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Concurrent Execution of Transactions

Serializability

Database Management Systems Transaction Processing

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- Conflict Serializability
- View Serializability
- Testing for Serializability

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Concurrent Execution of Transactions

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Basics

What is a transaction?

A unit of program execution that accesses and possibly updates various data items.

The properties (briefed as ACID) of a transaction maintained by the database system to ensure integrity of the data:

- Atomicity: None or all operations of the transaction are reflected properly in the database.
- Consistency: The database consistency is preserved by the execution of a transaction with no other transaction executing concurrently.
- <u>Isolation</u>: If multiple transactions execute concurrently, the system guarantees that for every transaction pair it appears one of them starts execution after the other finishes.
- Durability: Changes in database after the successful completion of a transaction are retained, even if there are system failures.

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An example

Suppose, 10 PCs are transferred from the PC attribute of the relation ISI to relation IISc.

The transaction (consisting of six instructions) required for the above operation is as follows:

- read(ISI_{PC})
- $\blacksquare \mathsf{ISI}_{PC} \leftarrow \mathsf{ISI}_{PC} 10$
- write(ISI_{PC})
- $\boxed{\mathsf{V}} \ \mathsf{IISc}_{PC} \leftarrow \mathsf{IISc}_{PC} + 10$
- ✓ write(IISc_{PC})

Note: We have to deal with system failures and manage concurrent execution of multiple instructions.

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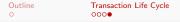


An example

Let us see how the ACID properties are managed:

- Atomicity: If the system fails at the steps 4-5 then this partial execution will not be incorporated.
- Consistency: If at any step the system fails then also the sum of ISI_{PC} and $IISc_{PC}$ should be same.
- <u>Isolation</u>: If any other transaction working on ISI and IISc appears, while executing the steps 3-6, it will wait until the current transaction completes.
- Durability: Once the steps 1-6 are executed the database changes will persist.

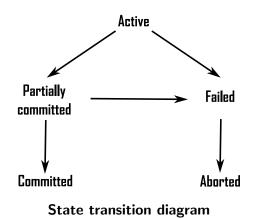
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Transaction life cycle



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Why concurrent execution of transactions?

- Increased processor and disk utilization
- Better transaction throughput
- Reduced waiting time
- Reduced average response time for transactions short transactions will not wait behind longer ones

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Scheduling of transactions

A schedule is a sequence of instructions that specify the chronological order in which instructions of concurrent transactions are executed

Some properties of scheduling:

- A schedule for a set of transactions should comprise all instructions of those transactions
- A schedule should retain the order in which the instructions appear in each individual transaction
- A transaction completing successful execution should have a commit instruction as the last statement
- A transaction that fails to successfully complete its execution should have an abort instruction as the last statement

Note: The number of possible schedules for a set of *n* transactions is much larger than n!.



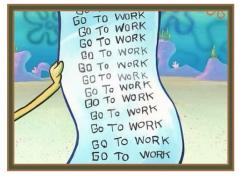
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Importance of a schedule



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Scheduling of transactions – Example 1

Serial schedule T_1 is followed by T_2 :

	Transaction T ₁	Transaction T ₂	$ISI_{PC}=20$, $IISc_{PC}=40$
IN01	$read(ISI_{PC})$		
IN02	$T \leftarrow ISI_{PC} * 0.05$		T=1
IN03	$ISI_{PC} \leftarrow ISI_{PC}$ - T		
IN04	write(ISI _{PC})		ISI _{PC} =19, IISc _{PC} =40
IN05	$read(IISc_{PC})$		
IN06	$IISc_{PC} \leftarrow IISc_{PC} + T$		
IN07	write(IISc _{PC})		ISI _{PC} =19, IISc _{PC} =41
IN08	commit		ISI _{PC} =19, IISc _{PC} =41
IN09		$read(ISI_{PC})$	
IN10		$ISI_{PC} \leftarrow ISI_{PC} - 10$	
IN11		write(ISI_{PC})	ISI _{PC} =9, IISc _{PC} =41
IN12		$read(IISc_{PC})$	
IN13		$IISc_{PC} \leftarrow IISc_{PC} + 10$	
IN14		write(IISc _{PC})	ISI _{PC} =9, IISc _{PC} =51
IN15		commit	ISI _{PC} =9, IISc _{PC} =51
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Scheduling of transactions – Example 2

Serial schedule T_2 is followed by T_1 :

