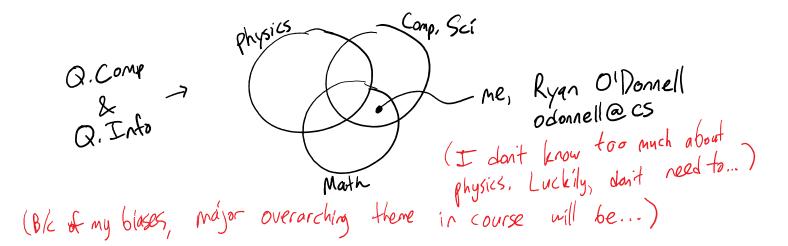
15-459 Undergrad Computation Quantum 10⁵⁰⁰ parallel universes
Rotate, compute, rotate (two lettinotitis for the Pavid Deutsch, coounder of quantum computing: "Quantum computing is... nothing less than a distinctively new way of harnessing nature... it will be the first technology that allows useful tasks to be performed in collaboration between parallel universes." -from 600k "Fabric of " Reality" (Ill Ain't that great? Who wouldn't want to take a class learning about that? Now, I agree with the first part of the quote - second part is ... a bit grand sounding ... Brings us to and leit motif, which we'll discuss in and letture: how Q.C. is also not so mystical/grand at all -just a small twist ("rotation") on everyday computing. Dual themes in course: . Q.C. is otherworkly/extraordinary lec.1 . Q.C. is straightforward & easy to learn.) lec.2



Computational complexity/efficiency (off-used word meaning "non-quantum") · Are Q, computers more 'powerful' than classical ones? · For which computational (/communication/info.) tasks? · Near-term propects for demonstrating such? (Already done for some info-theoretic tasks) (Want to spend a chunk of this lecture talking about computational efficiency, Independent of quantum vs. classical distinction.)

Physical us, unphysical numbers (For TCS compossion, I'm shothing
O() and P vs. EXP ideas been.)
10 - fingers (We normally care about #'s because they count physical
grantities)
100 - (# of blacks needed to bailed a lox(0 wall in Minecraft)
1000 =
$$a^{10}$$
 (I'm a C.S.ist, we count in powers of a :
Naive been in a room w/ 1000 people before)
1mil = $10^6 = a^{30}$ (Still not too band to immyine, People in Pithéagh.
Jellybeans in jellybean back - would fit in a car.
1mil = $10^6 = a^{30}$ (Still not too get serious. IB sec. = 315 years,
000, I'm a C.S.ist, we could fit in a car.
1mil = $10^6 = a^{30}$ (Stirth to get serious. IB sec. = 315 years,
000, I'm I'm zec. = 161/sec is clack speed of a compt
168 HDD no biggie: her 8611 (He myneticed regions that.)
169 = a^{40} (Itri sec = 30k years FLOPS of a flagstrian.
178 HDD still no biggie, but don't to talloc. an arry this
 a^{50} (1000 ITB HDDs. 50 DO TB HDDS)
 a^{60} (Storage of huge Gougle/NSA dota cater? FLOPS of
world's fistest supercompter)
 a^{64} (# of mem, loss nameable on a std. 64-611 compter)
 $10^{50} \approx a^{150}$ (Gillions of supercompters operations???)
 $10^{50} \rightarrow alem. particles in observable universe.
Physical #'s (Hey could conceivably courd something)
Unphysical #: 10^{500} , e.g.
Nute: its easy to write the name of such a #
 $SOO digits$ (Dishes - could do it sy and in Smiss.
Tost would and regenerating Physic.$

Computational challenge 1: Multiply two given 500-digit numbers (wtty would you want to do this is a good q. Doesn't co to any physical concept like blacks in a Minecraft wall.) As title says, just consider it to be a "challenge". a good q. Doesn't corresp. 1234567890123456789012345 Your phone (comp. has a chip that can, 1B/sec, ×3(41592653589793238462643 myHi two 64-6it = 20-digit #'s. But we have 500-digit #'s, so need to store in two (In C, reed to write a 10-line prog. Built into Python. You know one from 3rd grade.) # steps alg. takes... and how that scales as fcn. of input length. 1 if 500 digs × 500 digs, tableau is ~ 500° Jigits, n-digit mult: $\approx n^2$ operations (phone can do in 1 millisec.) La P-algorithm (l= physical P= polynomial # of steps) (emphasize: if n=106 = 1 mil: the 2 numbers represent unphysical gtys. But as computer alg. input/outputs, they're of physically ok lens.) Can mult. two mil-digit tis in I sec on a Playstation.) (Well, 1 sec is OK, but Comp. (xty always asks...) Faster Alg... (Possibly you hadn't even considered other mult, algs!) -> Yes! (Schönhage & Strassen ca. 1970.) n-digit × n-digit mult. in ~n (well, ~n. byn) steps! Uses Fast Fourier Transform (with this, can mult two mil-dig. #'s in a microsec. on PS4)

(Major: ty?) of people believe there isn't. At last, they bank on it.] (The assumption that it's not in P is basis of almost all crypto.) (What does factoring have to do ul crypto? Presumarily you know a little a bout RSA, but...) Multiplication > encrypting (the central paradigm in crypto -> easy > (Any time you go to a webpage w/ https, security relies on de facto impossibility of factoring hard factoring 1024-6H #'s) 2048, 15 of 2013

Punchline: [Probably not a poiler if you know even a little about Q.C.] Reter Shor, 1994: A Q.C. (if built) could factor n-bit #'s in $\approx n^2$ steps. In \mathbf{P} ! (on Q.C.) Factors 500-digit # in a few mil. steps [1 second, if at speed w?! We'll see, but relies on 'distinctively new way of harnessing nature") destroys all past (rypto!!] (How?, We'll see, Gut relies on "distinctively new way of harnessing nature") Uses basic fact of quantum mechanics: given, e.g., 1000 photons/electrons/..., their joint "state" is defined by 2'000 numbers ("amplitudes") G.C. expert Unesh Vazirani (of the videos): "We would like to hack into Nature's computer!")

