Outline	Data Redundancy	Normalization and Denormalization	Normal Forms
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Database Management Systems Database Normalization

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Data Redundancy

- 2 Normalization and Denormalization
- 3 Normal Forms
 - First Normal Form
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Redundancy in databases

Redundancy in a database denotes the repetition of stored data

Redundancy might cause various anomalies and problems pertaining to storage requirements:

- Insertion anomalies: It may be impossible to store certain information without storing some other, unrelated information.
- <u>Deletion anomalies</u>: It may be impossible to delete certain information without losing some other, unrelated information.
- Update anomalies: If one copy of such repeated data is updated, all copies need to be updated to prevent inconsistency.
- Increasing storage requirements: The storage requirements may increase over time.

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- Update anomalies: If one copy of such repeated data is updated, all copies need to be updated to prevent inconsistency.
- Increasing storage requirements: The storage requirements may increase over time.

These issues can be addressed by decomposing the database – normalization forces this!!!

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Insertion anomaly – An example

Consider the following table (the attributes are not null) detailing some of the cars available in the Kolkata market.

Company	Country	Make	Distributor
Maruti India		WagonR	Carwala
Maruti	India	WagonR	Bhalla
Toyota	Japan	RAV4	CarTrade
BMW	Germany	X1	CarTrade

Suppose Tesla, a company from US, is now collaborating with Toyota to bring the make RAV4 in the Kolkata market with no distributor announced yet.

This insertion is not possible in the above table as the Distributor cannot be null.

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Deletion anomaly – An example

Consider the following table (the attributes are not null) detailing some of the cars available in the Kolkata market.

Company Count		Make	Distributor
Maruti India		WagonR	Carwala
Maruti	India	WagonR	Bhalla
Toyota	Japan	RAV4	CarTrade
BMW	Germany	X1	CarTrade

Suppose CarTrade is no more a distributor for the make X1 of BMW, a company from Germany.

This deletion from the above table would result in the car record being deleted.

Update anomaly – An example

Consider the following table (the attributes are not null) detailing some of the cars available in the Kolkata market.

Company Country		Make	Distributor
Maruti India		WagonR	Carwala
Maruti	India	WagonR	Bhalla
Toyota	Japan	RAV4	CarTrade
BMW	Germany	X1	CarTrade

Suppose Maruti is no more an Indian company due to its 100% procurement by Suzuki Motor Corporation, a company from Japan.

This update is to be made in multiple records in the above table resulting into atomicity challenges.

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An overview of different normal forms in the literature

Normal Form	Details	Reference
1NF (Codd (1970),	Domains should be atomic/At least one can-	[1, 9]
Date (2006))	didate key	
2NF (Codd (1971))	No non-prime attribute is functionally depen-	[2]
	dent on a proper subset of any candidate key	
3NF (Codd (1971),	Every non-prime attribute is non-transitively	[2, 7]
Zaniolo (1982))	dependent on every candidate key	
BCNF (Codd	Every non-trivial functional dependency is a	[3]
(1974))	dependency on a superkey	
EKNF (Zaniolo	Every non-trivial functional dependency is ei-	[7]
(1982))	ther the dependency of an elementary key at-	
	tribute or a dependency on a superkey	
4NF (Fagin (1977))	Every non-trivial multi-valued dependency is	[4]
	a dependency on a superkey	
5NF (Fagin (1979))	Every non-trivial join dependency is implied	[5]
	by the superkeys	
DKNF (Fagin	Every constraint on the table is a logical con-	[6]
(1981))	sequence of the domain and key constraints	
6NF (Date <i>et al</i> .	No non-trivial join dependencies at all (w.r.t	[8]
(2002))	generalized join)	

Image: A matrix

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Motivations behind normalization

Normal Form	Basic Motivation	
1NF	Removing non-atomicity	
2NF	Removing partial dependency (Part of key attribute $ ightarrow$	
	Non-key attribute)	
3NF	Removing transitive dependency (Non-key attribute $ ightarrow$	
	Non-key attribute)	
BCNF	Removing any kind of redundancy	

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Problems with normalization



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Denormalization

Denormalization is the process of converting a normalized

schema to a non-normalized one

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Denormalization

Denormalization is the process of converting a normalized

schema to a non-normalized one

Note: Designers use denormalization to tune performance of systems to support time-critical operations. They assess the cost, benefit, and risk to identify the right normalization level with respect to the data, its use and its quality requirements.

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Normalization versus denormalization



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Applications

Normalization:

- **1** Use of normalization to minimize the impact of various anomalies created with database modification.
- **2** Use of normalization to reduce the data integrity problems.

Denormalization:

- Use of denormalization in case the data is not going to be updated after being created.
- **2** Use of denormalization results into the performance gain.

Note: There is no "ideal" normal form for a table or the data as a whole.

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First normal form

The domain (or value set) of an attribute defines the set of values it might contain.

A domain is *atomic* if elements of the domain are considered to be indivisible units.

