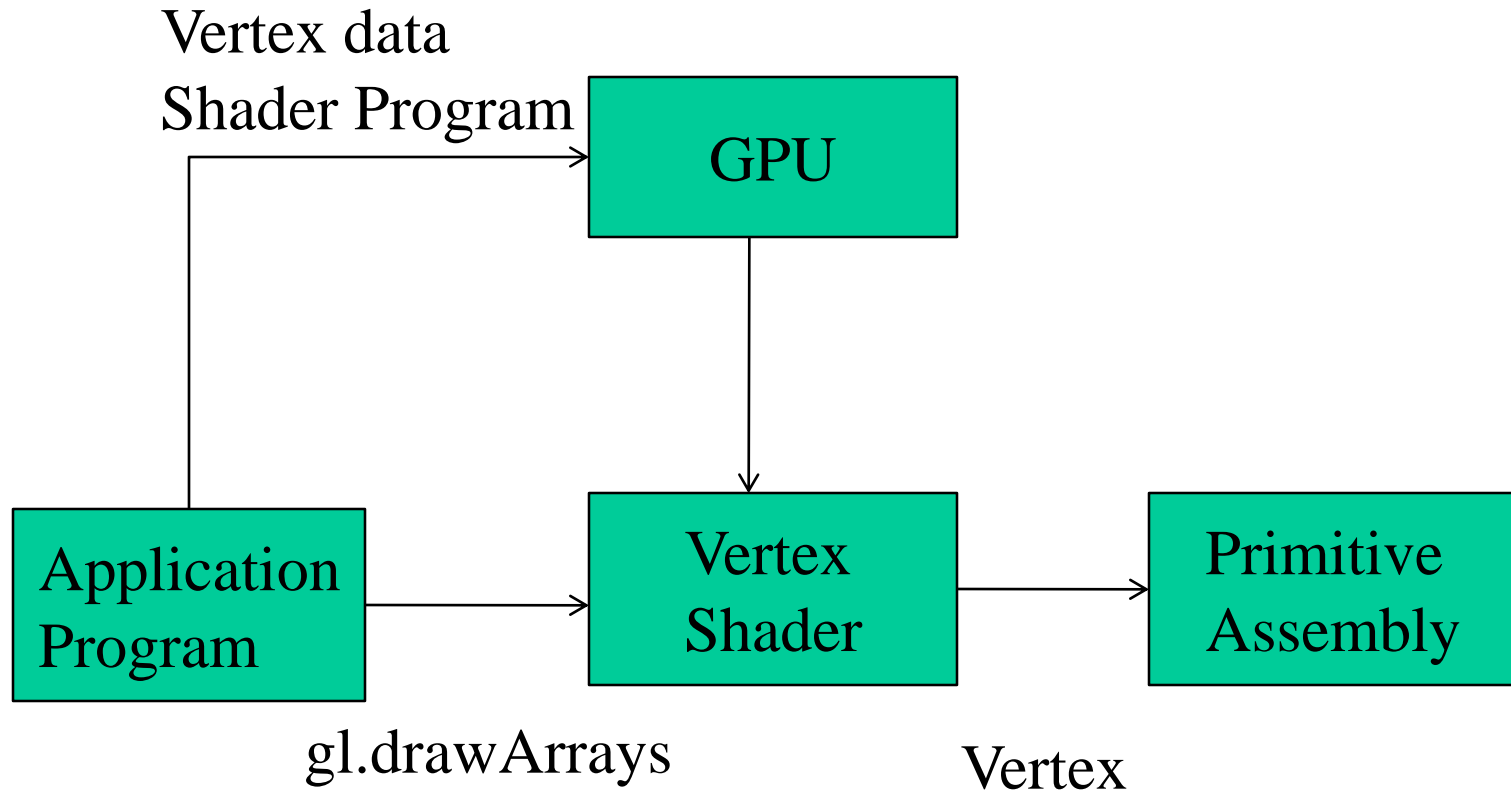
Simple Vertex Shader

```
    input from application
attribute vec4 vPosition;
void main(void)           must link to variable in application
{
    gl_Position = vPosition;
}
```

built in variable



Execution Model





Simple Fragment Program

precision mediump float;

void main(void)

{

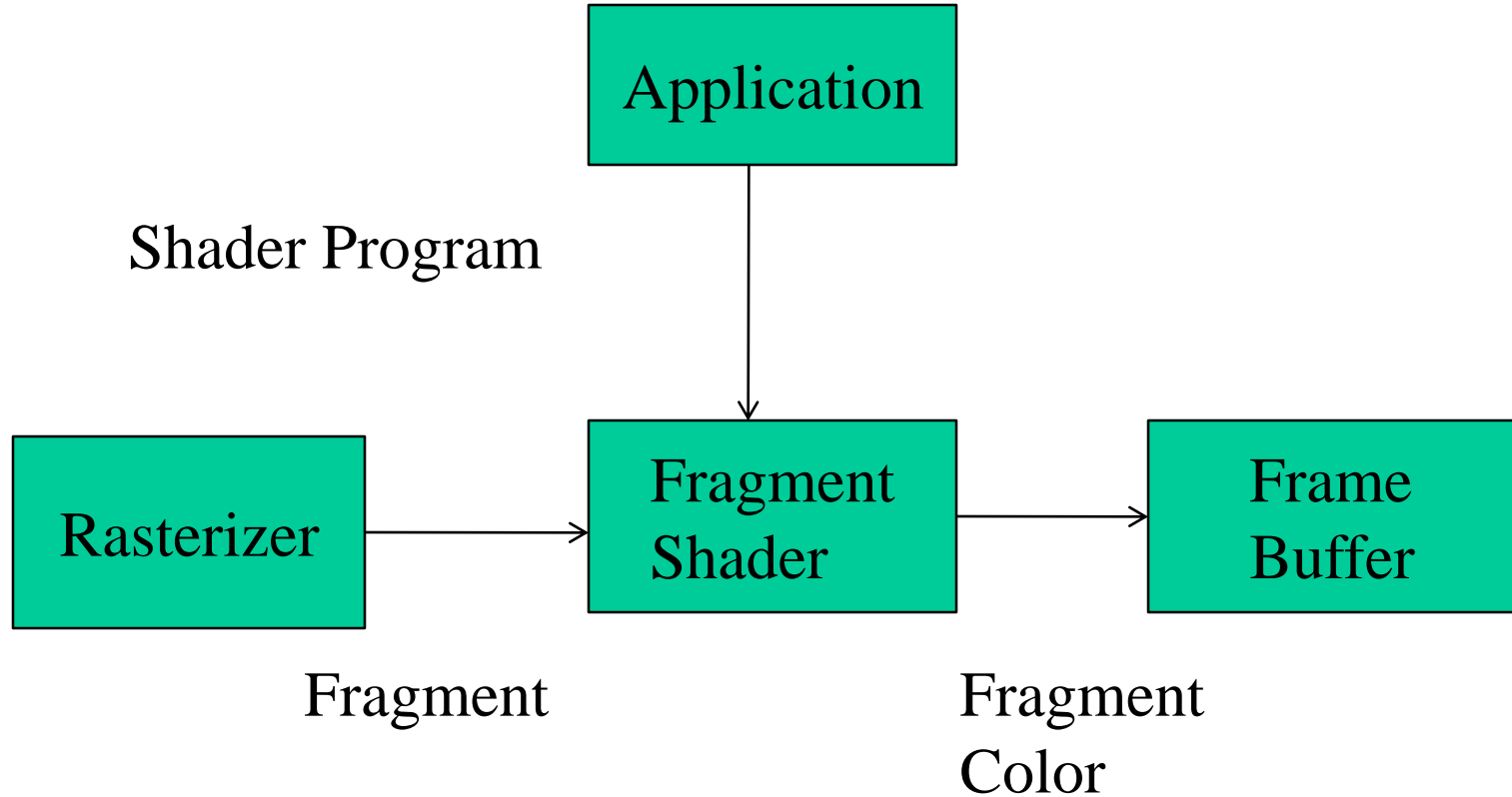
gl_FragColor = vec4(1.0, 0.0, 0.0, 1.0);

