Lecture 4: Encryption via enciphering

- Homework 2 due Monday 2/3
- Textbook reading for this week: Serious Cryptography, chapter 4
- I will try to post lecture slides before class (no promises though)

Recap: protecting data confidentiality at rest





encrypt **C** = *E*(**K**, **P**)

private message **P**



decrypt P = D(K, C)

???



Recap: block cipher

- - Forward direction called encipherin
 - Backward direction called decipher



• Family of finite permutations (i.e., codebooks), indexed by a secret key

$$\begin{array}{ll} & X \longrightarrow B_{K} \longrightarrow Y \\ \hline ring & Y \longrightarrow B_{K}^{-1} \longrightarrow X \end{array}$$

• B_K is strongly pseudorandom if every resource-bounded adversary can only distinguish the real cipher B_K from Π with very small probability ε

Recap: Rijndael, aka AES, is a concrete block cipher



Key alternating structure

- 128, 192, or 256 bit initial key
- Expand into r+1 round keys, each of which is 128 bits long
- Invertible key schedule: given key_i, can compute key_{i-1} or key_{i+1}

Iterated round structure

• 16 bytes of state



- Total of *r* = 10 to 14 rounds
- 3 invertible operations per round
 - Final round is slightly different
- Only S-box is nonlinear

Recap: brute force attack

- There is a large (but finite!) set of possible keys
- Brute force attack: Eve runs a for loop over all keys, checks if $B_{\mathcal{K}}(X) = Y$
- Ergo, best possible time bound t = 2^{λ}
- Two ways crypto can go bad
 - **Obsolete:** it is computationally feasible to run a brute force attack (e.g., DES)
 - **Broken:** there exists an attack that runs faster than brute force (e.g., 2DES)

Game	Search size	Solved
Connect 4	2^43	\checkmark
Limit hold 'em	2^47	\checkmark
Checkers	2^67	\checkmark
Modern crypto	2^128-2^256	
Chess	2^133	
No limit hold 'em	2^465	
Go (19 × 19)	2^568	



How to think about really large numbers

- <u>Converting to base-2</u> <u>Speed of cryptography on modern computers</u>
 - 2¹⁰ ≈ 10³ (kilo)
 Running AES: (2³¹ cycles/_{sec}) / (10 cycles/_{aes}) ≈ 2²⁷ aes/_{sec}
 - 2²⁰ ≈ 10⁶ (mega)
 - 2³⁰ ≈ 10⁹ (giga)
 - 2⁴⁰ ≈ 10¹² (tera)
 - 2⁵⁰ ≈ 10¹⁵ (peta)
 - 2⁶⁰ ≈ 10¹⁸ (exa)



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- So about $2^{52 \text{ ops}}/_{\text{year}}$, given that 1 year $\approx 2^{25}$ sec
- Entire bitcoin network: about 267 ops/sec

Difficulty of attacking crypto

Eve's search space	Time with laptop (2 ⁵² ops/yr)	Time with bitcoin network (2 ⁶⁷ ops/sec)
2 ²⁰ (your homework)	0.01 second	~instantaneous
2 ⁵⁶ (DES brute force)	24 = 16 CPU core-years	much less than 1 second
280	2 ²⁸ = 256 million CPU core-yr	2 ¹³ seconds ≈ 2 hours
2 ¹²⁸ (AES-128 brute force)	<pre>2⁷⁶ = 64 sextillion CPU core-yr = 2³³ × 2⁴³ = 8 trillion CPU core-yr for each person on earth</pre>	2 ⁶³ sec ≈ 2 ³⁸ year ≈ 100 billion y (cf. age of universe ≈ 14b years)
2 ²⁵⁶ (AES-256 brute force)	(about the energy of the sun)	









Alice's confidentiality + integrity goals





- Data privacy: Eve cannot learn P (today)
- Data authenticity: if Eve tampers with C, then Alice can detect the change
- Entity authenticity: future Alice knows that she previously created C
- "Confidentiality xor authenticity is **not possible**.
- If you don't have both, often you don't have either."
 - -Prof. Matthew Green, Johns Hopkins



Does a cipher give us confidential communication?



- First reaction: Yes! The cipher transforms X in a confusing way
- Full answer: not quite, we have 2 issues
 - Usability: Block cipher only supports messages where |X| = block length
 - Security: Vulnerable to *frequency attacks* if Alice enciphers the same block twice





Supporting longer messages

One simple mode: process each block of the message independently

This is called *Electronic Codebook (ECB)* mode





- **Def.** A *mode of operation* connects multiple calls to a block cipher (with one key K)



ECB mode \Rightarrow sad Linux penguins





Raw image of Linux penguin

Image after ECB mode



What we want encryption to do

What if message blocks don't repeat?

key K

encode $C_i = B_K(P_i)$

private data $P_1, P_2, \dots P_e$

key K

decode $P_i = B_K^{-1}(C_i)$



What if message blocks don't repeat?

key K

encode $C_i = \Pi(P_i)$

private data $P_1, P_2, \dots P_e$

key K

decode $P_i = \Pi^{-1}(C_i)$

How do we guarantee that message blocks don't repeat?

???



Lessons learned

- Randomness matters: We can confuse Eve! Just need to design a mode of operation that guarantees each enciphered block is unique.
- **Definitions matter:** Argument leverages the concept that a block cipher "looks like" a random permutation from Eve's point of view.

private **P** nonce N Mode ciphertext **C**





Lessons learned

- Randomness matters: We can confuse Eve! Just need to design a mode of operation that guarantees each enciphered block is unique.
- **Definitions matter:** Argument leverages the concept that a block cipher "looks like" a random permutation from Eve's point of view.

private **P** nonce **N** Mode ciphertext **C**





Cipher block chaining (CBC) mode

P

CBC

BK

N = random string for variety (sometimes called an initialization vector or IV)

N-

K = random string for privacy





CBC decryption







Apple's Common Crypto Library Defaults to a Zero IV if One is not Provided

Today I was writing some guidelines about generating keys for mobile applications at work. While providing code examples in Java and Obj-C for AES encryption I happened to look at Apple's Common <u>Crypto</u> library . While going through the source code for <u>CommonCryptor.c</u>, I noticed that IV is commented as /* optional initialization vector */. This makes sense because not all ciphers use IV and not all AES modes of operation (e.g. ECB mode). However; if an IV is not provided, the library will default to a zero IV.

You can see the code here inside the function ccInitCryptor (search for defaultIV) source. CC_XZEROMEM resets all bytes of IV to zero (that is 0x00):

```
static inline CCCryptorStatus ccInitCryptor
(CCCryptor *ref, const void *key, unsigned long key_len, const void *tweak_key, const void *iv
   size_t blocksize = ccGetCipherBlockSize(ref);
   uint8_t defaultIV[blocksize];
    if(iv == NULL) {
       CC_XZEROMEM(defaultIV, blocksize);
       iv = defaultIV;
```

```
. . .
return kCCSuccess;
```

While I am told this is probably common behavior in crypto libraries, I think it's dangerous. I ended up putting a comment in code examples warning developers about this behavior. So, heads up ;)

Source: parsiya.net/ blog/2014-07-03-applescommon-crypto-librarydefaults-to-a-zero-iv-ifone-is-not-provided/