Company	Make	
Maruti	WagonR, Ertiga	
Honda	City	
Tesla	RAV4	
Toyota	RAV4	
BMW	X1	

Only Company has atomic domain

Company	Make
Maruti	WagonR, Ertiga
Honda	City
Tesla, Toyota	RAV4
BMW	X1

None of the attributes have atomic domains

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First normal form

Definition (First normal form (1NF))

A relational schema R is in 1NF iff the domains of all attributes in R are *atomic*.

The advantages of 1NF are as follows:

- It eliminates redundancy
- It eliminates repeating groups.

Note: In practice, 1NF includes a few more practical constraints like each attribute must be unique, no tuples are duplicated, and no columns are duplicated.

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First normal form

The following relation is not in 1NF because the attribute Model is not atomic.

Company	Country	Make	Model	Distributor
Maruti	India	WagonR	LXI, VXI	Carwala
Maruti	India	Ertiga	VXI	Carwala
Maruti	India	WagonR	LXI	Bhalla
Honda	Japan	City	SV	Bhalla
Tesla	USA	RAV4	EV	CarTrade
Toyota	Japan	RAV4	EV	CarTrade
BMW	Germany	X1	Expedition	CarTrade

We can convert this relation into 1NF in two ways!!!

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First normal form

Approach 1: Break the tuples containing non-atomic values into multiple tuples.

Company	Country	Make	Model	Distributor
Maruti	India	WagonR	LXI	Carwala
Maruti	India	WagonR	VXI	Carwala
Maruti	India	Ertiga	VXI	Carwala
Maruti	India	WagonR	LXI	Bhalla
Honda	Japan	City	SV	Bhalla
Tesla	USA	RAV4	EV	CarTrade
Toyota	Japan	RAV4	EV	CarTrade
BMW	Germany	X1	Expedition	CarTrade

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First normal form

Approach 2: Decompose the relation into multiple relations.

Company	Country	Make
Maruti	India	WagonR
Maruti	India	Ertiga
Honda	Japan	City
Tesla	USA	RAV4
Toyota	Japan	RAV4
BMW	Germany	X1

Make	Model	Distributor
WagonR	LXI	Carwala
WagonR	VXI	Carwala
Ertiga	VXI	Carwala
WagonR	LXI	Bhalla
City	SV	Bhalla
RAV4	EV	CarTrade
X1	Expedition	CarTrade

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Why data dependencies are so important?

Choose the best keyset for the locks given below.

Locks	Keyset 1	Keyset 2	Keyset 3
\odot	¶	¶	ſ
L1	K1	K1	K3
\odot	¶	¶	ſ
L2	K1	K2	K4
\odot	¶	¶	¶
L3	K1	K3	K5
\odot	¶	ſ	ſ
L3	K1	K4	K5

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\odot	ſ	¶	ſ
L1	K1	K1	K3
\odot	¶	¶	ſ
L2	K1	K2	K4
\odot	ſ	¶	ſ
L3	K1	K3	K5
\odot	l ¶	ſ	ſ
L3	K1	K4	K5

- Keyset 1 is not appropriate because a single key can open multiple locks.
- Keyset 2 is not appropriate because the same lock can be opened with multiple keys.
- Keyset 3 is the best option!!!

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Functional dependency

Consider a relation schema R. A subset $X \subset A(R)$, the attributes in R, is a *superkey* of R if $t1 \neq t2$, for all pairs of tuples $t1, t2 \in R$, implies $t1[X] \neq t2[X]$. This means no two tuples in Rmay have the same value on attribute set X.

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The notion of functional dependency generalizes the notion of superkey. Let $X \subseteq A(R)$ and $Y \subseteq A(R)$. The functional dependency $X \rightarrow Y$ holds on schema R if

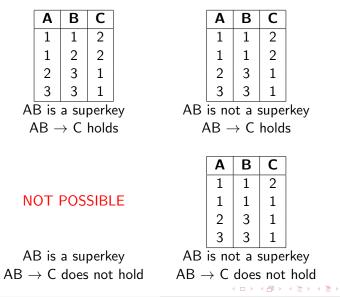
$$t1[X] = t2[X],$$

in any legal relation r(R), for all pairs of tuples t1 and t2 in r, then

$$t1[Y] = t2[Y].$$

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Superkey versus functional dependency



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Partial dependency

The partial dependency $X \to Y$ holds in schema R if there is a $Z \subset X$ such that $Z \to Y$.

We say Y is partially dependent on X if and only if there is a proper subset of X that satisfies the dependency.

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Partial dependency

The partial dependency $X \to Y$ holds in schema R if there is a $Z \subset X$ such that $Z \to Y$.

We say Y is partially dependent on X if and only if there is a proper subset of X that satisfies the dependency.

X	Υ	Ζ
10	10	20
10	20	20
20	30	10
30	30	10

$$XY \rightarrow Z$$
 is a partial dependency

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Note: The dependency $A \rightarrow B$ implies if the A values are same, then the B values are also same.

Second normal form

Definition (Second normal form (2NF))

A relational schema R is in 2NF if each attribute A in R satisfies one of the following criteria:

- 1 A is part of a candidate key.
- 2 A is not partially dependent on a candidate key.

In other words, no non-prime attribute (not a part of any candidate key) is dependent on a proper subset of any candidate key.