}



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Execution Model





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Data Types

- C types: int, float, bool
- Vectors:
 - float vec2, vec3, vec4
 - Also int (ivec) and boolean (bvec)
- Matrices: mat2, mat3, mat4
 - Stored by columns
 - Standard referencing m[row][column]
- C++ style constructors
 - `vec3 a = vec3(1.0, 2.0, 3.0)`
 - `vec2 b = vec2(a)`



No Pointers

- There are no pointers in GLSL
- We can use C structs which can be copied back from functions
- Because matrices and vectors are basic types they can be passed into and output from GLSL functions, e.g.

`mat3 func(mat3 a)`

- variables passed by copying



Qualifiers

- GLSL has many of the same qualifiers such as **const** as C/C++
- Need others due to the nature of the execution model
- Variables can change
 - Once per primitive
 - Once per vertex
 - Once per fragment
 - At any time in the application
- Vertex attributes are interpolated by the rasterizer into fragment attributes



Attribute Qualifier

- Attribute-qualified variables can change at most once per vertex
- There are a few built in variables such as `gl_Position` but most have been deprecated
- User defined (in application program)
 - `attribute float temperature`
 - `attribute vec3 velocity`
 - recent versions of GLSL use `in` and `out` qualifiers to get to and from shaders



Uniform Qualified

- Variables that are constant for an entire primitive
- Can be changed in application and sent to shaders
- Cannot be changed in shader
- Used to pass information to shader such as the time or a bounding box of a primitive or transformation matrices



Varying Qualified

- Variables that are passed from vertex shader to fragment shader
- Automatically interpolated by the rasterizer
- With WebGL, GLSL uses the varying qualifier in both shaders

```
varying vec4 color;
```

- More recent versions of WebGL use **out** in vertex shader and **in** in the fragment shader

```
out vec4 color; //vertex shader
```

```
in vec4 color; // fragment shader
```



Our Naming Convention

- attributes passed to vertex shader have names beginning with v (vPosition, vColor) in both the application and the shader
 - Note that these are different entities with the same name
- Varying variables begin with f (fColor) in both shaders
 - must have same name
- Uniform variables are unadorned and can have the same name in application and shaders



Example: Vertex Shader

```
attribute vec4 vColor;  
varying vec4 fColor; //out vec4 fColor;  
void main()  
{  
    gl_Position = vPosition;  
    fColor = vColor;  
}
```



Corresponding Fragment Shader

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precision mediump float;

varying vec4 fColor; //in vec4 fColor;

void main()

{

gl_FragColor = fColor;

}



Sending Colors from Application

```
var cBuffer = gl.createBuffer();  
gl.bindBuffer( gl.ARRAY_BUFFER, cBuffer );  
gl.bufferData( gl.ARRAY_BUFFER, flatten(colors),  
               gl.STATIC_DRAW );  
  
var vColor = gl.getAttributeLocation( program, "vColor" );  
gl.vertexAttribPointer( vColor, 3, gl.FLOAT, false, 0, 0 );  
gl.enableVertexAttribArray( vColor );
```




Sending a Uniform Variable

// in application

```
vec4 color = vec4(1.0, 0.0, 0.0, 1.0);  
colorLoc = gl.getUniformLocation( program, "color" );  
gl.uniform4f( colorLoc, color);
```

// in fragment shader (similar in vertex shader)

```
uniform vec4 color;  
void main()  
{  
    gl_FragColor = color;  
}
```



Operators and Functions

- Standard C functions
 - Trigonometric
 - Arithmetic
 - Normalize, reflect, length
- Overloading of vector and matrix types
 - mat4 a;
 - vec4 b, c, d;
 - c = b*a; // a column vector stored as a 1d array
 - d = a*b; // a row vector stored as a 1d array



Swizzling and Selection

- Can refer to array elements by element using [] or selection (.) operator with
 - x, y, z, w
 - r, g, b, a
 - s, t, p, q
 - **a[2], a.b, a.z, a.p** are the same
- **Swizzling** operator lets us manipulate components
 - vec4 a, b;**
 - a.yz = vec2(1.0, 2.0, 3.0, 4.0);**
 - b = a.yxzw;**



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Part 4: Color and Attributes

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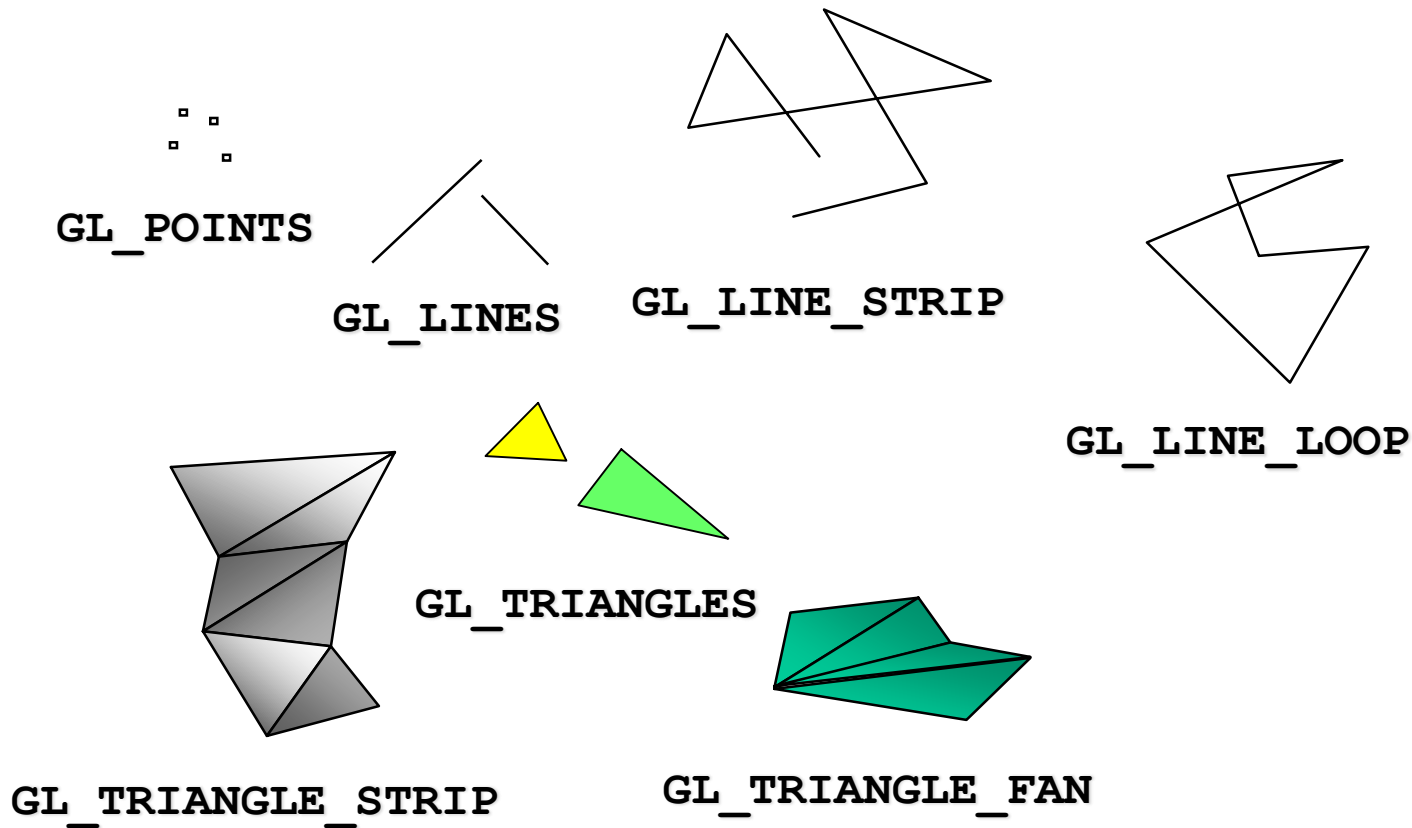
Objectives