	Transaction T_1	Transaction T ₂	$ISI_{PC}=20$, $IISc_{PC}=40$
IN01		$read(ISI_{PC})$	
IN02		$ISI_{PC} \leftarrow ISI_{PC}$ - 10	
IN03		write(ISI_{PC})	$ISI_{PC}=10$, $IISc_{PC}=40$
IN04		$read(IISc_{PC})$	
IN05		$IISc_{PC} \leftarrow IISc_{PC} + 10$	
IN06		write(IISc _{PC})	$ISI_{PC} = 10$, $IISc_{PC} = 50$
IN07		commit	$ISI_{PC}=10$, $IISc_{PC}=50$
IN08	$read(ISI_{PC})$		
IN09	$T \leftarrow ISI_{PC} * 0.05$		T = 0.5
IN10	$ISI_{PC} \leftarrow ISI_{PC}$ - T		
IN11	write(ISI _{PC})		ISI _{PC} =9.5, IISc _{PC} =50
IN12	$read(IISc_{PC})$		
IN13	$IISc_{PC} \leftarrow IISc_{PC} + T$		
IN14	write(IISc _{PC})		ISI _{PC} =9.5, IISc _{PC} =50.5
IN15	commit		ISI _{PC} =9.5, IISc _{PC} =50.5
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Scheduling of transactions – Example 3

Not a serial schedule but equivalent to T_2 is followed by T_1 :

	Transaction T_1	Transaction T ₂	$ISI_{PC}=20$, $IISc_{PC}=40$
IN01		$read(ISI_{PC})$	
IN02		$ISI_{PC} \leftarrow ISI_{PC}$ - 10	
IN03		write(ISI_{PC})	$ISI_{PC}=10$, $IISc_{PC}=40$
IN04	$read(ISI_{PC})$		
IN05	$T \leftarrow ISI_{PC} * 0.05$		T = 0.5
IN06	$ISI_{PC} \leftarrow ISI_{PC}$ - T		
IN07	write(ISI_{PC})		ISI _{PC} =9.5, IISc _{PC} =40
IN08		read(IISc _{PC})	
IN09		$IISc_{PC} \leftarrow IISc_{PC} + 10$	
IN10		write(IISc _{PC})	ISI _{PC} =9.5, IISc _{PC} =50
IN11		commit	ISI _{PC} =9.5, IISc _{PC} =50
IN12	$read(IISc_{PC})$		
IN13	$IISc_{PC} \leftarrow IISc_{PC} + T$		
IN14	write(IISc _{PC})		ISI _{PC} =9.5, IISc _{PC} =50.5
IN15	commit		ISI _{PC} =9.5, IISc _{PC} =50.5
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Scheduling of transactions - Example 4

Not a serial schedule and also inconsistent:

	Transaction T_1	Transaction T ₂	ISI _{PC} =20, IISc _{PC} =40
IN01		$read(ISI_{PC})$	
IN02		$ISI_{PC} \leftarrow ISI_{PC}$ - 10	
IN03	$read(ISI_{PC})$		
IN04	$T \leftarrow ISI_{PC} * 0.05$		T=1
IN05	$ISI_{PC} \leftarrow ISI_{PC}$ - T		
IN06	write(ISI_{PC})		ISI _{PC} =19, IISc _{PC} =40
IN07	$read(IISc_{PC})$		
IN08		write(ISI _{PC})	$ISI_{PC} = 19$, $IISc_{PC} = 40$
IN09		$read(IISc_{PC})$	
IN10		$IISc_{PC} \leftarrow IISc_{PC} + 10$	
IN11		write(IISc _{PC})	$ S _{PC}=19$, $ ISc_{PC}=50$
IN12		commit	$ S _{PC}=19$, $ Sc_{PC}=50$
IN13	$IISc_{PC} \leftarrow IISc_{PC} + T$		
IN14	write(IISc _{PC})		$ S _{PC} = 19$, $ ISc_{PC} = 51$
IN15	commit		$ S _{PC} = 19$, $ ISc_{PC} = 51$
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Assumption: Each transaction preserves database consistency.

So, the serial execution of a set of transactions should preserve the database consistency.

A schedule is serializable if it is equivalent to a serial schedule

Different forms of schedule equivalence give rise to the notions of - conflict serializability and view serializability. For both the cases our main concern is the read/write operation.

Note: We consider only read() and write() instructions to verify serializability.

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Concurrent Execution of Transactions

Serializability

Conflict serializability

Definition (Conflict)

Instructions I_i and I_j of transactions T_i and T_j respectively, conflict if and only if there exists some item Q accessed by both I_i and I_j and at least one of them is a write instruction.

Definition (Conflict equivalent)

If a schedule S can be transformed into a schedule S' by a series of swaps of non-conflicting instructions, we say that S and S' are conflict equivalent.

Definition (Conflict serializable)

A schedule S is conflict serializable if it is conflict equivalent to a serial schedule.

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Concurrent Execution of Transactions

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Understanding conflict equivalence

	Transaction T ₁	Transaction T ₂
\uparrow		$read(ISI_{PC})$
Block1		$ISI_{PC} \leftarrow ISI_{PC}$ - 10
\downarrow		write(ISI_{PC})
\uparrow	$read(ISI_{PC})$	
Block2	$T \leftarrow ISI_{PC} * 0.05$	
	$ISI_{PC} \leftarrow ISI_{PC}$ - T	
\downarrow	write(ISI_{PC})	
1	. ,	read(IISc _{PC})
Block3		$IISc_{PC} \leftarrow IISc_{PC} + 10$
		write(IISc _{PC})
\downarrow		commit
ŕ	$read(IISc_{PC})$	
Block4	$IISc_{PC} \leftarrow IISc_{PC} + T$	
	write(IISc _{PC})	
\downarrow	commit	

Consider swapping the instructions between the Blocks 2 and 3.