Note: A *candidate key* is a *superkey* for which no proper subset is a superkey, i.e. a minimal *superkey*.

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Second normal form

The following relation is in 1NF but not in 2NF because Country is a non-prime attribute that partially depends on Company, which is a proper subset of the candidate key {Company, Make, Model, Distributor}.

Company	Country	Make	Model	Distributor
Maruti	India	WagonR	LXI	Carwala
Maruti	India	WagonR	VXI	Carwala
Maruti	India	Ertiga	Ertiga VXI	
Maruti	India	WagonR	LXI	Bhalla
Honda	Japan	City	SV	Bhalla
Tesla	USA	RAV4	EV	CarTrade
Toyota	Japan	RAV4	EV	CarTrade
BMW	Germany	X1	Expedition	CarTrade

We can convert this relation into 2NF!!!

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Second normal form

Company	Country	Make	Model	Distributor
Maruti	India	WagonR	LXI	Carwala
Maruti	India	WagonR	VXI	Carwala
Maruti	India	Ertiga	VXI	Carwala
Maruti	India	WagonR	LXI	Bhalla
Honda	Japan	City	SV	Bhalla
Tesla	USA	RAV4	EV	CarTrade
Toyota	Japan	RAV4	EV	CarTrade
BMW	Germany	X1	Expedition	CarTrade

• {Company, Make, Model, Distributor} \rightarrow Country

• Company \rightarrow Country (Violating 2NF)

Note: Country is partially dependent on {Company, Make, Model, Distributor}.

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Second normal form

Approach: Decompose the relation into multiple relations.

		Company	Make	Model	Distributor
Company	Country	Maruti	WagonR	LXI	Carwala
Maruti	India	Maruti	WagonR	VXI	Carwala
		Maruti	Ertiga	VXI	Carwala
Honda	Japan	Maruti	WagonR	LXI	Bhalla
Tesla	USA	Honda	City	SV	Bhalla
Toyota	Japan	Tesla	RAV4	FV	CarTrade
BMW	Germany				
		Toyota	RAV4	EV	CarTrade
		BMW	X1	Expedition	CarTrade

Note: Each attribute in the left relation is either a part of the candidate key {Company} or having full functional dependency on it, and in the right relation is a part of the candidate key {Company, Make, Model, Distributor}.

Functional dependency

Armstrong's axioms:

- Reflexivity property: If X is a set of attributes and Y ⊆ X, then X → Y holds. (known as trivial functional dependency)
- Augmentation property: If X → Y holds and γ is a set of attributes, then γX → γY holds.
- **Transitivity property**: If both $X \to Y$ and $Y \to Z$ holds, then $X \to Z$ holds.

Functional dependency

Armstrong's axioms:

- Reflexivity property: If X is a set of attributes and Y ⊆ X, then X → Y holds. (known as trivial functional dependency)
- Augmentation property: If X → Y holds and γ is a set of attributes, then γX → γY holds.
- **Transitivity property**: If both $X \to Y$ and $Y \to Z$ holds, then $X \to Z$ holds.

Other properties:

- Union property: If $X \to Y$ holds and $X \to Z$ holds, then $X \to YZ$ holds.
- **Decomposition property**: If $X \to YZ$ holds, then both $X \to Y$ and $X \to Z$ holds.
- **Pseudotransitivity property**: If $X \to Y$ and $\gamma Y \to Z$ holds, then $X\gamma \to Z$ holds.

Closure of functional dependencies (FDs)

We can find F^+ , the closure of a set of FDs F, as follows:

```
Initialize F^+ with F
```

repeat

for each functional dependency $f = X \rightarrow Y \in F^+$ do

Apply reflexivity and augmentation properties on f and include the resulting functional dependencies in ${\cal F}^+$

- end for
- for each pair of functional dependencies $f_1, f_2 \in F^+$ do

if f_1 and f_2 can be combined together using the transitivity property then

Include the resulting functional dependency in F^+

end if

end for

until F^+ does not further change

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Closure of functional dependencies (FDs) – An example

Consider a relation $R = \langle UVWXYZ \rangle$ and the set of FDs = {U \rightarrow V, U \rightarrow W, WX \rightarrow Y, WX \rightarrow Z, V \rightarrow Y}. Let us compute some non-trivial FDs that can be obtained from this.

By applying the augmentation property, we obtain
UX → WX (from U → W)
WX → WXZ (from WX → Z)
WXZ → YZ (from WX → Y)
By applying the transitivity property, we obtain
U → Y (from U → V and V → Y)
UX → Z (from UX → WX and WX → Z)
WX → YZ (from WX → WXZ and WXZ → YZ)

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Closure of attribute sets

We can find A^+ , the closure of a set of attributes A, as follows:

```
Initialize A^+ with A

repeat

for each functional dependency f = X \rightarrow Y \in F^+ do

if X \subseteq A^+ then

A^+ \leftarrow A^+ \cup Y

end if

end for

until A^+ does not further change
```

Note: The closure is defined as the set of attributes that are functionally determined by A under a set of FDs F.