- Expanding primitive set
- Adding color
- Vertex attributes



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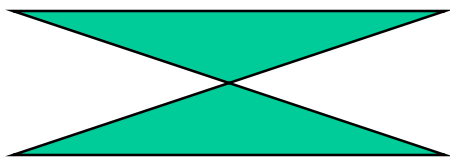
WebGLPrimitives





Polygon Issues

- WebGL will only display triangles
 - Simple: edges cannot cross
 - Convex: All points on line segment between two points in a polygon are also in the polygon
 - Flat: all vertices are in the same plane
- Application program must tessellate a polygon into triangles (triangulation)
- OpenGL 4.1 contains a tessellator but not WebGL



nonsimple polygon



nonconvex polygon



Polygon Testing

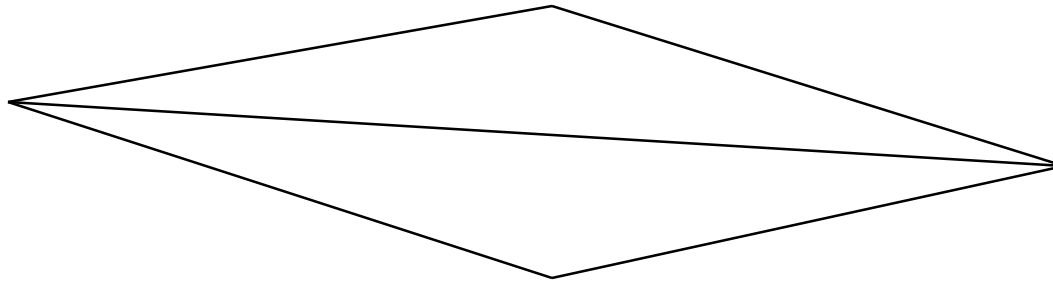
- Conceptually simple to test for simplicity and convexity
- Time consuming
- Earlier versions assumed both and left testing to the application
- Present version only renders triangles
- Need algorithm to triangulate an arbitrary polygon



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Good and Bad Triangles

- Long thin triangles render badly

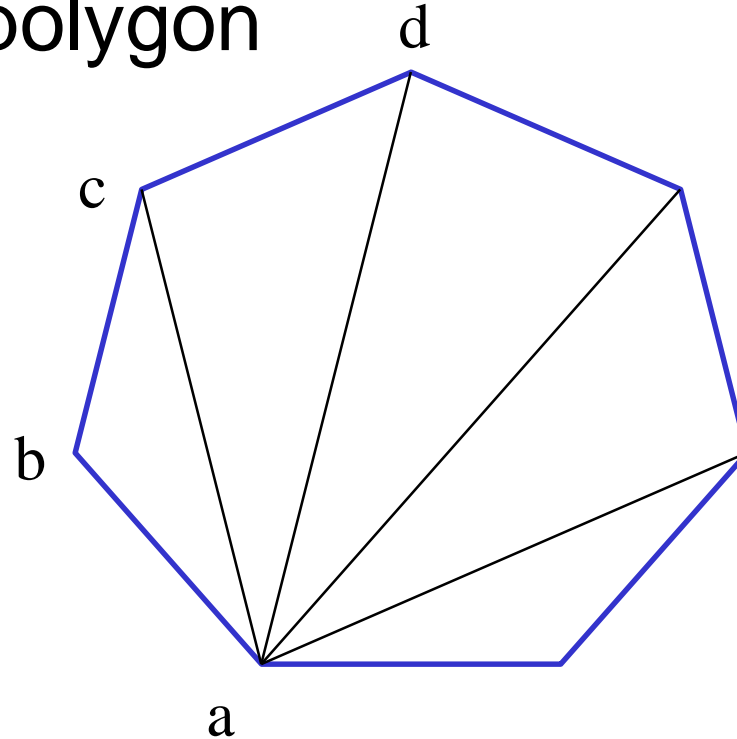


- Equilateral triangles render well
- Maximize minimum angle
- Delaunay triangulation for unstructured points