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Conflict serializability – Example 1

Transaction T_1	Transaction T ₂
	read(ISI _{PC}) write(ISI _{PC})
read(ISI _{PC}) write(ISI _{PC})	
(/	read(IISc _{PC}) write(IISc _{PC})
read(IISc _{PC}) write(IISc _{PC})	

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Concurrent Execution of Transactions

Serializability

Conflict serializability – Example 1

Transaction T_1	Transaction T ₂
	read(ISI _{PC}) write(ISI _{PC})
read(ISI _{PC}) write(ISI _{PC})	
	read(IISc _{PC}) write(IISc _{PC})
read(IISc _{PC}) write(IISc _{PC})	

The above schedule is conflict serializable because it is equivalent to the following serial schedule.

Transaction T_1	Transaction T ₂				
	$read(ISI_{PC})$ write(ISI_{PC}) read(IISc_{PC}) write(IISc_{PC})				
read(ISI _{PC}) write(ISI _{PC}) read(IISc _{PC}) write(IISc _{PC})	(B) (()) (< 王 →	141	୬୯୯



Concurrent Execution of Transactions



Conflict serializability – Example 2

The following schedule is not conflict serializable because it is not equivalent to any serial schedule. Note that, the conflicting instructions write($|SI_{PC})$ in both the transactions can not be swapped.

Transaction T ₁	Transaction T ₂
	read(ISI _{PC})
write(ISI _{PC})	
	write(ISI _{PC})

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View serializability

Definition (View equivalent)

Let S and S' be two schedules with the same set of transactions. S and S' are view equivalent if the following three conditions are met, for each data item Q:

- If in schedule S, transaction T_i reads the initial value of Q, then in schedule S' also transaction T_i must read the initial value of Q.
- If in schedule S transaction T_i executes read(Q), and that value was produced by transaction T_j, then in schedule S' also transaction T_i must read the value of Q that was produced by the same write(Q) operation of transaction T_j.
- The transaction (if any) that performs the final write(Q) operation in schedule S must also perform the final write(Q) operation in schedule S'.



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View serializability

Definition (View serializable)

A schedule S is view serializable if it is view equivalent to a serial schedule.

Note: A conflict serializable schedule is always view serializable but not the vice versa.

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View serializability – An example

Transaction T ₁	Transaction T ₂	Transaction T_3
	$read(ISI_{PC})$	
write(ISI_{PC})		
	write(ISI _{PC})	
		write(ISI _{PC})

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View serializability – An example

Transaction T_1	Transaction T ₂	Transaction T_3
-	read(ISI _{PC})	
write(ISI _{PC})		
	write(ISI _{PC})	
		write(ISI _{PC})

The above schedule is view serializable because it is equivalent to the following serial schedule.

Transaction T ₁	Transaction T ₂	Transaction T_3
-	read(ISI _{PC})	
	write($ S _{PC}$)	
write(ISI _{PC})		
. ,		write(ISI_{PC})

Note: The top schedule is not conflict serializable because the conflicting instructions write($|SI_{PC}|$) both in T_1 and T_2 cannot be swapped to obtain a serial schedule.



Concurrent Execution of Transactions

Serializability

Testing for conflict serializability

We can test conflict serializability through constructing precedence graphs.

Definition (Precedence graph)

Given a schedule *S*, a precedence graph is defined as a directed graph G = (V, E), where the set of vertices *V* consists of all the transactions participating in *S* and *E* consists of all the edges $T_i \rightarrow T_j$ for which one of three conditions holds in *S*: **1** T_i executes write(*Q*) before T_j executes read(*Q*).

- **2** T_i executes read(Q) before T_j executes write(Q).
- **3** T_i executes write(Q) before T_j executes write(Q).

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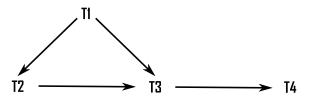


Concurrent Execution of Transactions

Testing for conflict serializability

The precedence graph for a conflict serializable schedule is always acyclic.

The following graph corresponds to a conflict serializable schedule because it is acyclic. Notably, $T1 \rightarrow T2 \rightarrow T3$ is not a cycle.



Note: A directed graph is acyclic if it has no cycle (a sequence of non-repeating directed edges except for the first and last one).

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Outline

Concurrent Execution of Transactions

Testing for conflict serializability

In general, cycle-detection algorithms incur $O(n^2)$ time, where *n* is the order of the graph. However, there exists better algorithms incurring O(n + e) time, where *e* denotes the size of the graph.

From an acyclic precedence graph, the serializability order can be obtained by a topological sorting of the graph.

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