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Closure of attribute sets

The usefulness of finding attribute closure is as follows:

Testing for superkey

– Compute A^+ and check whether $\mathcal{A}(R) \subseteq A^+$ and all the tuples are distinct.

- Testing functional dependencies
 - To check if an FD X \rightarrow Y holds, just check if Y \subseteq X^+
 - Same for checking if $X \rightarrow Y$ is in F^+ for a given F
- Computing closure of F
 - For each $A \subseteq \mathcal{A}(R)$, we find the closure A^+ , and for each
 - $S \subseteq A^+$, we output a functional dependency A o S

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Closure of attribute sets

The usefulness of finding attribute closure is as follows:

Testing for superkey

– Compute A^+ and check whether $\mathcal{A}(R) \subseteq A^+$ and all the tuples are distinct.

- Testing functional dependencies
 - To check if an FD X \rightarrow Y holds, just check if Y \subseteq X^+
 - Same for checking if $X \to Y$ is in F^+ for a given F
- Computing closure of F
 - For each $A \subseteq \mathcal{A}(R)$, we find the closure A^+ , and for each
 - $S\subseteq A^+$, we output a functional dependency A o S

<u>Note</u>: Even though a subset of attributes X functionally defines the other attributes, it cannot be a superkey until and unless all the tuples are distinct.

Closure of attribute sets – An example

Consider a relation $R = \langle UVWXYZ \rangle$ and the set of FDs = {U \rightarrow V, U \rightarrow W, WX \rightarrow Y, WX \rightarrow Z, V \rightarrow Y}. Let us compute UX⁺, i.e., the closure of UX.

Initially UX⁺ = UX

- Then we have $UX^+ = UVX$ (as $U \rightarrow V$ and $U \subseteq UX$)
- Then we have $UX^+ = UVWX$ (as $U \rightarrow W$ and $U \subseteq UVX$)
- Then we have $UX^+ = UVWXY$ (as $WX \rightarrow Y$ and $WX \subseteq UVWX$)
- Finally, we have $UX^+ = UVWXYZ$ (as $WX \rightarrow Z$ and $WX \subseteq UVWXY$)

Note: The closure of UX covers all the attributes in *R*.

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Decomposition of a relation

If a relation is not in a desired normal form, it can be decomposed into multiple relations such that each decomposed relation satisfies the required normal form.

Suppose a relation R consists of a set of attributes $\mathcal{A}(R) = \{A_1, A_2, \dots, A_n\}$. A *decomposition* of R replaces R by a set of (two or more) relations $\{R_1, \dots, R_m\}$ such that both the following conditions hold:

■
$$\forall i : \mathcal{A}(R_i) \subset \mathcal{A}(R)$$

■ $\mathcal{A}(R_1) \cup \cdots \cup \mathcal{A}(R_m) = \mathcal{A}(R)$

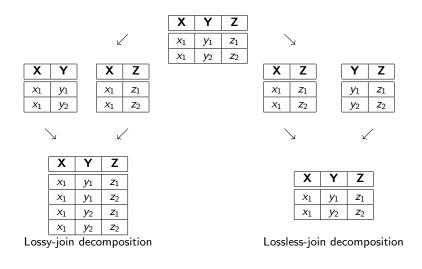


Decomposition criteria

The decomposition of a relation might aim to satisfy different criteria as listed below:

- Preservation of the same relation through join (lossless-join)
- Dependency preservation
- Repetition of information

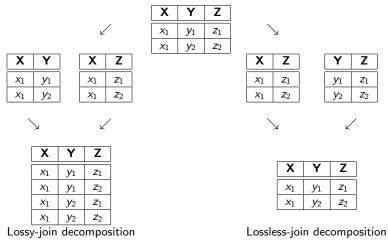
Preservation of the same relation through join



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Preservation of the same relation through join



Is the decomposition into $\langle XY \rangle$ and $\langle YZ \rangle$ lossy or lossless?

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Testing for lossless-join decomposition

A decomposition of R into $\{R_1, R_2\}$ is *lossless-join*, iff $\mathcal{A}(R_1) \cap \mathcal{A}(R_2) \to \mathcal{A}(R_1)$ or $\mathcal{A}(R_1) \cap \mathcal{A}(R_2) \to \mathcal{A}(R_2)$ in F^+ .

Consider the example of a relation $R = \langle UVWXY \rangle$ and the set of FDs = {U \rightarrow VW, WX \rightarrow Y, V \rightarrow X, Y \rightarrow U}.

Note that, the decomposition $R_1 = \langle UVW \rangle$ and $R_2 = \langle WXY \rangle$ is not lossless-join because $R_1 \cap R_2 = W$, and W is neither a key for R_1 nor for R_2 .

However, the decomposition $R_1 = \langle UVW \rangle$ and $R_2 = \langle UXY \rangle$ is lossless-join because $R_1 \cap R_2 = U$, and U is a key for R_1 .

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Dependency preservation

The decomposition of a relation R with respect to a set of FDs F replaces R with a set of (two or more) relations $\{R_1, \ldots, R_m\}$ with FDs $\{F_1, \ldots, F_m\}$ such that F_i is the subset of dependencies in F^+ (the closure of F) that include only the attributes in R_i .