Triangularization

- Convex polygon

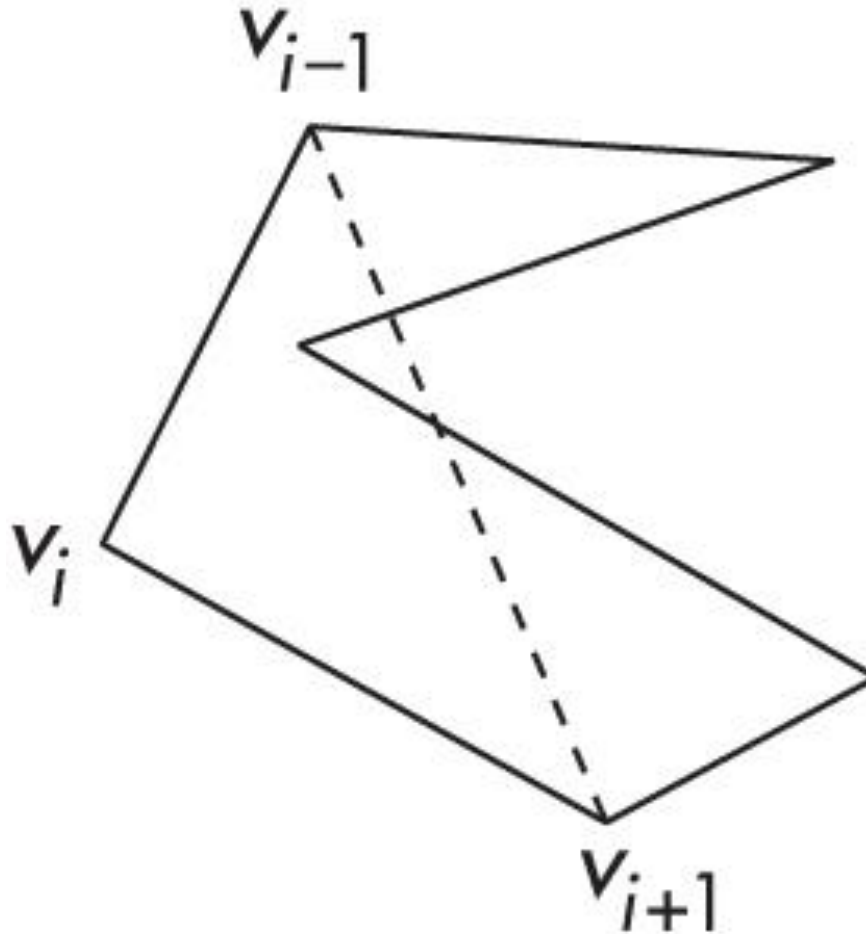


- Start with abc, remove b, then acd,



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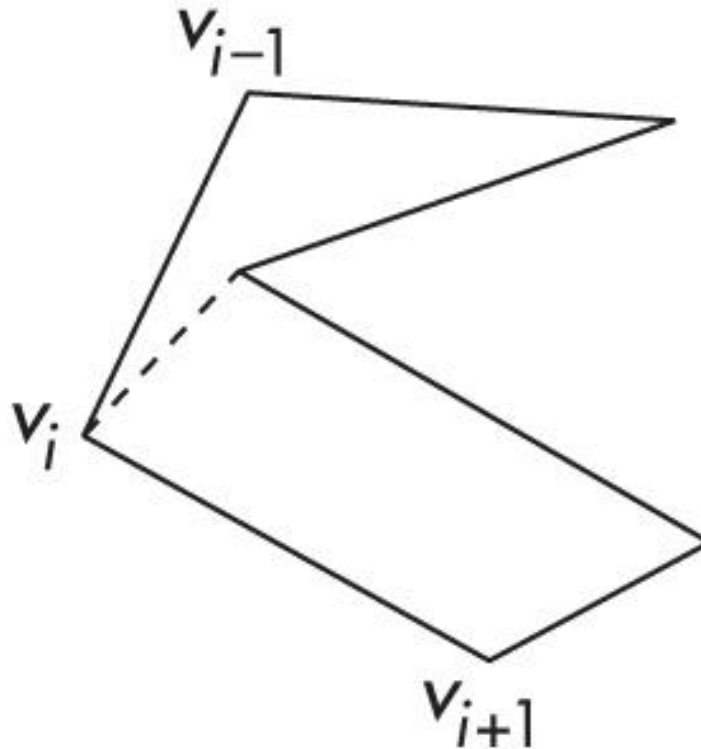
Non-convex (concave)





Recursive Division

- Find leftmost vertex and split





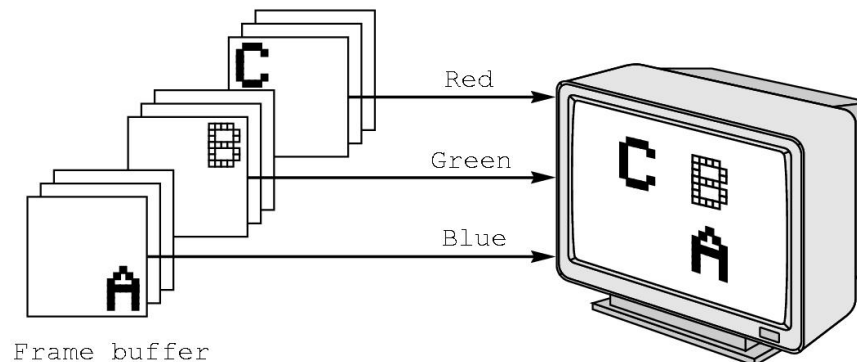
Attributes

- Attributes determine the appearance of objects
 - Color (points, lines, polygons)
 - Size and width (points, lines)
 - Stipple pattern (lines, polygons)
 - Polygon mode
 - Display as filled: solid color or stipple pattern
 - Display edges
 - Display vertices
- Only a few (`gl_PointSize`) are supported by WebGL functions



RGB color

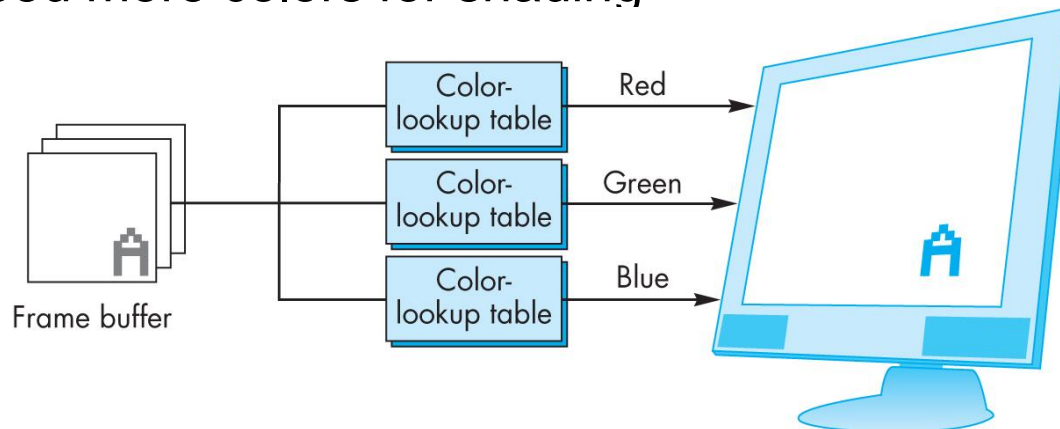
- Each color component is stored separately in the frame buffer
- Usually 8 bits per component in buffer
- Color values can range from 0.0 (none) to 1.0 (all) using floats or over the range from 0 to 255 using unsigned bytes





Indexed Color

- Colors are indices into tables of RGB values
- Requires less memory
 - indices usually 8 bits
 - not as important now
 - Memory inexpensive
 - Need more colors for shading

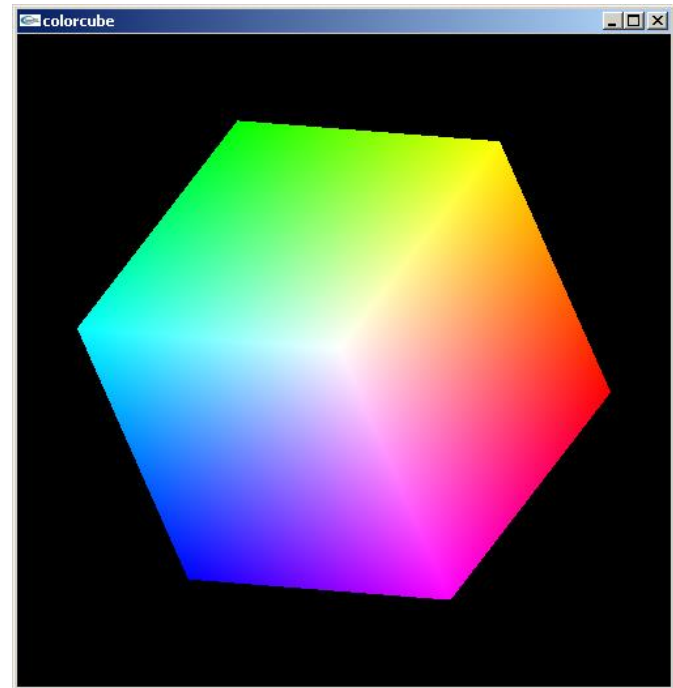




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Smooth Color

- Default is *smooth* shading
 - Rasterizer interpolates vertex colors across visible polygons
- Alternative is *flat shading*
 - Color of first vertex determines fill color
 - Handle in shader