(Q.C. cofounder Deutsch: Shor's alg. is a dramatic illustration of existence of parallel universes (!!!??!!?). 10500 of them, if you're factoring 500-digit tis...)

"When a quantum factorization engine is factorizing a 250-digit number, the number of interfering universes will be of the order of 10^500. This staggeringly large number is the reason why Shor's algorithm makes factorization tractable. I said [earlier in the book] that the algorithm requires only a few thousand [or maybe a million] operations. I meant, of course, a few thousand parallel operations in each universe that contributes to the answer. All those computations are performed in parallel, in different universes, and share their results through interference."

(Here Deutsch is espousing a certain "interpretation" of Q.M. called the Many Worlds Interpretation - Hugh Evenett, 1956/57 (There are a lot of philosophical gis surrounding Q.M.is. Not around the math, or the physical predictions it makes. These of 100% solid. but what to make of this 2¹⁰⁰⁰ #'s to store for 1000 particles? Or of the "measurement issue" - Schrödinger's Cat, etc.? Don't need to know, for this course. But for fun, 7'll tellyou a teeny bit about Everett & MWI, which is a minority apinion - but not overwhelming minority. Definitely preferred by many Serious, non-fringe physicists (eg. Deutsch). I kinda like it...)

(Everett: M.Sc. with Albert Tucker, a proto CSist, on military game theory.) Tucker M.Sc. Wheeler (farrows physicist - "blackhole", "wormhole") Everet Ph.D. on MWI Feynman Minsley (Scorned by physicists M. Blum (CMU) Deutsch Everett went to Pertagon, U. Vazirani Other colounder did computer Modeling of nukes. Switched to O.R. Became computer consultant.) Sudan More on he (Early '70s: physicist Bryce Dewitt began later. promoting Exercit's work. Late 705; started to get taken seriously, Griffiths (CMU, 1964-retirent) including by Wheeler's student-) (But around a lot, (1956 MWI thesis typed by Everet's fature has Ph() student...) wife Nancy - Heir kid Mark (aka "E") is frontman of band ER(S.)

(In case your soul is shahen by the concept of 10⁵⁰⁰ parallel universes, let me offer some no vocaine: · don't have to accept/understand MWI for Q.C.; just for fun · Leitmotif Q, "rotate, compute, rotate": as I'll sletch next time, Q.C. is not too complicated.)

Feynman: "It is safe to say that nobody understands quantum mechanics." (But that's just the 'interpretation'; in the end, it's just math.) Von Neumann [founder of the mathematics of Q.M.]:

"In mathematics, you don't understand things. You just get used to them." Me: "It is safe to say that any old graduate student can understand quantum computation."

(In this course, we'll spend a bunch of lectures getting used to the math of Q,M, & Q.C. We'll also see (ots of simple & fun applications of very basic quantum infor theory quantum money, secret key exchange, teleportation... then we'll get into Quantum computation, and finish Shor's alg... & still there will be half the course to go, So really Shor's not too bad...)

(Shoi's alg from 194. He was a well-lenour TCS-ist at the time, Ly Directly based on ("inspired"-shor) a slightly earlier (first-rejected) quantum alg. of Dan Simon) (CS postdoc at Univ. Montreal. Advisor: G. Brassard, influential early basically into crypto brossard asked him to look into Q.C. He did for a bit, published "Simon's Alg," Got interested in networking, left academia, went to networking & security product group at MSFT. Many gears later, C. Fuchs polled some Q.C. liminaries (Deutsch, Shor, etc.) about their work, and if Everett's MWI was influential in their thinking...

Simon: "Who's Everett, and what's his interpretation?"

"I was approaching the problem purely from a computer scientist's perspective. I learned the absolute bare minimum of physics I needed to be able to understand the computer science question, which (as I saw it) was, "these crazy people are claiming that if you add these very-weird-yet-theoretically-physically-implementable functions to a computer, then you should be able to do amazing things with them. Prove them right or wrong." I actually started out trying to prove that quantum computing was useless, and eventually narrowed down the difficult, unsimulateable part [of QC's power] to, "Rotate, compute, rotate". That helped guide my search for a computationally interesting quantum algorithm."

(We'll talk about "rotate, compute, rotate" in Lecture 2. In brief, the one thing a Q.C. can de is... the Boolean Fourier Transform. Which is a rotation. In 10500 dimensional space.) (As he says, don't need physics QC can be boiled down to classical comp with a lin. alg. twist. Shor's response also emphasized he didn't think about 10500 parallel universes, and he thought that gave a misleading picture of Q.C.'s power. E.g. ne don't think Q.C.'s an efficiently solve "NP-complete probs,") (So next time I want to convince you that Q.C. is not mysterious & crazy. But it is fun to talk about the moteries of 10500 parallel universer some times :)