The decomposition is *dependency preserving* iff $(\cup_i F_i)^+ = F^+$.

<u>Note</u>: Through dependency preserving decomposition, we want to minimize the cost of global integrity constraints based on FDs' (i.e., avoid big joins in assertions).

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Testing for dependency preserving decomposition

Consider the example of a relation $R = \langle XYZ \rangle$, having the key X, and the set of FDs = {X \rightarrow Y, Y \rightarrow Z, X \rightarrow Z}.

Note that, the decomposition $R_1 = \langle XY \rangle$ and $R_2 = \langle XZ \rangle$ is lossless-join but not dependency preserving because $F_1 = \{X \rightarrow Y\}$ and $F_2 = \{X \rightarrow Z\}$ incur the loss of the FD $\{Y \rightarrow Z\}$, resulting into $(F_1 \cup F_2)^+ \neq F^+$.

However, the decomposition $R_1 = \langle XY \rangle$ and $R_2 = \langle YZ \rangle$ is lossless-join and also dependency preserving because $F_1 = \{X \rightarrow Y\}$ and $F_2 = \{Y \rightarrow Z\}$, satisfying $(F_1 \cup F_2)^+ = F^+$.

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Third normal form

Definition (Third normal form (3NF))

A relational schema R is in 3NF if for every non-trivial functional dependency $X \rightarrow A$, where $X \cap A = \emptyset$, one of the following statements is true:

- **1** X is a superkey of R.
- **2** A is a part of any candidate key of R.

Note: A *superkey* is a set of one or more attributes that can uniquely identify an entity in the entity set.

Third normal form

The following relation is in 2NF but not in 3NF because Country is a non-prime attribute that depends on Company, which is again a non-prime attribute. Notably, the candidate key in this relation is {PID}.

PID	Company	Country	Make	Model	Distributor
P01	Maruti	India	WagonR	LXI	Carwala
P02	Maruti	India	WagonR	VXI	Carwala
P03	Maruti	India	Ertiga	VXI	Carwala
P04	Maruti	India	WagonR	LXI	Bhalla
P05	Honda	Japan	City	SV	Bhalla
P06	Tesla	USA	RAV4	EV	CarTrade
P07	Toyota	Japan	RAV4	EV	CarTrade
P08	BMW	Germany	X1	Expedition	CarTrade

We can convert this relation into 3NF!!!

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Third normal form

PID	Company	Country	Make	Model	Distributor
P01	Maruti	India	WagonR	LXI	Carwala
P02	Maruti	India	WagonR	VXI	Carwala
P03	Maruti	India	Ertiga	VXI	Carwala
P04	Maruti	India	WagonR	LXI	Bhalla
P05	Honda	Japan	City	SV	Bhalla
P06	Tesla	USA	RAV4	EV	CarTrade
P07	Toyota	Japan	RAV4	EV	CarTrade
P08	BMW	Germany	X1	Expedition	CarTrade

PID \rightarrow {Company, Country, Make, Model, Distributor}

• {Company, Make, Model, Distributor} \rightarrow Country (Violating 3NF)

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Third normal form

Approach: Decompose the relation into multiple relations.

		PID	Company	Make	Model	Distributor
Company	Country	P01	Maruti	WagonR	LXI	Carwala
Maruti	India	P02	Maruti	WagonR	VXI	Carwala
		P03	Maruti	Ertiga	VXI	Carwala
Honda	Japan	P04	Maruti	WagonR	LXI	Bhalla
Tesla	USA	P05	Honda	City	SV	Bhalla
Toyota	Japan	P06	Tesla	RAV4	EV	CarTrade
BMW	Germany	P07	Toyota	RAV4	EV	CarTrade
		P08	BMW	X1	Expedition	CarTrade

Note: Each non-trivial functional dependency in the left relation is on the superkey {Company}, and in the right relation is on the superkey {PID}.

Boyce-Codd normal form

Definition (Boyce-Codd normal form (BCNF))

A relational schema R is in BCNF if for every non-trivial functional dependency $X \rightarrow A$, where $X \cap A = \emptyset$, X is a superkey of R.

Note: A *superkey* is a set of one or more attributes that can uniquely identify an entity in the entity set.

Boyce-Codd normal form

The following relation is in 3NF but not in BCNF because the attribute Distributor, which depends on the non-key attribute ShopID, is a part of the key. Notably, the candidate key in this relation is {Company, Make, Model, Distributor}.

Company	Make	Model	Distributor	ShopID
Maruti	WagonR	LXI	Carwala	S1
Maruti	WagonR	VXI	Carwala	S1
Maruti	Ertiga	VXI	Carwala	S2
Maruti	WagonR	LXI	Bhalla	S3
Honda	City	SV	Bhalla	S4
Tesla	RAV4	EV	CarTrade	S5
Toyota	RAV4	EV	CarTrade	S5
BMW	X1	Expedition	CarTrade	S6
BMW	X1	Expedition	CarTrade	S6

We can convert this relation into BCNF!!!