Setting Colors

- Colors are ultimately set in the fragment shader but can be determined in either shader or in the application
- Application color: pass to vertex shader as a uniform variable or as a vertex attribute
- Vertex shader color: pass to fragment shader as varying variable
- Fragment color: can alter via shader code



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Part 5: More GLSL

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Objectives

- Coupling shaders to applications
 - Reading
 - Compiling
 - Linking
- Vertex Attributes
- Setting up uniform variables
- Example applications



Linking Shaders with Application

- Read shaders
- Compile shaders
- Create a program object
- Link everything together
- Link variables in application with variables in shaders
 - Vertex attributes
 - Uniform variables



Program Object

- Container for shaders
 - Can contain multiple shaders
 - Other GLSL functions

```
var program = gl.createProgram();
```

```
gl.attachShader( program, vertShdr );  
gl.attachShader( program, fragShdr );  
gl.linkProgram( program );
```



Reading a Shader

- Shaders are added to the program object and compiled
- Usual method of passing a shader is as a null-terminated string using the function
- `gl.shaderSource(fragShdr, fragElem.text);`
- If shader is in HTML file, we can get it into application by `getElementById` method
- If the shader is in a file, we can write a reader to convert the file to a string



Adding a Vertex Shader

```
var vertShdr;  
var vertElem =  
    document.getElementById( vertexShaderId );  
  
vertShdr = gl.createShader( gl.VERTEX_SHADER );  
  
gl.shaderSource( vertShdr, vertElem.text );  
gl.compileShader( vertShdr );  
  
// after program object created  
gl.attachShader( program, vertShdr );
```



Shader Reader

- Following code may be a security issue with some browsers if you try to run it locally

- Cross Origin Request

```
function getShader(gl, shaderName, type) {  
    var shader = gl.createShader(type);  
    shaderScript = loadFileAJAX(shaderName);  
    if (!shaderScript) {  
        alert('Could not find shader source:  
            '+shaderName);  
    }  
}
```



Precision Declaration

- In GLSL for WebGL we must specify desired precision in fragment shaders
 - artifact inherited from OpenGL ES
 - ES must run on very simple embedded devices that may not support 32-bit floating point
 - All implementations must support mediump
 - No default for float in fragment shader
- Can use preprocessor directives (`#ifdef`) to check if highp supported and, if not, default to mediump



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Pass Through Fragment Shader

```
#ifdef GL_FRAGMENT_SHADER_PRECISION_HIGH  
    precision highp float;  
#else  
    precision mediump float;  
#endif  
  
varying vec4 fcolor;  
void main(void)  
{  
    gl_FragColor = fcolor;  
}
```



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Part 6: Three Dimensions

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Objectives

- Develop a more sophisticated three-dimensional example
 - Sierpinski gasket: a fractal
- Introduce hidden-surface removal



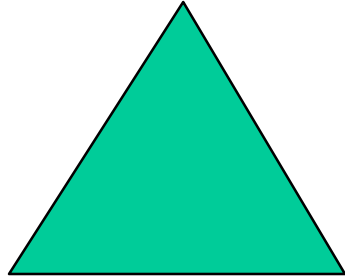
Three-dimensional Applications

- In WebGL, two-dimensional applications are a special case of three-dimensional graphics
- Going to 3D
 - Not much changes
 - Use `vec3`, `gl.uniform3f`
 - Have to worry about the order in which primitives are rendered or use hidden-surface removal

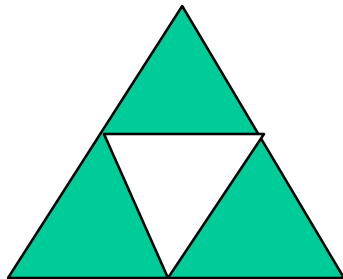


Sierpinski Gasket (2D)

- Start with a triangle



- Connect bisectors of sides and remove central triangle



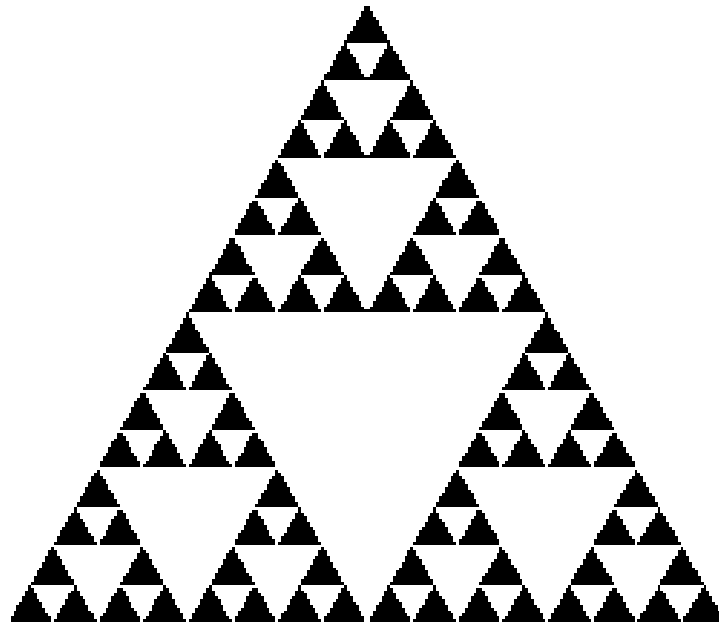
- Repeat



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Example

- Five subdivisions





The gasket as a fractal

- Consider the filled area (black) and the perimeter (the length of all the lines around the filled triangles)
- As we continue subdividing
 - the area goes to zero
 - but the perimeter goes to infinity
- This is not an ordinary geometric object
 - It is neither two- nor three-dimensional
- It is a *fractal* (fractional dimension) object



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Gasket Program

- HTML file
 - Same as in other examples
 - Pass through vertex shader
 - Fragment shader sets color
 - Read in JS file



Gasket Program

```
var points = [];  
var NumTimesToSubdivide = 5;  
  
/* initial triangle */  
  
var vertices = [  
    vec2( -1, -1 ),  
    vec2(  0,  1 ),  
    vec2(  1, -1 )  
];  
  
divideTriangle( vertices[0], vertices[1],  
                vertices[2], NumTimesToSubdivide);
```



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Draw one triangle

```
/* display one triangle */  
  
function triangle( a, b, c ){  
    points.push( a, b, c );  
}
```



Triangle Subdivision

```
function divideTriangle( a, b, c, count ){
    // check for end of recursion
    if ( count === 0 ) {
        triangle( a, b, c );
    }
    else {
        //bisect the sides
        var ab = mix( a, b, 0.5 );
        var ac = mix( a, c, 0.5 );
        var bc = mix( b, c, 0.5 );
        --count;
        // three new triangles
        divideTriangle( a, ab, ac, count-1 );
        divideTriangle( c, ac, bc, count-1 );
        divideTriangle( b, bc, ab, count-1 );
    }
}
```



init()

```
var program = initShaders( gl, "vertex-  
  shader", "fragment-shader" );  
    gl.useProgram( program );  
    var bufferId = gl.createBuffer();  
gl.bindBuffer( gl.ARRAY_BUFFER, bufferId )  
gl.bufferData( gl.ARRAY_BUFFER,  
  flatten(points), gl.STATIC_DRAW );  
var vPosition = gl.getAttributeLocation(  
  program, "vPosition" );  
    gl.vertexAttribPointer( vPosition, 2,  
gl.FLOAT, false, 0, 0 );  
    gl.enableVertexAttribArray( vPosition );  
    render();
```




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Render Function

```
function render() {  
    gl.clear( gl.COLOR_BUFFER_BIT );  
    gl.drawArrays( gl.TRIANGLES, 0, points.length  
    );  
}
```



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Moving to 3D

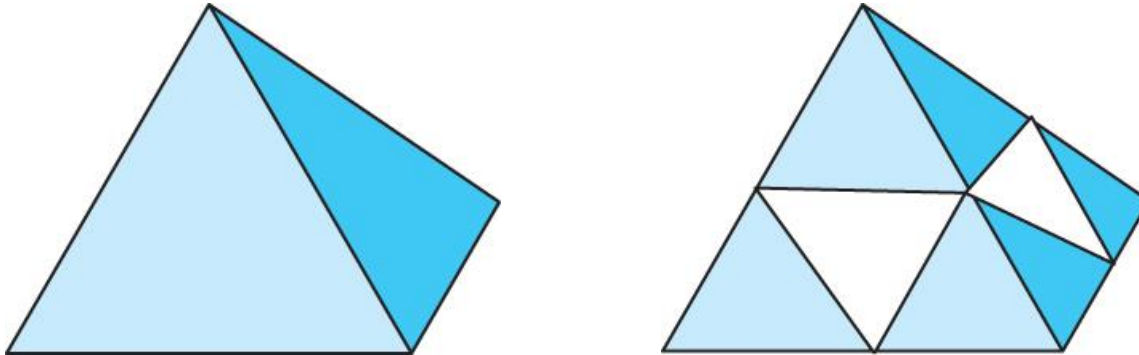
- We can easily make the program three-dimensional by using three dimensional points and starting with a tetrahedron

```
var vertices = [  
    vec3( 0.0000, 0.0000, -1.0000 ),  
    vec3( 0.0000, 0.9428, 0.3333 ),  
    vec3( -0.8165, -0.4714, 0.3333 ),  
    vec3( 0.8165, -0.4714, 0.3333 ) ];  
subdivide each face
```



3D Gasket

- We can subdivide each of the four faces

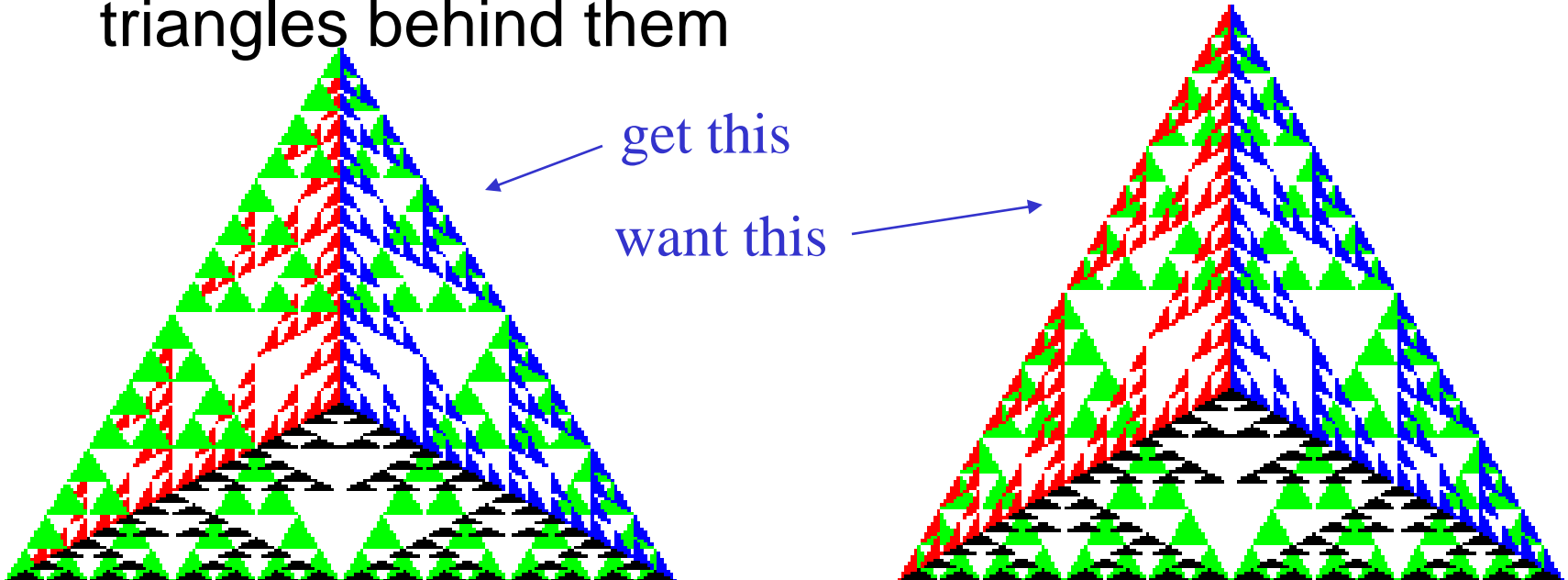


- Appears as if we remove a solid tetrahedron from the center leaving four smaller tetrahedra
- Code almost identical to 2D example



Almost Correct

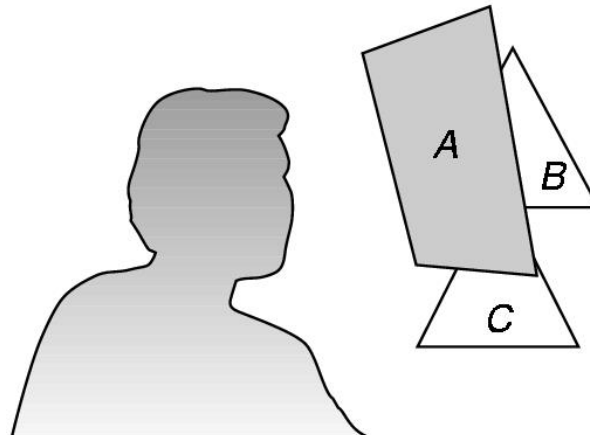
- Because the triangles are drawn in the order they are specified in the program, the front triangles are not always rendered in front of triangles behind them





Hidden-Surface Removal

- We want to see only those surfaces in front of other surfaces
- OpenGL uses a *hidden-surface* method called the z-buffer algorithm that saves depth information as objects are rendered so that only the front objects appear in the image





Using the z-buffer algorithm

- The algorithm uses an extra buffer, the z-buffer, to store depth information as geometry travels down the pipeline
- Depth buffer is required to be available in WebGL
- It must be
 - Enabled
 - `gl.enable(gl.DEPTH_TEST)`
 - Cleared in for each render
 - `gl.clear(gl.COLOR_BUFFER_BIT | gl.DEPTH_BUFFER_BIT)`