Boyce-Codd normal form

Company	Make	Model	Distributor	ShopID
Maruti	WagonR	LXI	Carwala	S1
Maruti	WagonR	VXI	Carwala	S1
Maruti	Ertiga	VXI	Carwala	S2
Maruti	WagonR	LXI	Bhalla	S3
Honda	City	SV	Bhalla	S4
Tesla	RAV4	EV	CarTrade	S5
Toyota	RAV4	EV	CarTrade	S5
BMW	X1	Expedition	CarTrade	S6
BMW	X1	Expedition	CarTrade	S6

- {Company, Make, Model, Distributor} \rightarrow ShopID
- ShopID → Distributor (Violating BCNF)

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Boyce-Codd normal form

Approach: Decompose the relation into multiple relations.

		Company	Make	Model	ShopID
Distributor	ShopID	Maruti	WagonR	LXI	\$1
Carwala	S1	Maruti	WagonR	VXI	S1
Carwala	S2	Maruti	Ertiga	VXI	S2
Bhalla	S3	Maruti	WagonR	LXI	S3
Bhalla	S4	Honda	City	SV	S4
CarTrade	S5	Tesla	RAV4	EV	S5
CarTrade	S6	Toyota	RAV4	EV	S5
		BMW	X1	Expedition	S6

Note: Each non-trivial functional dependency in the left relation is on the superkey {ShopID}. What about the relation in the right?

Decomposition into BCNF – An algorithm

Result := $\{R\}$ and flag := FALSE Compute F^+ while NOT flag do **if** There is a schema $R_i \in Result$ that is not in BCNF **then** Let $X \to Y$ be a non-trivial functional dependency that holds on R_i such that $(X \to R_i) \notin F^+$ and $X \cap Y = \phi$. Result := $(Result - R_i) \cup (R_i - Y) \cup (X, Y) //$ This is simply decomposing R into R - Y and XY provided $X \rightarrow Y$ in R violates BCNF else flag := TRUEend if

end while

Decomposition into BCNF – An algorithm

Result := $\{R\}$ and flag := FALSE Compute F^+ while NOT flag do **if** There is a schema $R_i \in Result$ that is not in BCNF **then** Let $X \to Y$ be a non-trivial functional dependency that holds on R_i such that $(X \to R_i) \notin F^+$ and $X \cap Y = \phi$. Result := $(Result - R_i) \cup (R_i - Y) \cup (X, Y) //$ This is simply decomposing R into R - Y and XY provided $X \rightarrow Y$ in R violates BCNF else flag := TRUEend if end while

Note: This decomposition process ensures lossless property.

Decomposition into BCNF – Example I

Consider a relation $R = \langle ABCDE \rangle$ having the functional dependencies $\{A \rightarrow BC, C \rightarrow DE\}$.

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Decomposition into BCNF – Example I

Consider a relation $R = \langle ABCDE \rangle$ having the functional dependencies $\{A \rightarrow BC, C \rightarrow DE\}$.

Solution: The attribute closures provide $A^+ = ABCDE$, $B^+ = B$, $C^+ = CDE$, $D^+ = D$, and $E^+ = E$. Hence, A is the key of R.

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Decomposition into BCNF – Example I

Consider a relation $R = \langle ABCDE \rangle$ having the functional dependencies $\{A \rightarrow BC, C \rightarrow DE\}$.

Solution: The attribute closures provide $A^+ = ABCDE$, $B^+ = B$, $C^+ = CDE$, $D^+ = D$, and $E^+ = E$. Hence, A is the key of R.

Note that, the functional dependency A \rightarrow BC does not violate BCNF but C \rightarrow DE does violate. By applying C \rightarrow DE, we decompose *R* and obtain <ABC> and <CDE>.

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Decomposition into BCNF – Example I

Consider a relation $R = \langle ABCDE \rangle$ having the functional dependencies $\{A \rightarrow BC, C \rightarrow DE\}$.

Solution: The attribute closures provide $A^+ = ABCDE$, $B^+ = B$, $C^+ = CDE$, $D^+ = D$, and $E^+ = E$. Hence, A is the key of R.

Note that, the functional dependency A \rightarrow BC does not violate BCNF but C \rightarrow DE does violate. By applying C \rightarrow DE, we decompose *R* and obtain <ABC> and <CDE>.

Now both <ABC> (A is the key) and <CDE> are in BCNF (C is the key).

Decomposition into BCNF – Example II

Suppose a relation $R = \langle ABCD \rangle$ is given with the functional dependencies $\{AB \rightarrow C, B \rightarrow D, C \rightarrow A\}$.

Decomposition into BCNF – Example II

Suppose a relation $R = \langle ABCD \rangle$ is given with the functional dependencies $\{AB \rightarrow C, B \rightarrow D, C \rightarrow A\}$.

Solution: The attribute closures provide $A^+ = A$, $B^+ = BD$, $C^+ = AC$, $D^+ = D$, $AB^+ = ABCD$, and $BC^+ = ABCD$. Hence, AB and BC are the keys of R. Note that, the functional dependency $AB \rightarrow C$ does not violate BCNF but $B \rightarrow D$ and $C \rightarrow A$ do violate. By applying $B \rightarrow D$, we decompose R and obtain $\langle ABC \rangle$ and $\langle BD \rangle$.