Surface vs Volume Subdivision

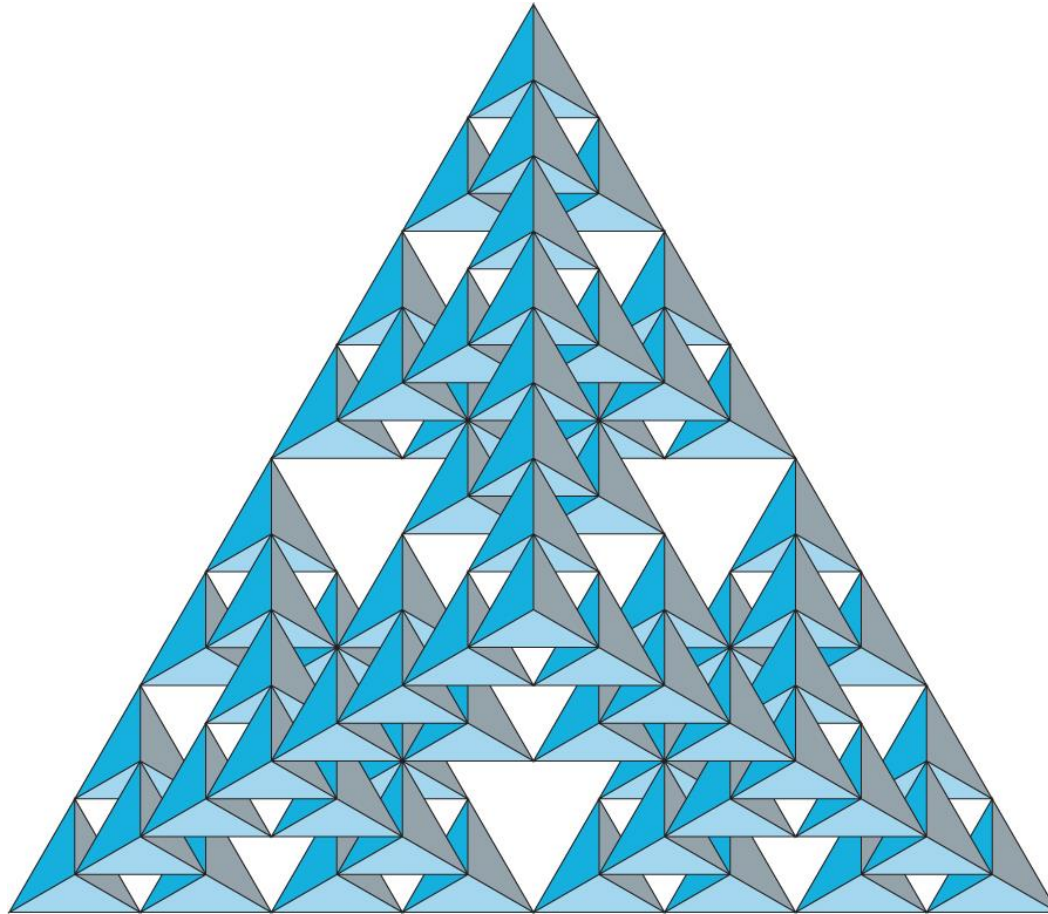
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-
- In our example, we divided the surface of each face
 - We could also divide the volume using the same midpoints
 - The midpoints define four smaller tetrahedrons, one for each vertex
 - Keeping only these tetrahedrons removes a *volume* in the middle
 - See text for code



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Volume Subdivision





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Incremental and Quaternion Rotation

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Objectives

- This is an optional lecture that
 - Illustrates the difference between using direction angles and Euler angles
 - Considers issues with incremental rotation
 - Introduces quaternions as an alternate to rotation matrices



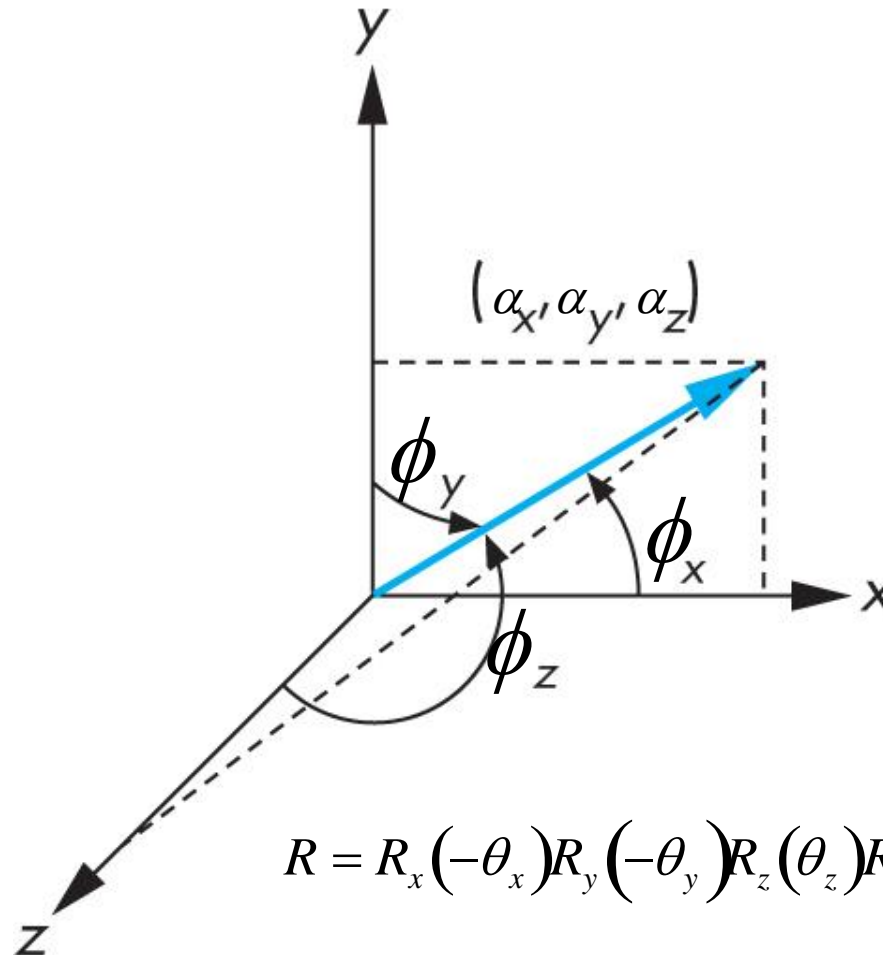
Specifying a Rotation

- Pre 3.1 OpenGL had a function `glRotate` (θ , dx , dy , dz) which incrementally changed the current rotation matrix by a rotation with fixed point of the origin about a vector in the direction (dx , dy , dz)
- We implemented `rotate` in `MV.js`
- Implementations of `Rotate` often decompose the general rotation into a sequence of rotations about the coordinate axes as in Chapter 4.



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Euler from Direction Angles



$$R = R_x(-\theta_x)R_y(-\theta_y)R_z(\theta_z)R_y(\theta_y)R_x(\theta_x)$$



Efficiency

$$R = R_x(-\theta_x)R_y(-\theta_y)R_z(\theta_z)R_y(\theta_y)R_x(\theta_x)$$

should be able to write as

$$R = R_x(\varphi_x)R_y(\varphi_y)R_z(\varphi_z)$$

If we knew the angles, we could use RotateX, RotateY and RotateZ from mat.h

But is this an efficient method?