Decomposition into BCNF – Example II

Suppose a relation $R = \langle ABCD \rangle$ is given with the functional dependencies $\{AB \rightarrow C, B \rightarrow D, C \rightarrow A\}$.

Solution: The attribute closures provide $A^+ = A$, $B^+ = BD$, $C^+ = AC$, $D^+ = D$, $AB^+ = ABCD$, and $BC^+ = ABCD$. Hence, AB and BC are the keys of R. Note that, the functional dependency $AB \rightarrow C$ does not violate BCNF but $B \rightarrow D$ and $C \rightarrow A$ do violate. By applying $B \rightarrow D$, we decompose R and obtain $\langle ABC \rangle$ and $\langle BD \rangle$.

Now $\langle BD \rangle$ is in BCNF (B is the key) but not $\langle ABC \rangle$. The functional dependency C \rightarrow A violates BCNF. By applying C \rightarrow A, we further decompose $\langle ABC \rangle$ and obtain $\langle BC \rangle$ and $\langle CA \rangle$. Now $\langle BD \rangle$, $\langle BC \rangle$ and $\langle CA \rangle$ are all in BCNF.

Decomposition into BCNF – Example II

Suppose a relation $R = \langle ABCD \rangle$ is given with the functional dependencies $\{AB \rightarrow C, B \rightarrow D, C \rightarrow A\}$.

Solution: The attribute closures provide $A^+ = A$, $B^+ = BD$, $C^+ = AC$, $D^+ = D$, $AB^+ = ABCD$, and $BC^+ = ABCD$. Hence, AB and BC are the keys of R. Note that, the functional dependency $AB \rightarrow C$ does not violate BCNF but $B \rightarrow D$ and $C \rightarrow A$ do violate. By applying $B \rightarrow D$, we decompose R and obtain $\langle ABC \rangle$ and $\langle BD \rangle$.

Now $\langle BD \rangle$ is in BCNF (B is the key) but not $\langle ABC \rangle$. The functional dependency C \rightarrow A violates BCNF. By applying C \rightarrow A, we further decompose $\langle ABC \rangle$ and obtain $\langle BC \rangle$ and $\langle CA \rangle$. Now $\langle BD \rangle$, $\langle BC \rangle$ and $\langle CA \rangle$ are all in BCNF.

Note: This BCNF decomposition does not preserve dependencies.

Comments

Note that

- BCNF is stronger than 3NF if a schema R is in BCNF then it is also in 3NF.
- 3NF is stronger than 2NF if a schema *R* is in 3NF then it is also in 2NF.
- 2NF is stronger than 1NF if a schema R is in 2NF then it is also in 1NF.

Comparison

	Preservation of	Functional
Decomposition	the same relation	dependency
	through join	preservation
1NF	lossless	kept
2NF	lossless	kept
3NF	lossless	kept
BCNF	lossless	lost

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Elementary key normal form

Definition (Elementary key normal form (EKNF))

A relational schema R is in EKNF if for every non-trivial functional dependency $X \rightarrow A$, one of the following statements is true:

- **1** X is a superkey of R.
- **2** X is an elementary key attribute

<u>Note</u>: A non-trivial functional dependency $X \to Y$ is an elementary dependency if there exist no partial dependency. A key K is elementary key if $K \to Y$ is an elementary dependency.

Multi-valued dependency

Consider a relation schema R, and let $X \subseteq R$ and $Y \subseteq R$. The functional dependency $X \twoheadrightarrow Y$ holds on schema R if

$$t1[X] = t2[X],$$

in any legal relation r(R), for all pairs of tuples t1 and t2 in r, implies

where the two tuples t3 and t4 are also in r and Z denotes $R - (X \cup Y)$.

Multi-valued dependency

Consider a relation schema R, and let $X \subseteq R$ and $Y \subseteq R$. The functional dependency $X \twoheadrightarrow Y$ holds on schema R if

$$t1[X] = t2[X],$$

in any legal relation r(R), for all pairs of tuples t1 and t2 in r, implies

•
$$t1[X] = t2[X] = t3[X] = t4[X]$$

• $t1[Y] = t3[Y]$ and $t2[Y] = t4[Y]$
• $t1[Z] = t4[Z]$ and $t2[Z] = t3[Z]$
where the two tuples $t3$ and $t4$ are also in r and Z denotes $R - (X \cup Y)$.

Note: The tuples t1, t2, t3 and t4 are not necessarily distinct.