No, we can do better with quaterions



Incremental Rotation

$$R(t + dt) = R(t)R_z(\theta_z)R_y(\theta_y)R_x(\theta_x)$$

where θ_x , θ_y and θ_z are small angles

For small angles $\sin \theta \approx \theta$

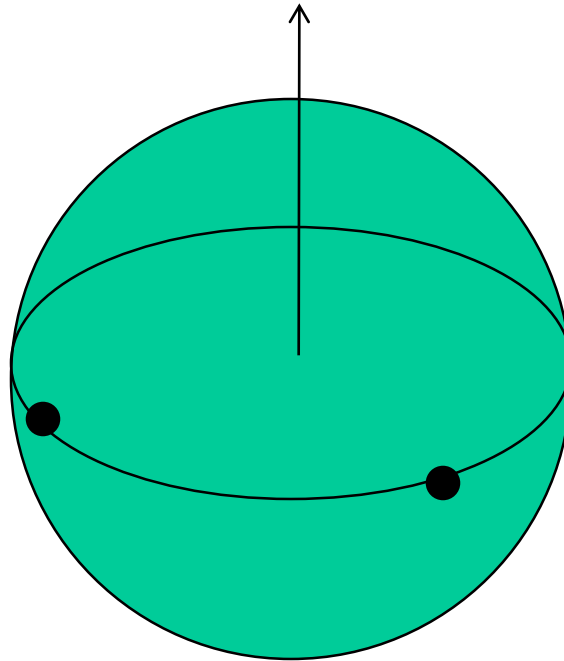
$$\cos \theta \approx 1$$

$$R_z(\theta_z)R_y(\theta_y)R_x(\theta_x) \approx \begin{bmatrix} 1 & -\theta_z & \theta_y & 0 \\ \theta_z & 1 & -\theta_x & 0 \\ -\theta_y & \theta_x & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



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Great Circles





Rotation and Great Circles

- Shortest path between two points on a sphere is the great circle passing through the two points
- Corresponding to each great circle is vector normal to the circle
- Rotation about this vector carries us from the first point to the second



Quaternion Rotation

Definition: $a = (q_0, q_1, q_2, q_3) = (q_0, \mathbf{q})$

Quaternion Arithmetic: $a + b = (a_0 + b_0, \mathbf{a} + \mathbf{b})$

$$ab = (a_0 b_0 - \mathbf{a} \bullet \mathbf{b}, a_0 \mathbf{b} + b_0 \mathbf{a} + \mathbf{a} \times \mathbf{b})$$

$$|a|^2 = (q_0^2, \mathbf{q} \bullet \mathbf{q})$$

$$a^{-1} = \frac{1}{|a|^2} (q_0, -\mathbf{q})$$

Representing a 3D point: $p = (0, \mathbf{p})$

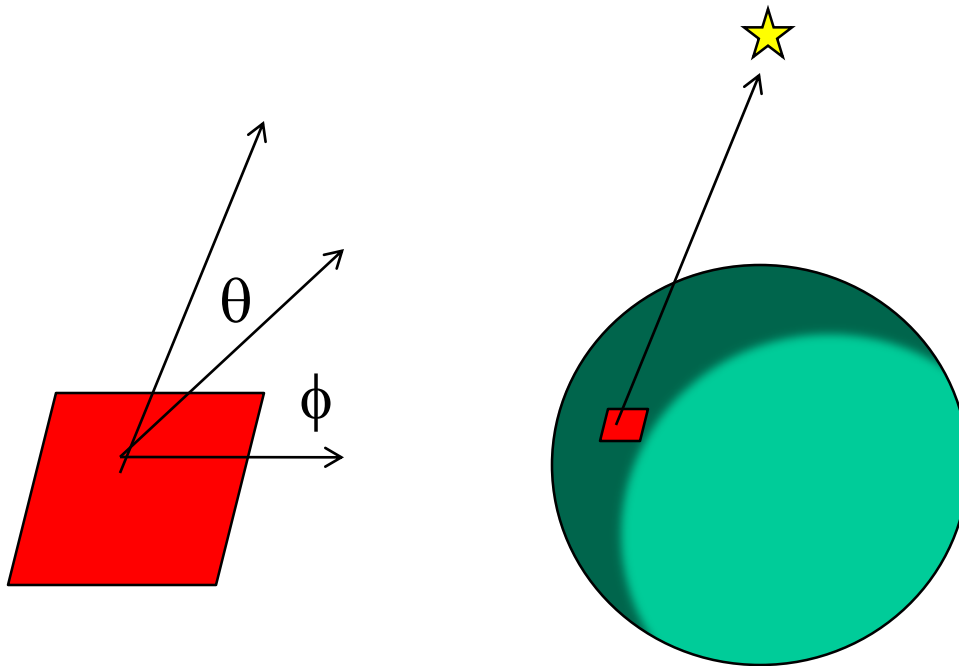
Representing a Rotation: $r = \left(\cos \frac{\theta}{2}, \sin \frac{\theta}{2} \mathbf{v} \right)$

Rotating a Point: $p' = r p r^{-1}$



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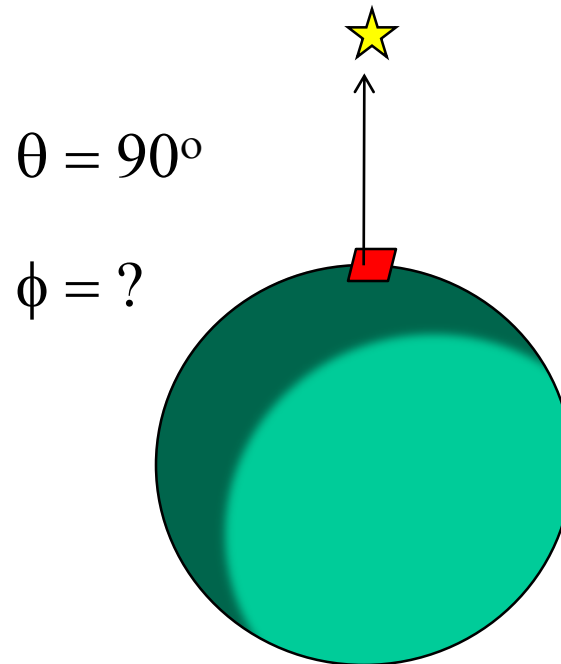
Looking at the North Star





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At North Pole





Gimbal Lock

- Suppose you rotate about the y axis by 90°
- This action removes a degree of freedom

$$R_z(\theta_z)R_y(\theta_y)R_x(\theta_x) \approx \begin{bmatrix} 0 & \sin(\theta_x - \theta_z) & \cos(\theta_x - \theta_z) & 0 \\ 0 & \cos(\theta_x - \theta_z) & -\sin(\theta_x - \theta_z) & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



Quaternions and Computer Graphics

- (Re)discovered by both aerospace and animation communities
- Used for head mounted display in virtual and augmented reality
- Used for smooth camera paths
- Caveat: quaternions do not preserve up direction



Working with Quaternions

- Quaternion arithmetic works well for representing rotations around the origin
- There is no simple way to convert a quaternion to a matrix representation
- Usually copy elements back and forth between quaternions and matrices
- Can use directly without rotation matrices in the virtual trackball
- Quaternion shaders are simple