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Visualizing multi-valued dependency

	X	Y	$R-(X\cup Y)$
t1	- '	$m_{i+1}m_j$	$m_{j+1}m_k$
t2	m_1m_i	$n_{i+1}n_i$	$n_{j+1}n_k$

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Visualizing multi-valued dependency

	X	Y	$R-(X\cup Y)$
t1	<i>m</i> ₁ <i>m_i</i>	$m_{i+1}m_j$	$m_{j+1}m_k$
t2	m_1m_i	$n_{i+1}n_i$	$n_{j+1}n_k$
t3	m_1m_i	$m_{i+1}m_j$	$n_{j+1}n_k$
<i>t</i> 4	<i>m</i> 1 <i>m</i> i	$n_{i+1}n_i$	$m_{j+1}m_k$

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Visualizing multi-valued dependency

	X	Y	$R-(X\cup Y)$
t1	m_1m_i	$m_{i+1}m_j$	$m_{j+1}m_k$
t2	<i>m</i> ₁ <i>m_i</i>	$n_{i+1}n_i$	$n_{j+1}n_k$
t3	m_1m_i	$m_{i+1}m_{j}$	$n_{j+1}n_k$
t4	m1mi	$n_{i+1}n_i$	$m_{j+1}m_k$

An example of $X \twoheadrightarrow Y$

Inference rules for multi-valued dependency

- If $X \twoheadrightarrow Y$ holds, then $X \twoheadrightarrow (R (X \cup Y))$ holds.
- If $X \twoheadrightarrow Y$ holds and $W \supseteq Z$, then $WX \twoheadrightarrow YZ$ holds.
- If $X \rightarrow Y$ and $Y \rightarrow Z$ both holds, then $X \rightarrow (Z Y)$ holds.
- If $X \to Y$ holds, then $X \twoheadrightarrow Y$ holds.
- If $X \to Y$ holds and there exists W such that (a) $W \cap Y = \phi$, (b) $W \to Z$ and (c) $Y \supseteq Z$, then $X \to Z$ holds.

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Fourth normal form

Definition (Fourth normal form (4NF))

A relational schema R is in 4NF if for every non-trivial multi-valued dependency $X \rightarrow A$, X is a superkey of R.

Note: A *superkey* is a set of one or more attributes that can uniquely identify an entity in the entity set.



Fourth normal form

The following relation is not in 4NF because it satisfies the multi-valued dependency Name \rightarrow Age in which Name is not a superkey.

Name	Age	Codeword	Media
Irfan	28	abc	News
Irfan	40	xyz	Radio
Irfan	40	abc	News
Irfan	28	xyz	Radio
Imran	42	abc	News

We can convert this relation into 4NF!!!

Fourth normal form

Approach: Decompose the relation into multiple relations.

Name	Age	Name	Codeword	Media
Irfan	28	Irfan	abc	News
Irfan	40	Irfan	xyz	Radio
Imran	42	Imran	abc	News

Note: No multi-valued dependency exists in the decomposed relations.

Decomposition into 4NF – An algorithm

Result := {R} and flag := FALSE Compute D^+ // Given schema R_i , let D_i denote the restriction of D^+ to R_i

while NOT flag do

if There is a schema $R_i \in Result$ that is not in 4NF w.r.t. D_i then

Let $X \to Y$ be a non-trivial functional dependency that holds on R_i such that $(X \to R_i) \notin D_i$ and $X \cap Y = \phi$. Result := $(Result - R_i) \cup (R_i - Y) \cup (X, Y) //$ Decompose R into R - Y and XY provided $X \to Y$ in R violates 4NF else

flag := TRUE
end if
end while

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Decomposition into 4NF – An algorithm

Result := {R} and flag := FALSE Compute D^+ // Given schema R_i , let D_i denote the restriction of D^+ to R_i

while NOT flag do

if There is a schema $R_i \in Result$ that is not in 4NF w.r.t. D_i then

Let $X \twoheadrightarrow Y$ be a non-trivial functional dependency that holds on R_i such that $(X \to R_i) \notin D_i$ and $X \cap Y = \phi$. Result := $(Result - R_i) \cup (R_i - Y) \cup (X, Y) //$ Decompose R into R - Y and XY provided $X \twoheadrightarrow Y$ in R violates 4NF else

end while

Note: The decomposition process ensures lossless property



Join dependency

Given a relation schema R, a join dependency $JD(R_1, R_2, \ldots, R_n)$ is defined by the constraint that every legal relation r(R) should have a non-additive join decomposition into R_1, R_2, \ldots, R_n , i.e. for every such r we have

$$(\pi_{R_1}(r),\pi_{R_2}(r),\ldots,\pi_{R_n}(r))=r.$$

Note: Multi-valued dependency is a special case of join dependency where n = 2.

Fifth normal form

Definition (Fifth normal form (5NF))

A relational schema R is in 5NF if for every non-trivial join dependency $JD(R_1, R_2, ..., R_n)$ in F^+ , every R_i is a superkey of R.

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Fifth normal form

Definition (Fifth normal form (5NF))

A relational schema R is in 5NF if for every non-trivial join dependency $JD(R_1, R_2, ..., R_n)$ in F^+ , every R_i is a superkey of R.

Note: 5NF is also known as project-join normal form.

Domain key normal form

Definition (Domain key normal form (DKNF))

A relational schema R is in DKNF if all the constraints and dependencies that should hold on the valid relation states is a logical consequence of the domain and key constraints on the relation.

Sixth normal form

Definition (Sixth normal form (6NF))

A relational schema R is in 6NF if there exists no non-trivial join dependencies at all (with reference to generalized join operator).

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